# Exploiting Radio Fingerprints for Simultaneous Localization and Mapping

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Simultaneous localization and mapping (SLAM) is paramount for unmanned systems to achieve self-localization and navigation. It is challenging to perform SLAM in large environments, due to sensor limitations, complexity of the environment, and computational resources. We propose a novel approach for localization and mapping of autonomous vehicles using radio fingerprints, for example wireless fidelity or long term evolution radio features, which are widely available in the existing infrastructure. In particular, we present two solutions to exploit the radio fingerprints for SLAM. In the first solution—namely Radio SLAM, the output is a radio fingerprint map generated using SLAM technique. In the second solution—namely Radio+LiDAR SLAM, we use radio fingerprint to assist conventional LiDAR-based SLAM to improve accuracy and speed, while generating the occupancy map. We demonstrate the effectiveness of our system in three different environments, namely outdoor, indoor building, and semi-indoor environment.

Simultaneous localization and mapping (SLAM) is essential for unmanned system to carry out high level tasks, such as navigation and exploration in unknown environments.<sup>1</sup> SLAM allows to build a map and localize an autonomous vehicle at the same time. With tremendous improvements in computing power and availability of low-cost sensors, SLAM is now used for many robotics applications. One example is DARPA subterranean challenge,<sup>2</sup> which explored innovative technologies to rapidly map, navigate, and search in subterranean domains using robotic systems.

Odometry is commonly used to estimate the position of vehicle. However, long period of localization often suffers from accumulative error. SLAM is considered as a fundamental problem in robotics community. The core of SLAM is to correct the drifting error of odometry by recognizing if a place has been revisited by the robot. Efficient SLAM solvers have been introduced and their performance has been evaluated with a variety of sensors (e.g., visual camera and LiDAR). We are now entering an era of robust perception, which considers the long-term operation of the vehicle in large environments.

With the growing popularity of smartphones, most existing buildings have been deployed with wireless fidelity (WiFi) and long term evolution (LTE) networks for communication purposes.<sup>3</sup> Such radio network can be exploited for localization and mapping with low-hardware requirement and computational cost.<sup>4</sup>



FIGURE 1. Overview of the SLAM solutions based on different sensors.

In contrast to visual camera and LiDAR, which measure the similarity of observations by scan matching or feature matching, the radio infrastructure provides an opportunity for SLAM in a cost-efficient way. Each base station carries a unique ID, which tells if vehicle is in the proximity. Particularly, fingerprinting-based approach uses a set of radio signals to represent location<sup>5,6</sup> which is more accurate when compared to model-based approaches.

This article provides an overview of the current status of SLAM with emphasis on the challenges and future research directions. An illustration of the SLAM approaches based on different sensors is shown in Figure 1. For Radio SLAM, the SLAM is simultaneous localization and radio fingerprint mapping, while the LiDAR SLAM is with the mapping of range scanning. Each approach has its advantages as well as challenges. For example, LiDAR gives an accurate representation of the environment, but it has issues during loop closure in perceptually degraded environment. Radio fingerprint uses a collection of radio signals to represent location, which is shown to be robust again environmental distortions when compared to visual or LiDAR-based approaches, but obtaining a precise position estimation is challenging, due to multipath signal propagation.

To utilize radio features in the existing infrastructure, we present two solutions to use radio fingerprints to perform SLAM. In the first solution—namely Radio SLAM, while generating the trajectory, we generate a radio fingerprint map using SLAM technique, where the produced radio map can be used for localization with the state-of-the-art fingerprinting-based approaches.<sup>3,7</sup> In the second solution—namely Radio +LiDAR SLAM, we use radio fingerprint to assist conventional LiDAR-based SLAM. While generating the trajectory, we also generate occupancy map and show that the mapping processing is faster than the conventional approach. We conducted experiments in three different environments to illustrate the effectiveness of our approach.

# SENSORS AND ALGORITHMS IN SLAM

Over the past decades, indoor positioning shows a growing popularity due to the increasing demand of location-aware applications.<sup>3</sup> SLAM addresses the problem of SLAM in unknown environment, which has achieved significant achievements over the past years. In this section, we review the popular sensors and algorithms used for SLAM.

