

# Auburn University GAVLAB

## GNC & UGV Research

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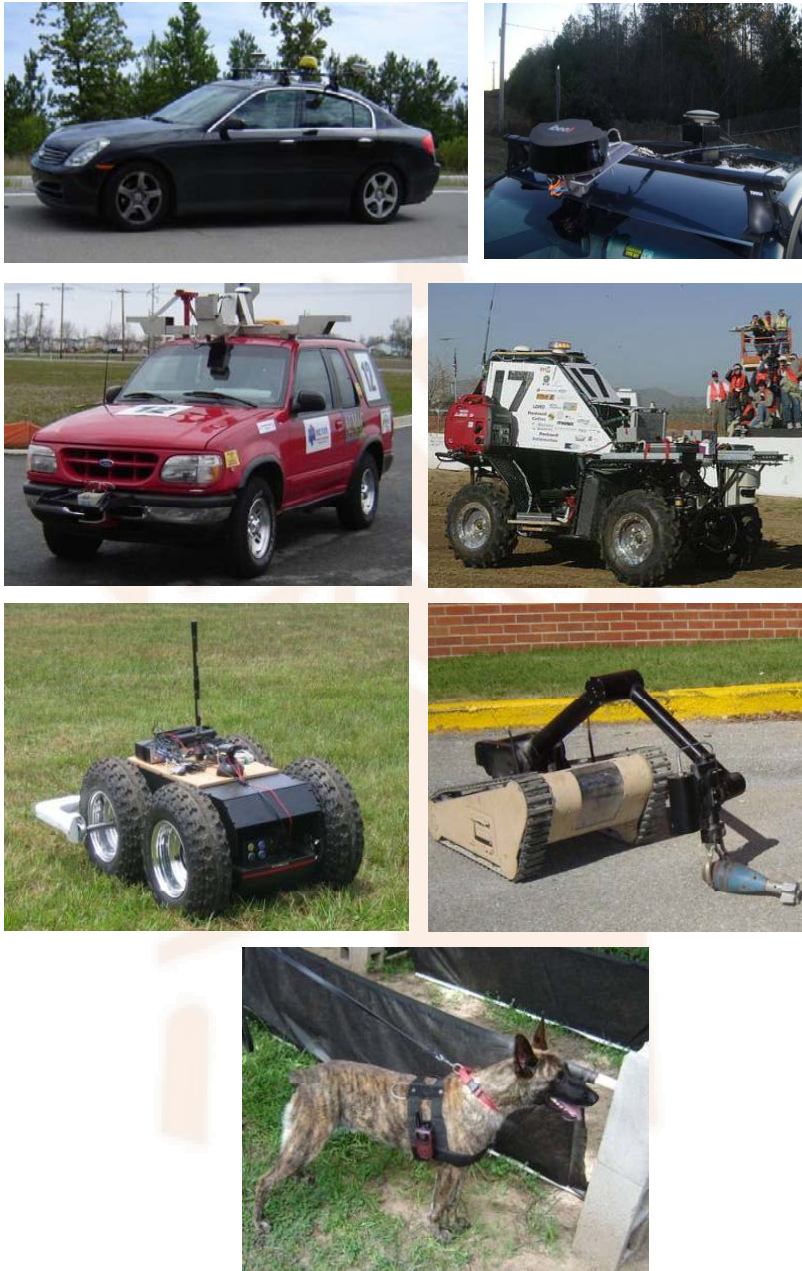


Currently 20 Students (8 PhD, 8 MS, 4 BS) at \$500K/year

- Vehicle modeling
- Vehicle parameter estimation
- Determination of rollover propensity
- Vehicle sensor fusion/integration
- GPS/INS navigation
  - Using various grade IMUs and receivers
  - Analysis of different aiding techniques
  - Loosely, Tightly, and Ultra-Tightly Coupled Algorithms
- IMU & laser scanner fusion
- Sensor characterization and modeling
- Development of a software GPS receiver
- High speed control of ground vehicles

# GAVLAB Resources

## Instrumented and Automated Vehicles



## Various Grade GPS Receivers Lidars, Cameras. etc



## Various Grade IMUs





# NCAT Test Track

- Two Lane Track
- 1.7 Mile Oval
- Asphalt Instrumentation
- Well Surveyed
  - Level
  - 2° Crowns
  - 8° Banked Turns
- 802.11 and wireless serial communication around entire facility
- RTK system setup with corrections available in all paved areas



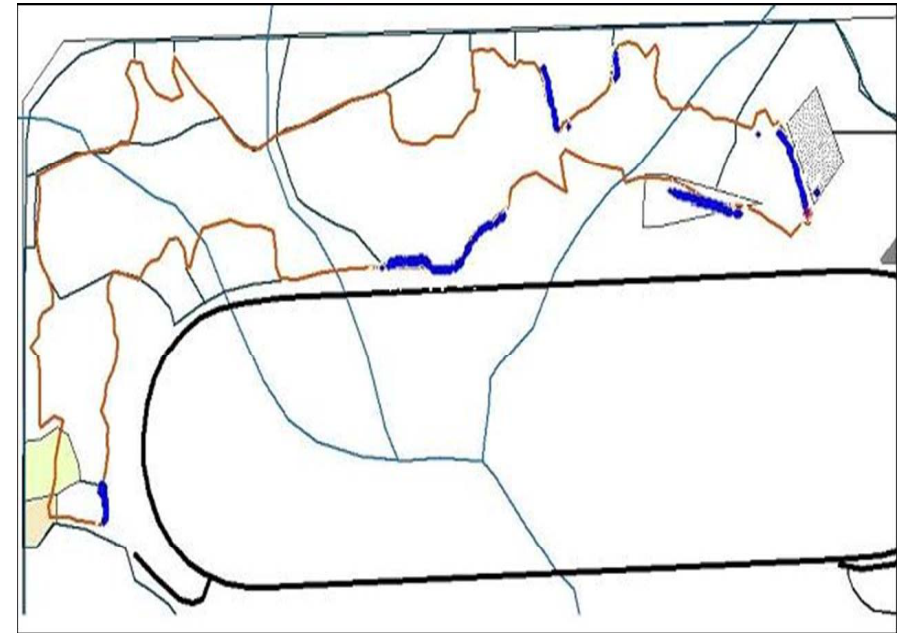
Test facility is available for validating vehicle modeling and estimation algorithms using instrumented vehicle test-beds



