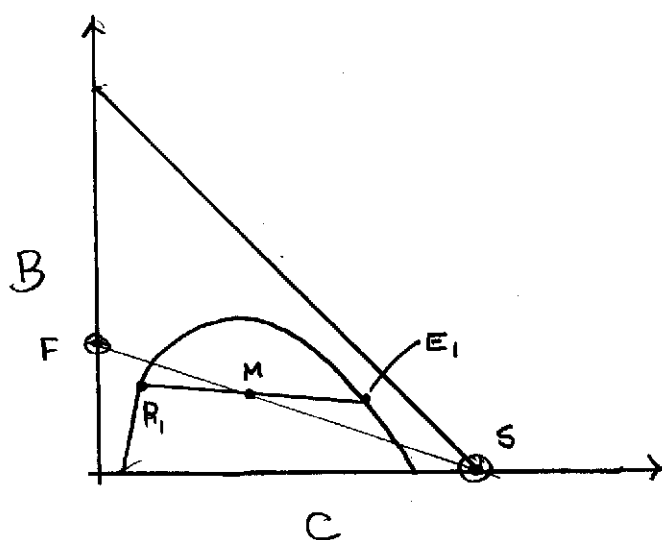
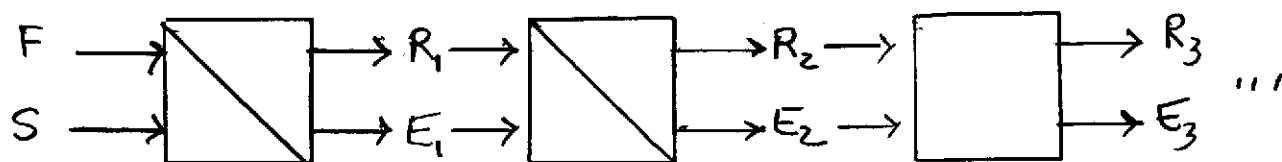