#### Sensors Used for SLAM

Depending on the types of sensors, one can classify the SLAM into LiDAR SLAM, visual SLAM, mmWave SLAM, and WiFi SLAM. LiDAR SLAM uses LiDAR to create structural map of an environment. Visual SLAM utilizes camera to construct 3D model of the scene. Visual SLAM (for example ORB-SLAM3<sup>8</sup> and Superpoint<sup>9</sup>) has undergone significant upgrades in recent years due to the evolution of neural networks. mmWave carries massive amounts of data at high speed and low latency, which will soon become a fundamental component of 5G-and-beyond communication networks. The emerging mmWave technology opens new opportunity for localization and SLAM in both wireless and robotics community.<sup>10,11</sup> Although SLAM is used for some practical applications, several technical challenges prevent more general-purpose adoption. One challenge is the high computational cost in data processing, particularly when implementing SLAM on compact and low-energy embedded microprocessors.

With the development of Internet of Things and wireless communication,<sup>12,13</sup> urban environments are deployed with WiFi APs and LTE base stations, which can be exploited for SLAM. WiFi SLAM uses wireless signature and odometry for localization and radio mapping in unknown environments. Ismail et al.<sup>13</sup> proposed to estimate the pose of the vehicle with WiFi fingerprint sequence. Adhivarahan and Dantu<sup>12</sup> used WiFi to determine the coarse orientation between LiDAR submaps during online distributed mapping.

#### Algorithms in SLAM

Throughout the years, many techniques and algorithms have been proposed for SLAM,<sup>1</sup> including filtering-based solutions and graph-based solutions. The choice of the SLAM solution depends on sensors, computational resources, and applications. Graphbased approaches<sup>1</sup> formulate the SLAM as maximum likelihood estimation and has become one of the favorable approaches. The graph-based approach consists of two main modules: frontend and backend. The

frontend constructs pose graph based the sensor measurements, while the backend performs optimization based on the pose graph obtained from the frontend.

When the vehicle operates in the environment for a long time, the size of pose graph becomes unbounded, which prevents the optimization of SLAM in real time. A common technique is sparsification, which reduces the number of nodes in the graph by pruning.<sup>14</sup> The wrong loop closures impair the quality of the backend optimization. A number of strategies have been proposed to address this problem. Pfeifer et al.<sup>15</sup> presented maxmixture model for robust sensor fusion by combining expectation–maximization and nonlinear least square optimization. Several researchers also proposed to remove outliers at the frondend. For example Neira and Tardos<sup>16</sup> used joint compatibility test to reject spurious constraints.

# CHALLENGES AND OPEN RESEARCH DIRECTIONS

Despite tremendous improvements in SLAM, the implementation and deployment of SLAM in practice still face a number of challenges. In this section, we discuss the challenges as well as potential research trends in SLAM.

Data association with sensor fusion: The introduction of novel sensors innovates new applications in SLAM. The choice of sensors depends on the applications and environments. It is difficult to rely on a single sensor to achieve effective frontend sensor fusion due to the sensor limitations. For example, LiDAR enables the creation of occupancy map of an environment, but LiDAR does not work well in perceptually degraded environments (for example long corridors or tunnels). In our approach, each radio base station has a unique ID. This makes the data association easier, as entering the same area can be known by the base station ID.

Mapping in large environment: With a continuous operation in large scale environment, the size of map may become unbounded, which prevents the loop closure detection in real time. The design of efficient SLAM solutions with acceptable memory and computational cost is necessary. One solution is to develop efficient similarity searching algorithms to find potential loop closures. One example is Faiss library<sup>a</sup> from Facebook, which allows fast similarity search of dense vectors. Our approach uses radio signature as features to assist the conventional LiDAR SLAM to create a map in large environment. Another solution is to perform distributed SLAM with multiple robots. Mangelson et al.<sup>17</sup> proposed a mechanism called pairwise consistency maximization to filter out spurious loop closures between robots.

*Failure recovery mechanism:* Incorrect data association ruins the optimization in SLAM. To address this issue, researchers have proposed several techniques in the backend to deal with outliers.<sup>15,16</sup> These methods determine the validity of loop closure by checking the residual error during optimization. Despite the efforts made on the backend optimization, current SLAM solutions are susceptible to false loop closures, which lead to poor estimation and prevent the exclusion of spurious loop closures afterward. Therefore, a mechanism to recover from such failures is a future research trend.