# Auburn's Mini Baja Track

- Approximately 2.08 miles long, 20 ft wide, and 90 ft of elevation change with various types of terrain
- Average Speed in a Mini Baja car is 15 mph (top speed of 35+ mph)
- UGV proving ground

Located adjacent to the 1.7 mile NCAT paved test track

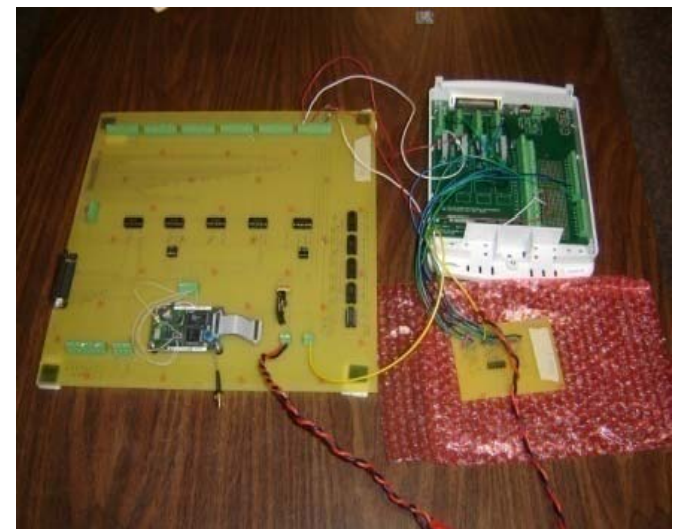


Red—Baja Course  
Blue – Navcom Starfire GPS Coverage  
Black—NCAT Track



# Real-Time L1 GPS Software Receiver

- NordNav R30:
  - Can record raw IF samples and replay the data through the receiver multiple times
  - Built-in tracking loops are reconfigurable
  - Can open up the tracking loops to provide >50 Hz GPS data
  - Ability to simulate various scenarios (signal loss, multi-path, loss of specific satellites, etc.)
- GAVLAB DIv1
  - All of the above features
  - User-definable tracking loop framework allows use of external inputs (INS) for real-time use



- DRTK
  - Performing accurate relative position
  - Integrating DRTK with INS (align leader/follower IMU)
- GPS Error Compensation
  - Remove erroneous errors caused by multi-path or foliage
- GPS Simulator
- Terrain Characterization
  - Generate simulated terrain
  - Characterize real terrain for simulation
- Vehicle Modeling
  - Estimate friction to predict stopping distance
  - Estimate rollover prediction
- IMU integration with Object Registration
  - Develop object registration based navigation
  - Align leader/follower IMU using object registration
- Experimental Studies
  - Setting up UGV for experimental validation

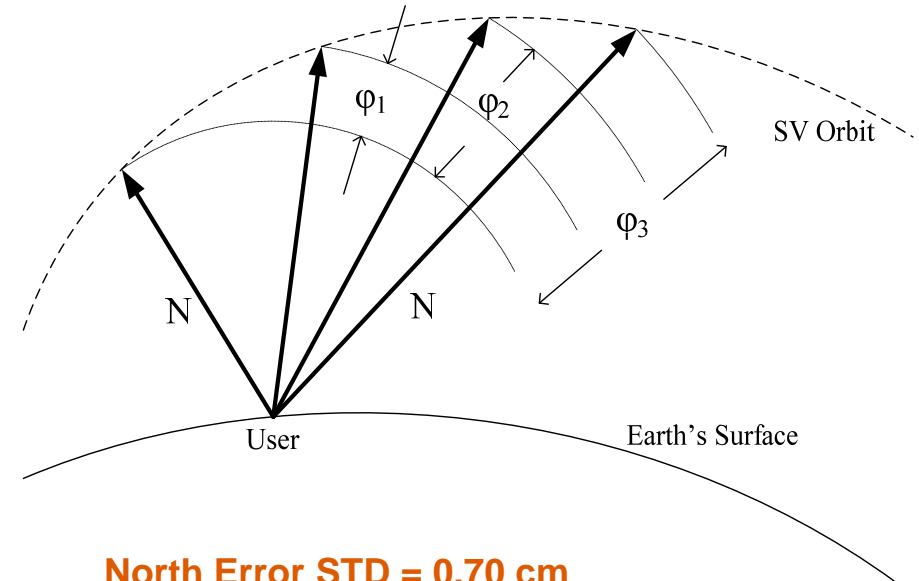


# Recent Technology Integration

- DRTK integrated into ANS with GDRS
  - Evaluated L1 only DRTK performance to fit existing ANS capabilities
- DRTK integrated into War Fighter with Lockheed Martin (i.e. CAST) in January
- Terrain characterization and vehicle modeling are being integrated into the ANS simulation environment
- Object registration work is being incorporated into a SLAM algorithm for GDRS work funded by the ARL