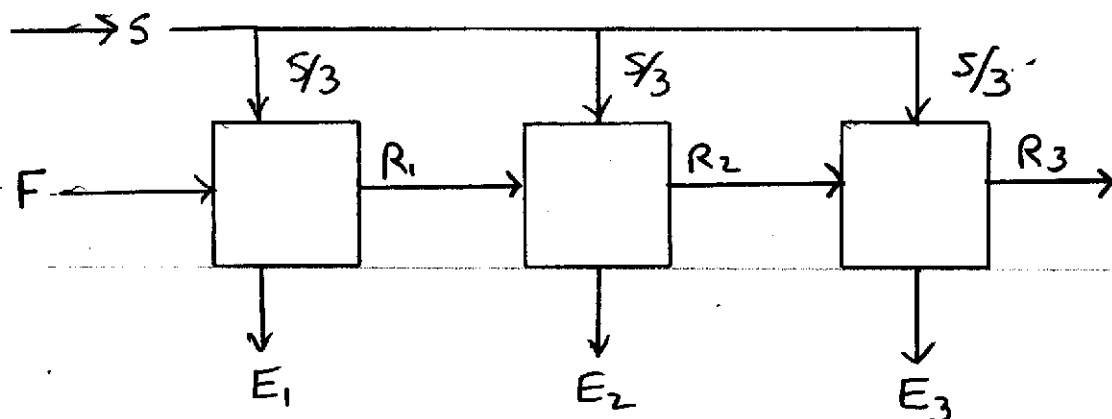
8-1

Cascades of Equilibrium Stages

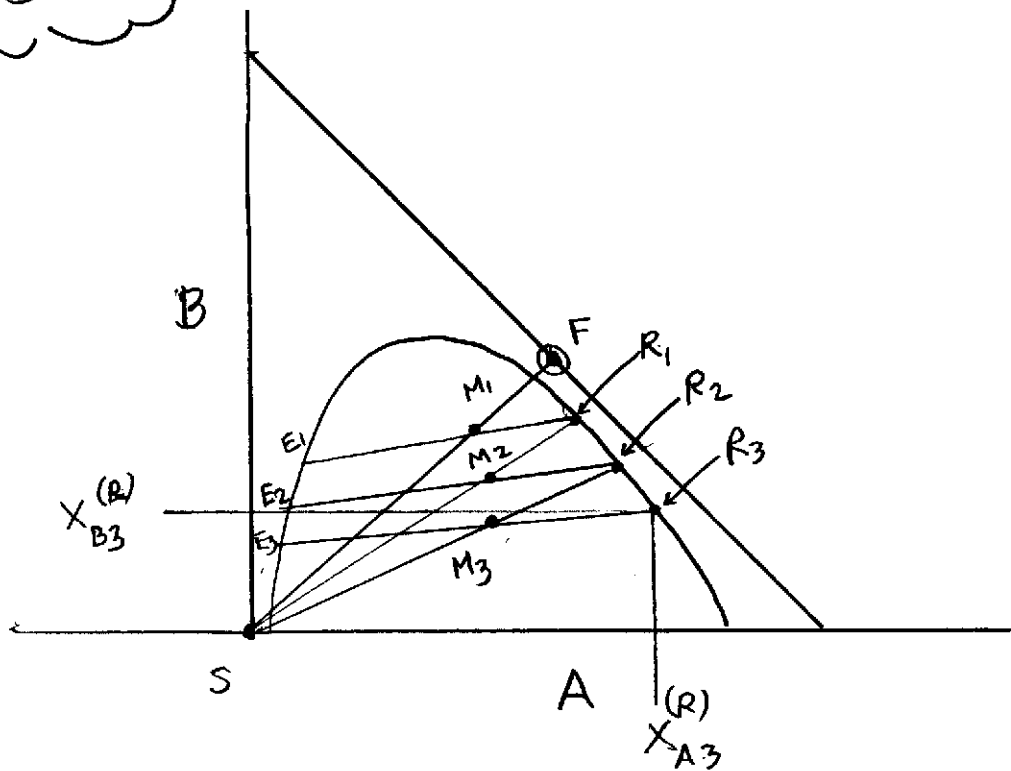
Series



Cross Flow (Repeated application of solvent)



8-2

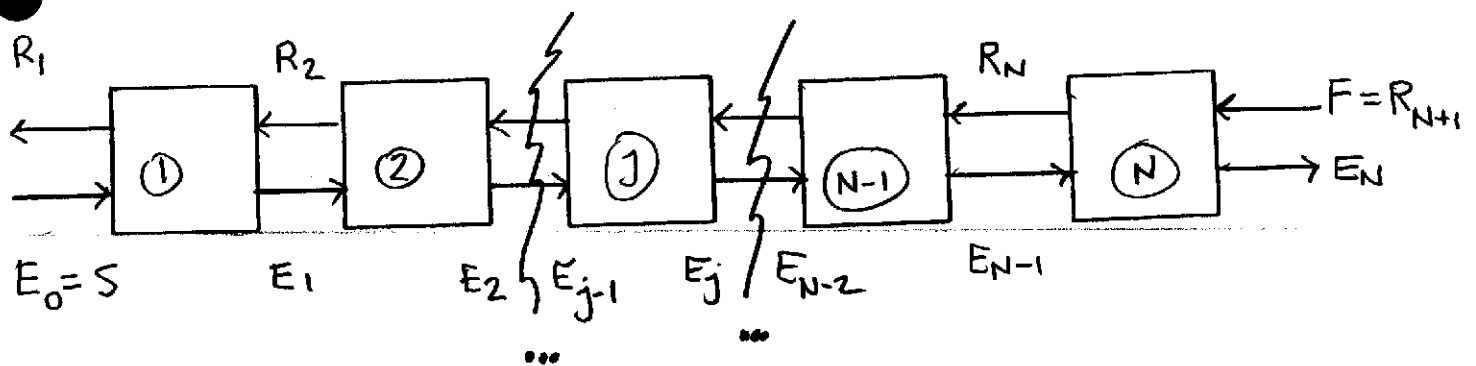


Notes and comments

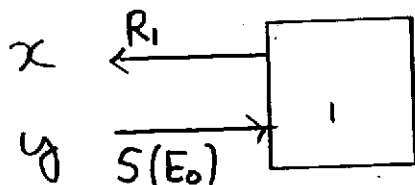
- (1) $n = 2, 3, 4, \dots$
- (2) Solvent does not need to be equally partitioned
- (3) Solvent concentration may vary from stage to stage
- (4) Multiple solvents could be employed (Stage 1 use S₁, Stage 2 use S₂, etc).