Semantic mapping: In contrast to the geometric representation of the environment, semantic mapping<sup>18</sup> provides an opportunity to understand the scene and interact with the environment. This technique represents the scene in an unambiguous and informative way, enabling large scale autonomy and robust perception in highly unstructured environments. The development of semantic mapping is still at its early phase and new tools for example deep learning will obviously hasten the progress of semantic SLAM in real applications.

# RADIO SLAM AND RADIO+LIDAR SLAM

Radio signals are commonly used for localization in many commercial and industrial applications.<sup>3</sup> We propose to use radio fingerprints as alternative to the conventional range-based or visual-based SLAM. We present two solutions to use radio fingerprints for SLAM. In the first solution-Radio SLAM, we use radio fingerprint to estimate the trajectory of a robot and generate a radio map of the environment. In the second solution-Radio+LiDAR SLAM, we incorporate LiDAR by scan matching to produce a more accurate trajectory and generate an occupancy map of the environment. An overview of the proposed approach is shown in Figure 2. The similarity check and SLAM are working in parallel in the proposed approach. The similarity check is used to determinate if two locations are in the same place (i.e., loop closures). Meanwhile, the SLAM takes the loop closures as inputs to optimize the trajectory. Our approach provides an efficient way to perform SLAM in large scale environment, while the conventional LiDAR-based SLAM falls short due to the lack of robust data association algorithms.

<sup>&</sup>lt;sup>a</sup>[Online]. Available: https://faiss.ai/

Input:Radio finge	Input:LiDAR scans		
Similarity computing for close fingerprints Training mean and variance model	Loop closure detection by similarity comparision First pose graph optimization Output:Trajectory est. + radio map	Registration of LiDAR scans in proximity LiDAR loop closures by scan matching Second pose graph optimization	
Offline model generation	Radio SLAM	+occupancy map Radio+LiDAR SLAM	

FIGURE 2. Overview of Radio SLAM and Radio+LiDAR SLAM.

### Overview of Graph-Based SLAM

Graph-based approach formulates the SLAM as maximum likelihood estimation. We denote the pose of robot as  $\mathbf{x} = \{x, y, \theta\}$ , where x and y are the 2D location and  $\theta$  is the heading of the robot. The sensors carried by the robot are used to infer the constraints. Graph optimization aims to find the best configuration of nodes to minimize the following equation given constraints  $\mathbb{C}$ :

$$\underset{\mathbf{x}}{\operatorname{arg\,min}} \sum_{(\mathbf{x}_i, \mathbf{x}_j) \in \mathbb{C}} (\mathbf{z}_{ij} - \hat{\mathbf{z}}_{ij} (\mathbf{x}_i, \mathbf{x}_j))^{\mathsf{T}} {\Sigma_{ij}}^{-1}$$

$$\times (\mathbf{z}_{ij} - \hat{\mathbf{z}}_{ij} (\mathbf{x}_i, \mathbf{x}_j))$$
(1)

where, the subscript i and j are used to denote the time reported from the sensor. We use  $\mathbf{z}_{ij}$  to represent the constraint and its associated weight is denoted as covariance matrix  $\Sigma_{ij}$ . The constraint can be either successive odometry or loop closure inferred from nonsequential observations. Two types of loop closures are involved in optimization, namely radio-based loop closures and LiDAR-based loop closures. The former is represented as the distance, which is determined by the fingerprint similarity, as shown in the "Radio SLAM based on Fingerprint Similarity" section. The latter is denoted as the rigid body transformation by LiDAR scan matching. We consider a pair < i, j >as WiFi loop closure if the similarity score is over a threshold. We treat a pair  $\langle i, j \rangle$  as LiDAR loop closure if the scan matching satisfies a predefined condition. Those loop closures (i.e., WiFi loop closures and LiDAR loop closures) and odometry are used as constraints to optimize the trajectory of the robot through pose graph optimization, as shown in (1).