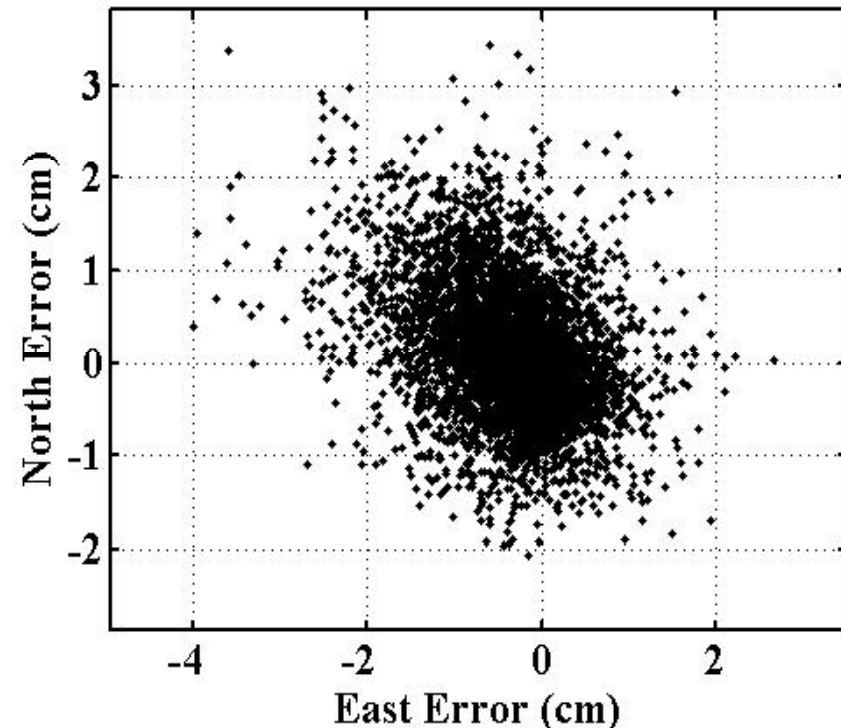
# DRTK Overview

- Code based range measurements have meter level accuracy
- Phase based range measurements are near millimeter level accurate, but are ambiguous
- Relative position measurements are formed by differencing range measurements between two receivers



North Error STD = 0.70 cm

East Error STD = 0.68 cm



## Carrier Phase Signal Model

$$\phi_A^j(t) = \phi_A - \phi^j + N_A^j + f\delta^j + f\delta_A - \gamma_I + \tau_T + Q_A^j$$

$$\phi_B^j(t) = \phi_B - \phi^j + N_B^j + f\delta^j + f\delta_B - \gamma_I + \tau_T + Q_B^j$$

## Single Difference

$$\Delta\phi_{AB}^j = \phi_{AB}^j(t) + N_{AB}^j + f^j\delta_{AB}(t) + Q_{AB}^j$$

$$\Delta\phi_{AB}^k = \phi_{AB}^k(t) + N_{AB}^k + f^k\delta_{AB}(t) + Q_{AB}^k$$

# DRTK – L2/L1 and L1 Only Comparison

- DRTK accuracy and reliability analysis with single and dual frequency GPS
- Testing performed to determine feasibility of implementing DRTK with current ANS hardware

## Accuracy

### Mean Error

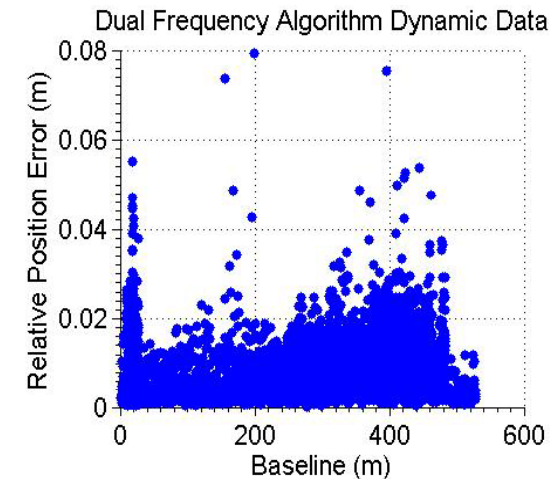
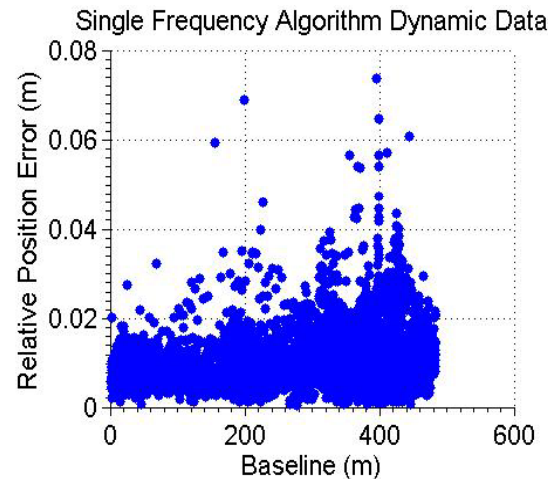
Single – 1.1 cm

Dual – 0.9 cm

### Standard Deviation

Single – 0.7 cm

Dual – 0.6 cm

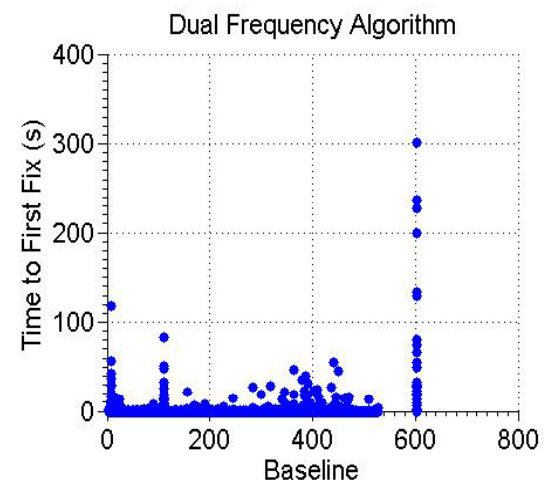
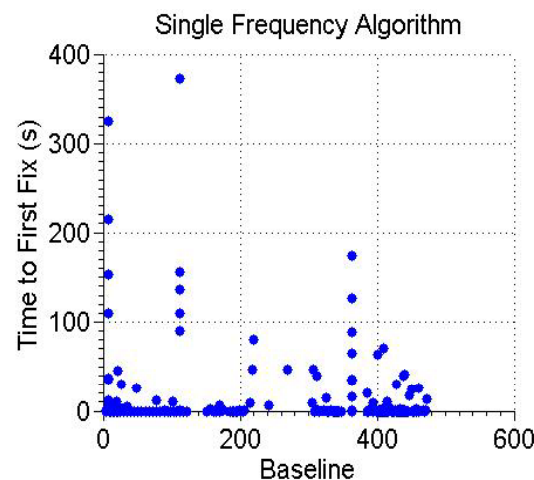