8-3

Countercurrent extractions



$$X_{A1}^{(R)} = X_{A1} \leftarrow \text{simplex nomenclature}$$



$$X_{A0}^{(S)} = y_{A0} \leftarrow$$

External Balances

$$(1) \quad E_0 + R_{N+1} = R_1 + E_N$$

$$(S + F = R_1 + E_N)$$

$$(2) \quad E_0 y_{A0} + R_{N+1} x_{A,N+1} = R_1 x_{A1} + E_N y_{AN}$$

$$(3) \quad E_0 y_{B0} + R_{N+1} x_{B,N+1} = R_1 x_{B1} + E_N y_{BN}$$

(or "C")

8-4

Equilibrium Relationships

(1) Each stage is an equilibrium contact so streams leaving a stage are at equilibrium.

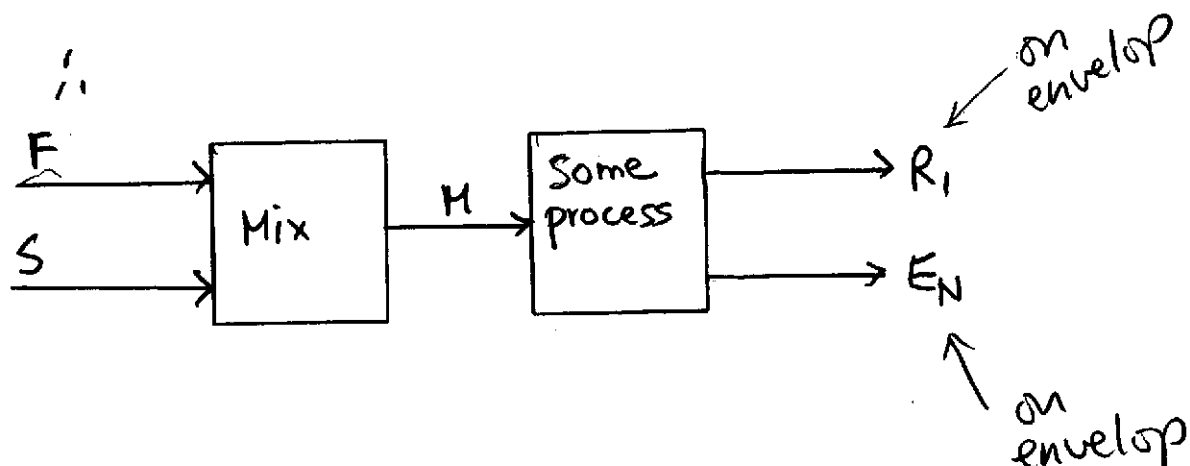
$$\therefore E_1 = EE(R_1) \quad E_2 = EE(R_2) \text{ etc.}$$

(same subscript)

(2) Streams at equilibrium must lie on phase envelop.

$$E_1, R_1, E_2, R_2, \text{ etc}$$

(3) streams leaving the process are equilibrium streams, but not at equilibrium with each other.



8-5

This "black box" separation process has a mixing point M and its own balances.