#### **Fingerprint Similarity**

Given a received signal strength (RSS) from a base station, it is straightforward to know if an area has been visited by the robot, since each reported RSS is associated with a unique ID. Estimating the precise transformation between two fingerprints turns out to be tricky, since radio signal neither reports distance nor bearing information. In our approach, the closeness of two locations is determined by the fingerprint similarity. We train a model to represent the distance and variance of radio-based loop closures given the similarity of two location fingerprints, which will be detailed in the "Radio SLAM based on Fingerprint Similarity" section.

We represent a fingerprint at pose  $\mathbf{x}_t$  as a pair  $\mathbf{F}_t = (\mathbf{f}_t, \mathbf{x}_t)$ .  $\mathbf{f}_t$  consists of RSS from L access points (APs) or base stations:  $\mathbf{f}_t = \{f_{t,1}, \ldots, f_{t,L}\}$ . Let  $L_i$  and  $L_j$  denote the number of detections in  $\mathbf{f}_i$  and  $\mathbf{f}_j$ , respectively.  $L_{ij} = |\mathbf{f}_i \cap \mathbf{f}_j|$  represents the common APs or base stations in  $\mathbf{f}_i$  and  $\mathbf{f}_j$ . We use a cosine similarity metric to measure the similarity  $\cos(\mathbf{F}_i, \mathbf{F}_j)$  between two fingerprints  $\mathbf{F}_i$  and  $\mathbf{F}_j$ 

$$s_{ij} = \cos(\mathbf{F}_i, \mathbf{F}_j) = \frac{\sum_{l=1}^{L_{ij}} f_i^l f_j^l}{\sqrt{\sum_{l=1}^{L_i} (f_i^l)^2} \sqrt{\sum_{l=1}^{L_j} (f_j^l)^2}}.$$
 (2)

# Radio SLAM Based on Fingerprint Similarity

Parameterization of the constraint is required to optimize the pose graph. For odometry-based constraint, the parameter is obtained from the motion model. We need to derive a model to represent the distance and uncertainty given two fingerprints. Our solution is to train such model by passing over odometry and radio recordings. Although odometry error accumulates over long period, it is sufficiently small for a short distance traveled. Therefore, we compute the degree of similarity for close fingerprint pairs, which are annotated with the distance determined by the odometry. As a result, we obtain a set of K training samples:  $\{s_k, d_k\}_{k=1}^K$ , where  $s_k$  is the fingerprint similarity and  $d_k$  is the physical distance of the fingerprint pair. We then train a model, which features the mean distance  $\mu(d|s)$  and variance var(d|s) given a similarity value s by binning

$$\mu(d|s) = \frac{1}{c(\mathbf{b}(s,r))} \sum_{k \in \mathbf{b}(s,r)} d_k^2$$
  
var $(d|s) = \frac{1}{c(\mathbf{b}(s,r))} \sum_{k \in \mathbf{b}(s,r)} (d_k - \mu(d|s))^2$  (3)

where,  $\mathbf{b}(s, r)$  denotes the samples that sit in the interval r around a similarity value s.  $c(\cdot)$  counts the number of samples. Equation (3) gives the covariance matrix for radio-based loop closure for (1). To optimize the trajectory with (1), we need to find the constraints for nonconsecutive poses. We compute the similarity  $s_{ij}$  between two recorded fingerprints  $F_i$  and  $F_j$  if the distance traveled by the robot is larger than a predefined thresholds (100 meters). The distance  $z_{ij}$  is

Environment	Traj. length (m)	Traj. duration (s)	WiFi MAC per scan/ total MAC	LTE CellID per scan/total LTE	Odom. (m)	WiFi SLAM (m)	LTE SLAM (m)
SUTD outdoor	5171.3	5494.7	88.23/4488	18.74/170	75.06	8.82±3.94	18.38±10.70
SUTD indoor	1114.9	3092.1	118.34/1921	19.49/193	10.01	3.69±2.21	5.18±2.59
NTU semi- indoor	1072.6	2583.9	48.88/1046	16.59/85	51.98	4.48±2.98	12.22±10.95

**TABLE 1.** Description of the data collected in three environments and accuracy evaluation of pure odometry, wifi SLAM, and LTE SLAM (mean and standard deviation in meters).