## Time To First Fix

### Mean Time to First Fix

Single – 7.7 seconds

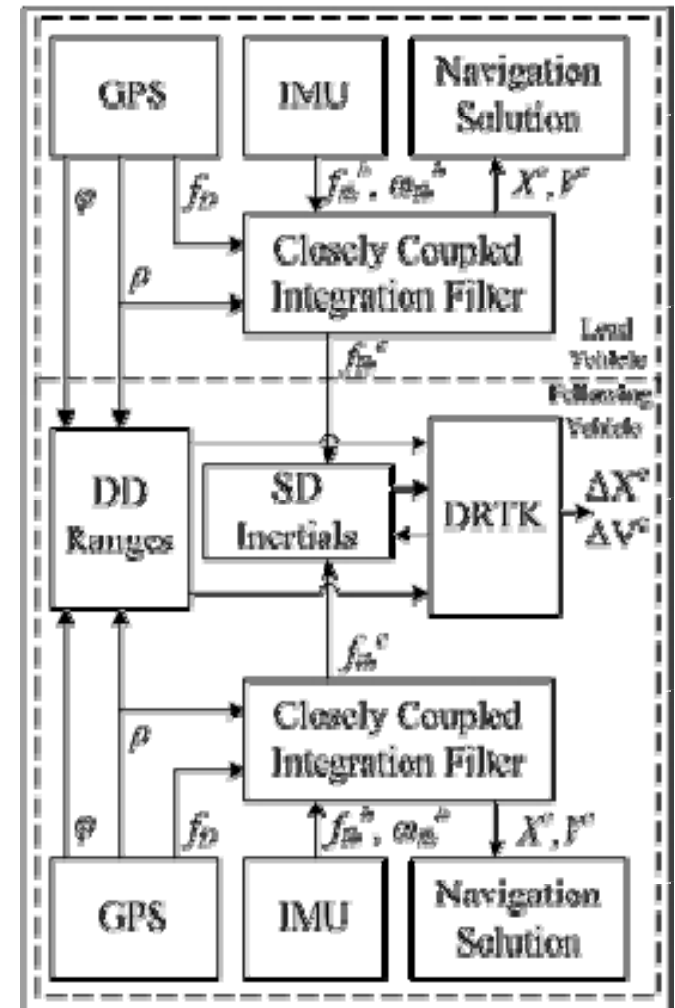
Dual – 0.2 seconds





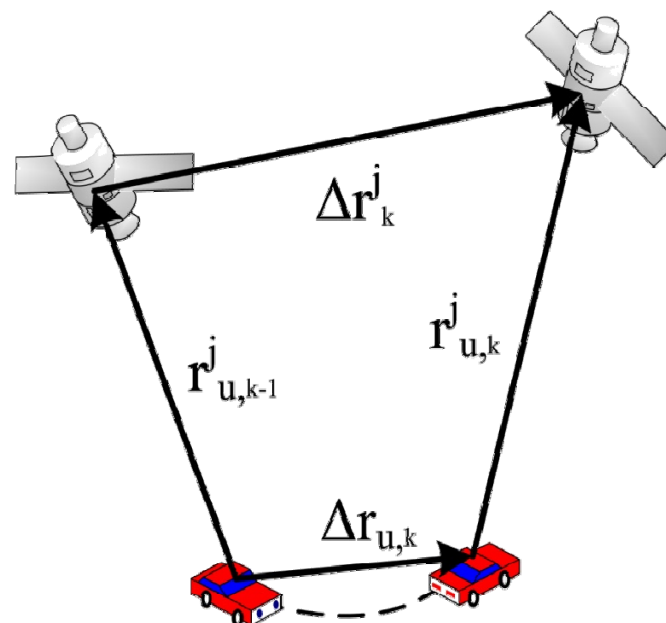
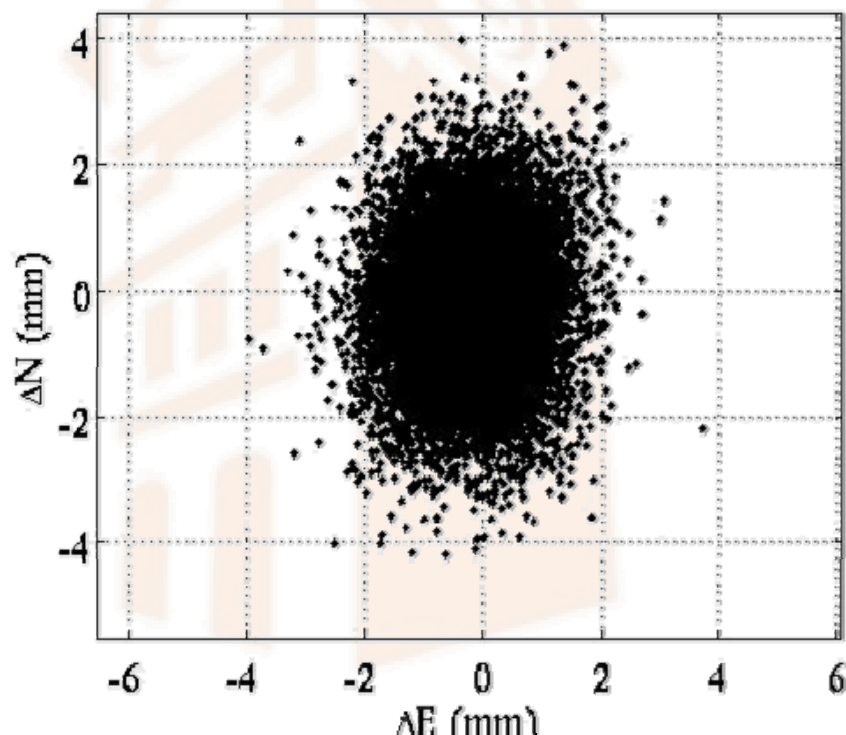
## DRTK/INS Integration

- Pseudo-range and Doppler data is fused with inertial data at each vehicle
- Relative inertial and state information is produced by differencing the corrected inertial measurements and states from each vehicle after a rotation into the navigation (ECEF) frame
- Double difference range and carrier phase measurements combine with the relative inertial measurements and/or state information, on the following vehicle, to produce a relative position to a lead vehicle