Overall Balance

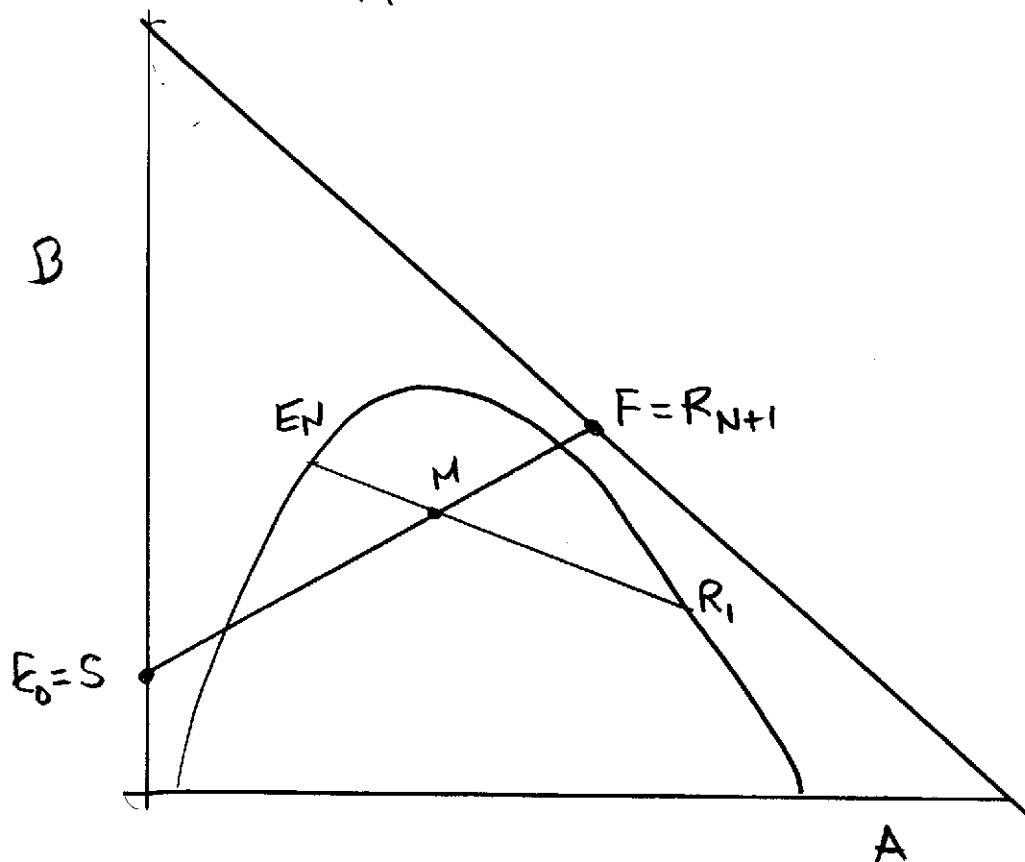
$$E_0 + R_{N+1} = M = E_N + R_1$$

Imaginary Mixing Op

$$S + F \equiv M \equiv E_0 + R_{N+1}$$

Imaginary Separation Process (NonEq)

$$M \equiv E_N + R_1$$



8-6

The coordinates of "M" can be found by ILAR or analytically.

$$X_{AM} = \frac{E_0 y_{A0} + R_{N+1} X_{AN+1}}{E_0 + R_{N+1}}$$

$$X_{BM} = \frac{E_0 y_{B0} + R_{N+1} X_{BN+1}}{E_0 + R_{N+1}}$$

Difference points and stage by stage calculations.

In the "real" process, we will need to do stage by stage calculations (in order to learn the number of stages required).

Given F , X_{AN+1} , X_{BN+1} (or C)
 S , y_{A0} , y_{B0} (or C)
 * , X_{A1} , X_{B1} (or C)

① Find y_{AN} , y_{BN} , E_N , R_1

* Assume specification for exit raffinate given in problem.

8-7

Note, these are external balances

(2) Start at stage 1.

E_1 is in equilibrium with R_1
(like $x_1 = f(y_1)$ in BD)
 $\therefore$ on same tie line

(3) Streams E_1 and R_2 are
passing streams
(like $y_{j+1} = f(x_j)$)

Relate compositions by
material balance.

Note Stream R_2 is in
equilibrium with E_2 and
therefore lies on phase
envelop. (Find R_2)

(4) Stream E_2 relates to R_2
by equilibrium (tie-line)

(5) Streams E_2 and R_3 are
passing streams