obtained based on the pretrained model in (3). We add a tuple  $\langle \mathbf{x}_i, \mathbf{x}_j, z_{ij} \rangle$  as a loop closure if the similarity  $s_{ij}$  exceeds a threshold  $\vartheta_s$ . Based on the radio loop closures, we optimize (1) using g20 with Levenberg– Marquardt solver.<sup>1</sup>

### Radio+Lidar SLAM

Based on the trajectory obtained from Radio SLAM, we further refine the trajectory by fusing LiDAR scans. This is achieved through a second pose graph optimization by considering LiDAR constraints (as shown in Figure 2). By LiDAR scan registration, a precise transformation between two poses can be computed. A common method is iterative closest point (ICP), which minimizes the sum of square distance (i.e., fitness score) between correspondences in two scans. We consider the following two manners to incorporate LiDAR measurements.

- Registration of LiDAR scans in proximity: we perform ICP for the consecutive LiDAR scans to correct the short-term odometry errors. The odometry measurement is used as an initial guess of ICP algorithm to avoid the convergence to local minima.
- LiDAR loop closures: based on the optimized trajectory from Radio SLAM, we perform the LiDAR scan matching if the displacement between two poses is smaller than a threshold. We consider a LiDAR loop closure if the fitness score and the matching points satisfy certain criteria. This step determines loop closures between nonconsecutive poses with a better accuracy when compared to radio fingerprints. We perform the second pose graph optimization by minimizing (1) again but considering the new constraints from LiDAR scan matching. The output of Radio +LiDAR SLAM is occupancy map (the same as the conventional LiDAR SLAM), which can be used for the navigation and path planning for autonomous vehicles.

### **EXPERIMENTAL RESULTS**

#### Experimental Setup

The experiments were performed using a Clearpath Husky vehicle. We evaluated the effectiveness of the proposed algorithm in three different environments, which consist of Singapore University of Technology and Design (SUTD) campus (outdoor, approx. 75000 m<sup>2</sup>), SUTD building (indoor, approx. 5000 m<sup>2</sup>), and Nanyang Technological University (NTU) carpark (semi-indoor, approx. 5100 m<sup>2</sup>). Five Xiaomi Max3 smartphones were placed on the robot to scan WiFi APs and LTE base stations. Each phone is configured to scan one LTE band in Singapore. Wheel odometry were recorded at a frequency of 10 Hz. Hokuyo UST-20LX LiDAR was used for LiDAR scans. In outdoor experiment, we obtain the ground truth by Android location service. For indoor environments, we have created an indoor map of the environment based on GMapping<sup>b</sup>. With the created indoor map, we apply adaptive Monte Carlo localization (AMCL) for ground truth based on probabilistic algorithms. Particularly, AMCL tracks the 2D pose of the robot against a known map based on particle filtering. The algorithm performs pose prediction and weights update of particles based on odometry and 2D LiDAR, respectively. During our implementation, the map resolution is set to be 0.05 m and position of the robot is known during the initialization of the particle filtering. Throughout the experiments, the robot traveled at an average speed of 0.4 m/s. Table 1 summarizes the data collected in three environments.

The models of WiFi and LTE generated with a binning size of 0.05 are visualized in Figure 3(a) and (b), respectively. As can be seen from these figures, given a similarity value, LTE model gives large distance and standard deviation when compared to WiFi model. For NTU environment, we obtain mean

<sup>&</sup>lt;sup>b</sup>[Online]. Available: http://wiki.ros.org/gmapping/



FIGURE 3. A comparison of the models in three different environments and visualization of ground truth, odometry, LTE SLAM, and WiFi SLAM in NTU semi-indoor environment. (a) WiFi model. (b) LTE model. (c) Trajectory estimation with different algorithms in NTU environment.

distance of 30.25 m and standard deviation of 22.13 m of LTE model given a similarity value of 0.8, which are larger when compared to WiFi model (mean distance of 3.79 m and standard deviation of

2.70 m). To detect radio-based loop closures, we use a similarity threshold of  $\vartheta_s$ =0.7 for both WiFi and LTE.