# TDCP – Change in Position

- Accurate change in position can be estimated using *time differenced carrier phase* (TDCP) measurements
- Differencing two measurements across time “removes” atmospheric and SV clock errors, and the integer ambiguity, assuming the time difference is small



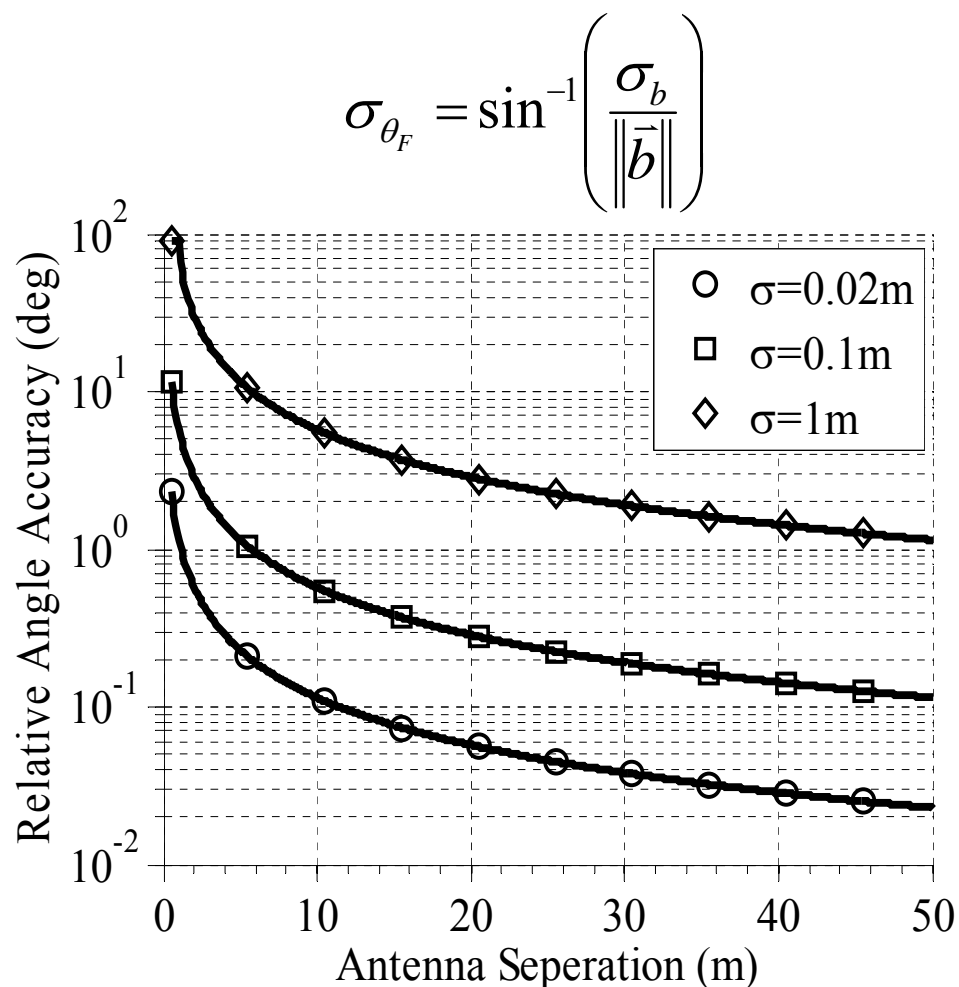
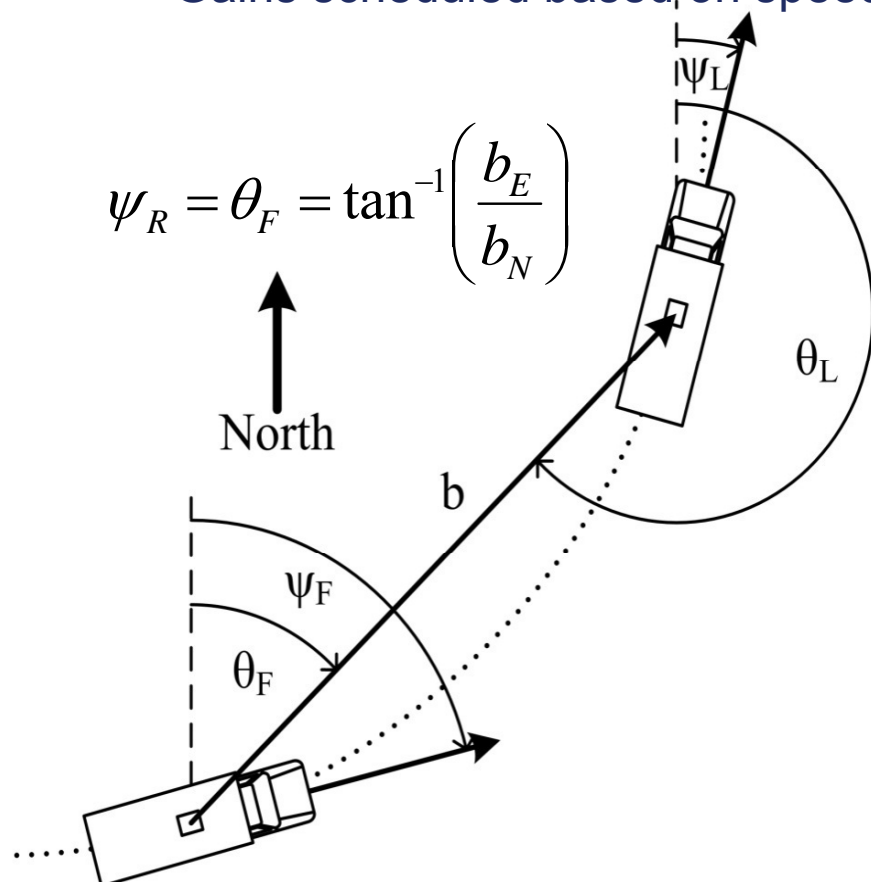
$$\Delta \phi_{Ak,k-\tau}^j = \lambda^{-1} \Delta \left| \vec{r}_A^j \right|_{k,k-\tau} + f \Delta \delta_{Ak-\tau} + Q_{Ak,k-\tau}^j$$

**$\Delta$ North Error STD = 0.75 mm**

**$\Delta$  East Error STD = 1.09 mm**

# Path Duplication – Short Distance Following

- The short distance following approach was to control the following vehicle as if it were a trailer
  - The following vehicle's navigation system provided its heading estimate and yaw rate
  - The heading reference was set equal to the global relative angle between the vehicles determined from the DRTK solution
  - Gains scheduled based on speed





# Path Duplication – Experimental Results



- n = index of closest point of past leader position  
j = # of measurements between follower and leader at index n

reduced

$n = i$   
 $j = \#$   
 $a$

North

$R$

$\psi_L$

$\theta_F$

$\theta_L$

$\gamma$

$b$

$\psi_F$

$\theta_F$

$\gamma$

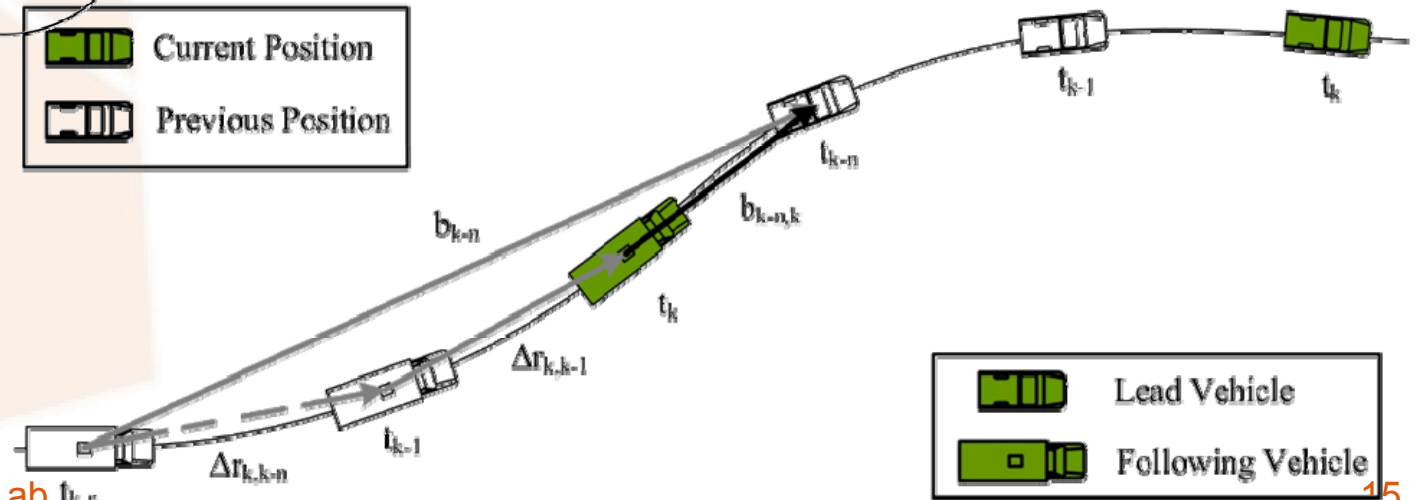
$\psi_R = \theta_F + \gamma = 2\theta_F - \psi_L$

Current Position

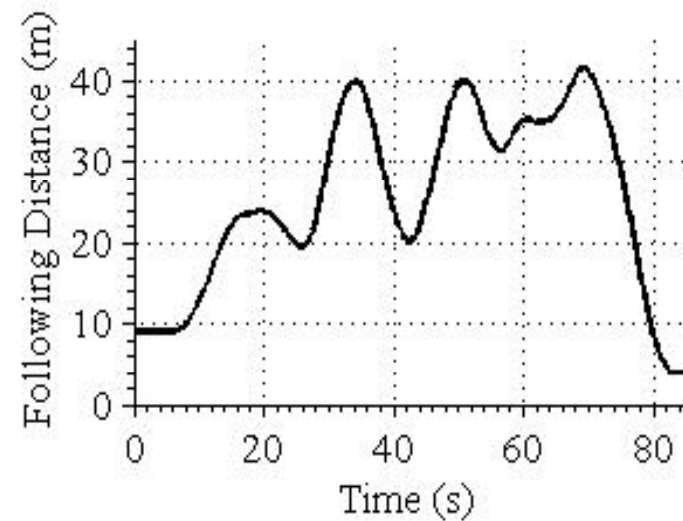
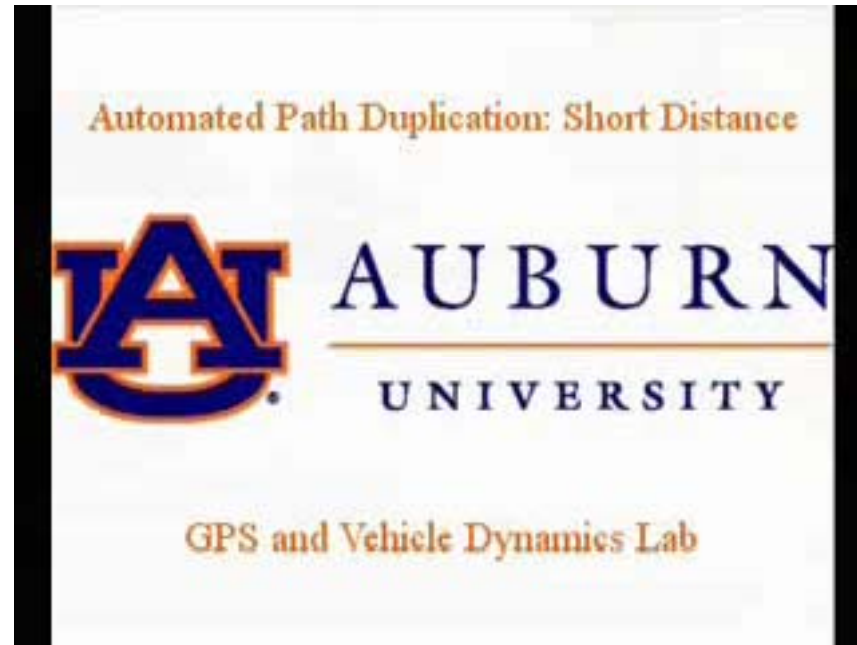
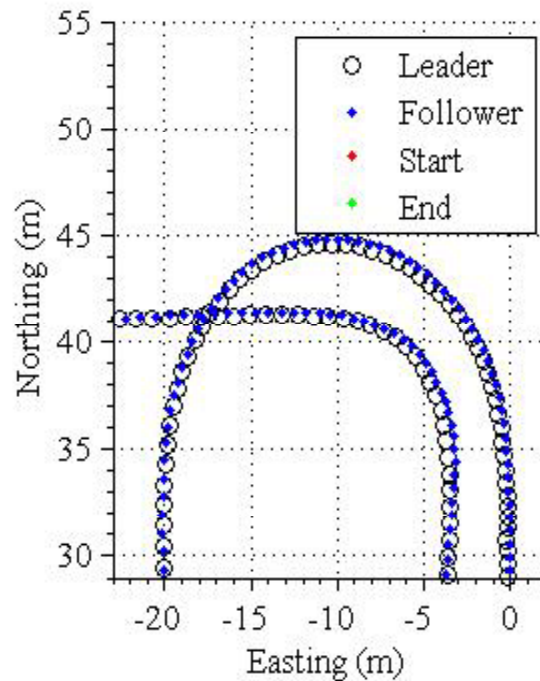
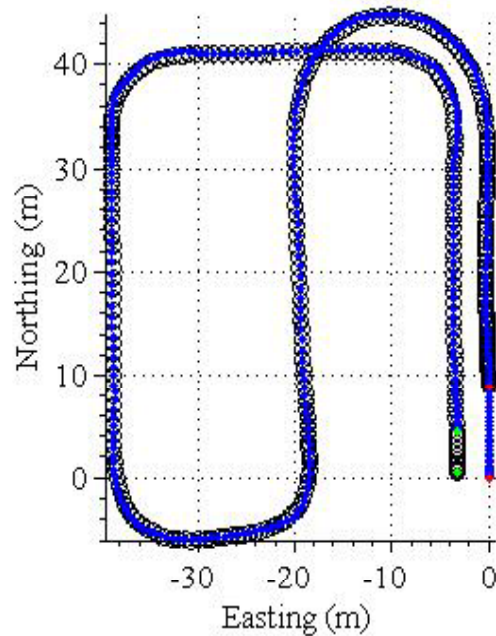
Previous Position