# **Evaluation of Radio SLAM**

The comparison of the track between odometry, LTE SLAM, WiFi SLAM, and ground truth in NTU environment are visualized in Figure 3(c). Table 1 summarizes the results of three experiments. As can be seen from this table, our proposed radio SLAM is more accurate when compared to pure odometry. For WiFi SLAM, indoor environments give better accuracy when compared to outdoor environment. For example, in SUTD indoor and NTU semi-indoor, we obtain a localization accuracy of 3.69 and 4.48 m, which are better than the accuracy of SUTD outdoor environment (8.82 m). Although a large number of APs are detected in outdoor environment, low signal strength values result in more uncertainty, since these APs inside buildings are far away from the moving path of the robot. In general, WiFi SLAM gives better accuracy than LTE SLAM, due to the dense WiFi coverage in the environment. For NTU semi-indoor environment, we obtain an accuracy of 4.48 m with WiFi SLAM, which is an improvement of 63.34% when compared to LTE SLAM (12.22 m).

# Evaluation of Radio+LiDAR SLAM

Based on the optimized trajectory obtained from Radio SLAM, we perform LiDAR scan matching to further improve the accuracy based on the technique in the "Radio+LiDAR SLAM" section. A valid match is identified if the fitness score is smaller than 0.1 and the matching points are larger than half of the average number of points in both scans. For NTU carpark semiindoor environment, our WiFi+LiDAR SLAM provided a localization accuracy of 0.84 m, while GMapping gave a localization accuracy of 4.31 m and failed to correct odometry error.

We tested our approach on Intel Core i7-6700HQ CPU with 2.6 GHz frequency and 8 GB RAM. We observe that the time consumed for WiFi SLAM is insignificant as compared to time of data recording, while the computational time for WiFi+LiDAR SLAM is much longer, due to the high cost of LiDAR scan matching. The time required for performing one WiFi similarity comparison with 44 MAC addresses is 0.029 ms, while the time required for one LiDAR scan matching of 600 points is 13.04 ms. Therefore, LiDAR scan matching is the current bottleneck of the proposed Radio+LiDAR SLAM.

To visually inspect the quality of the optimized trajectory, we generate the occupancy grid map by evaluating the respective grid using LiDAR scans at optimized poses, as shown in Figure 4. We also



FIGURE 4. Comparison of the occupancy maps created by different approaches. (a) WiFi+LiDAR SLAM. (b) GMapping. (c) Ground truth.

compared our results with GMapping, which applies particle filtering-based approach for SLAM. The map generated with GMapping is not consistent with the true map due to the drift of odometry. This can be seen from the nonoverlapping boundaries representing the walls in Figure 4(b). The quality of the map is significantly improved by the fusion of WiFi in Figure 4(a).

A comparison of the path required for mapping large indoor building based on different approaches is shown in Figure 5. To ensure the quality of map using the conventional LiDAR-based SLAM (i.e., GMapping), we have to design a cumbersome strategy for the robot (see the blue path in Figure 5 with a total travel time of 8619.2 s) to traverse different small regions and avoid large loops, which normally lead to mapping failure due to the lack of LiDAR loop closures to correct the large odometry drift after long distance travel. Our approach uses radio fingerprints to assist the conventional LiDAR-based SLAM. The proposed approach provides a comparable mapping quality when compared to the conventional LiDAR-based SLAM, but at a much faster scanning speed. It is important to point out that the deployment of radio infrastructure in the testing area is a necessity to perform the proposed radio SLAM. The accuracy will be decreasing if the density of APs or base stations is low.



**FIGURE 5.** Illustration of the path traveled by the conventional LiDAR-based SLAM (i.e., GMapping) and our proposed Radio +LiDAR SLAM for the mapping of a large indoor building.

#### CONCLUSION

This article discussed the favorable sensors, popular algorithms, and critical challenges in SLAM. We proposed to use opportunistic WiFi and LTE signals, which are available in the existing infrastructure to perform SLAM. The performance of the system is verified in three different environments. We achieve a positioning accuracy of less than 10 m using WiFi SLAM in all test environments. In addition, we present Radio+LiDAR SLAM that integrates LiDAR scan matching to improve the accuracy. The proposed approach produced comparable map quality versus LiDAR-based SLAM but at a much faster scanning speed. Our approach makes use of the existing radio infrastructure for sensing and has no assumption about the locations of the base stations. In future, we would like to test our approach in different environments to validate the generalization of the proposed approach. Another direction to investigate the possibility to use the created occupancy map for the navigation and path following of autonomous vehicles.

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