$\Delta r_{k,k-n}$

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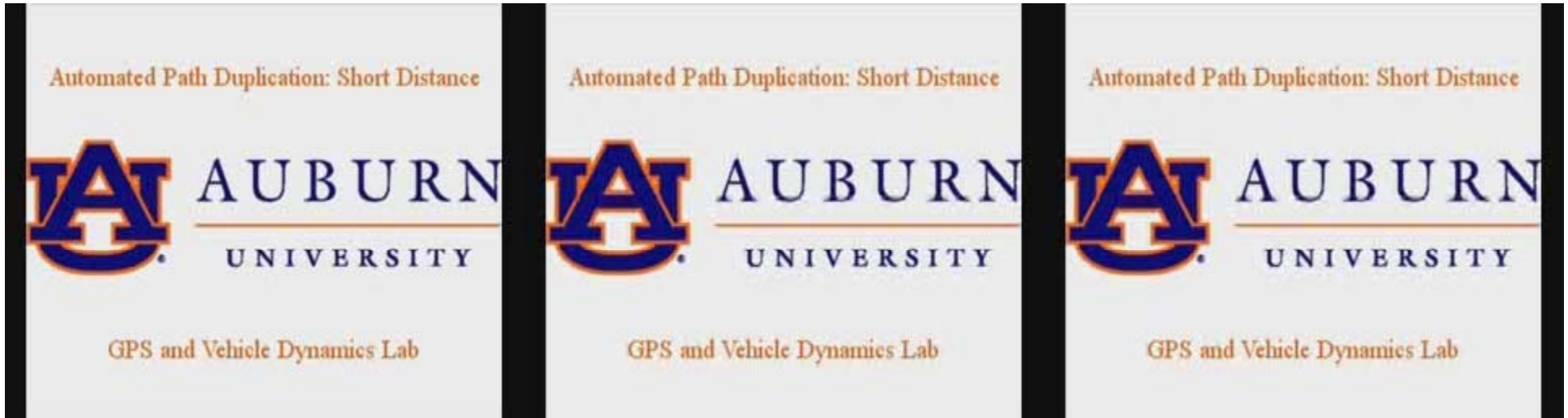


# Path Duplication – Long Distance

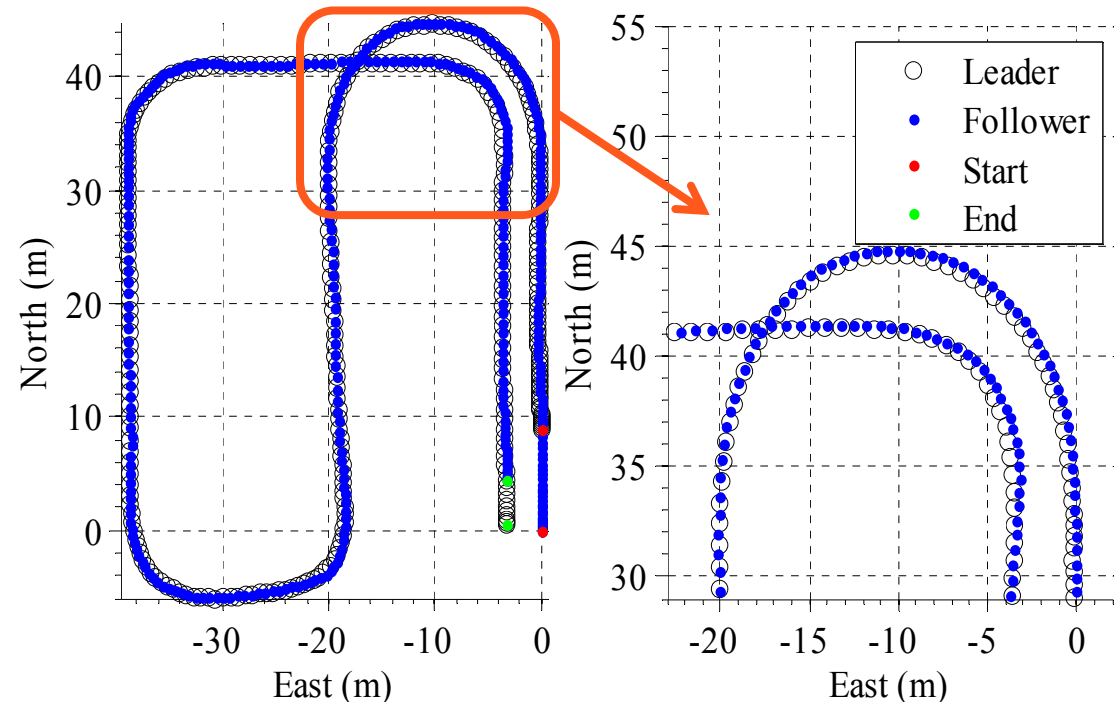




# Long Distance Following



- NLOS method implemented in real time on UGV
  - Tested with dynamic paths through parking lot and on NCAT track
  - Following distances varied from 10 to 120 m



# Path Duplication – Delayed Following

Automated Path Duplication: 5 Minute Delay

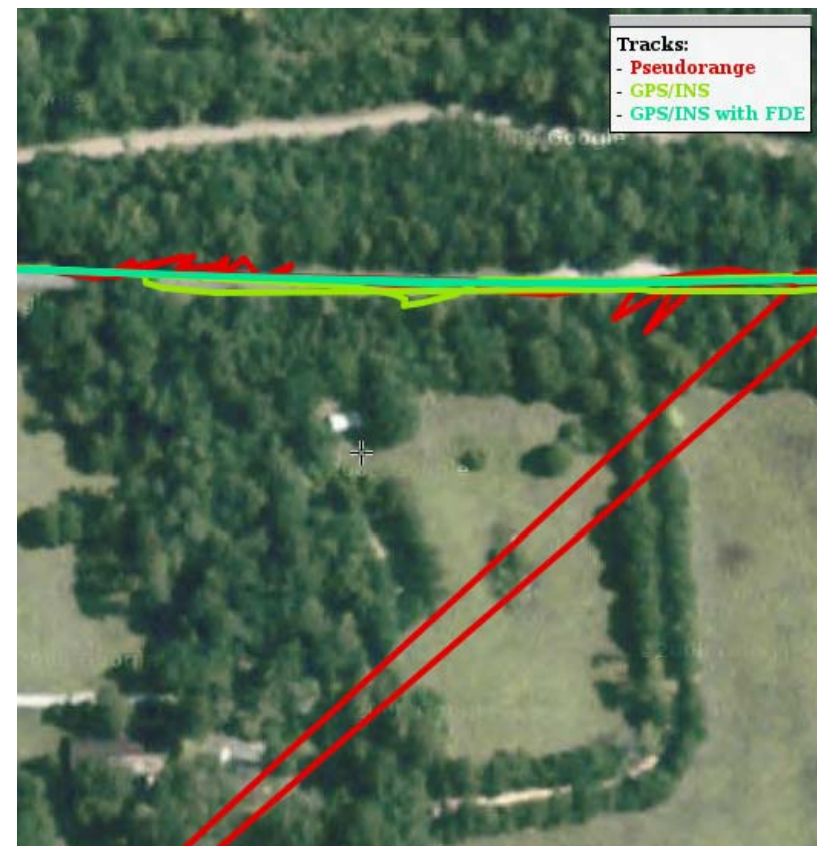
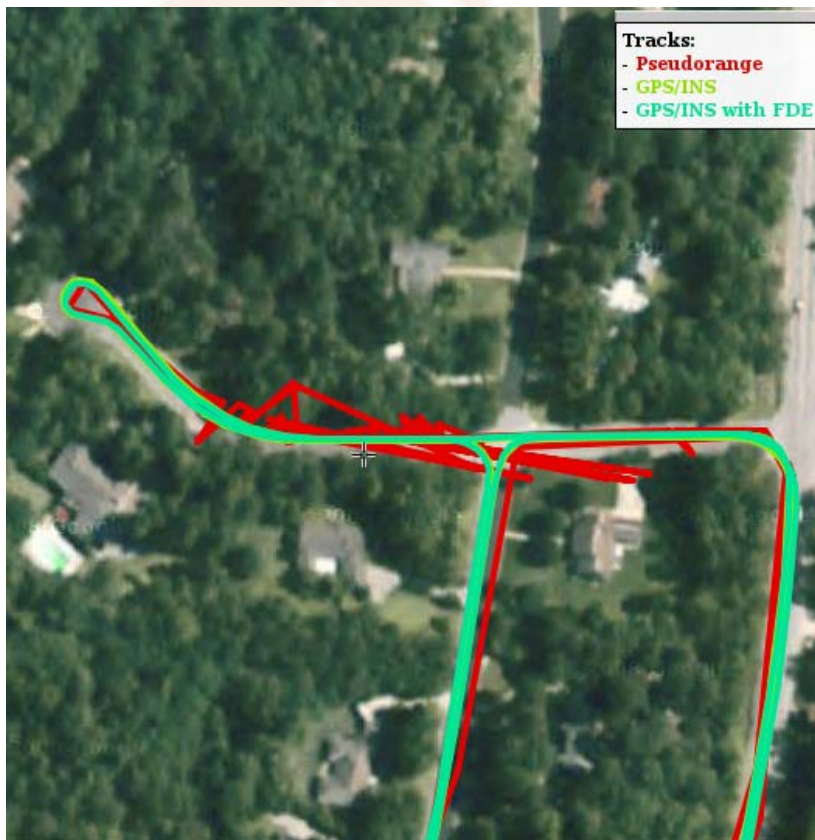


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# GPS/INS with FDE

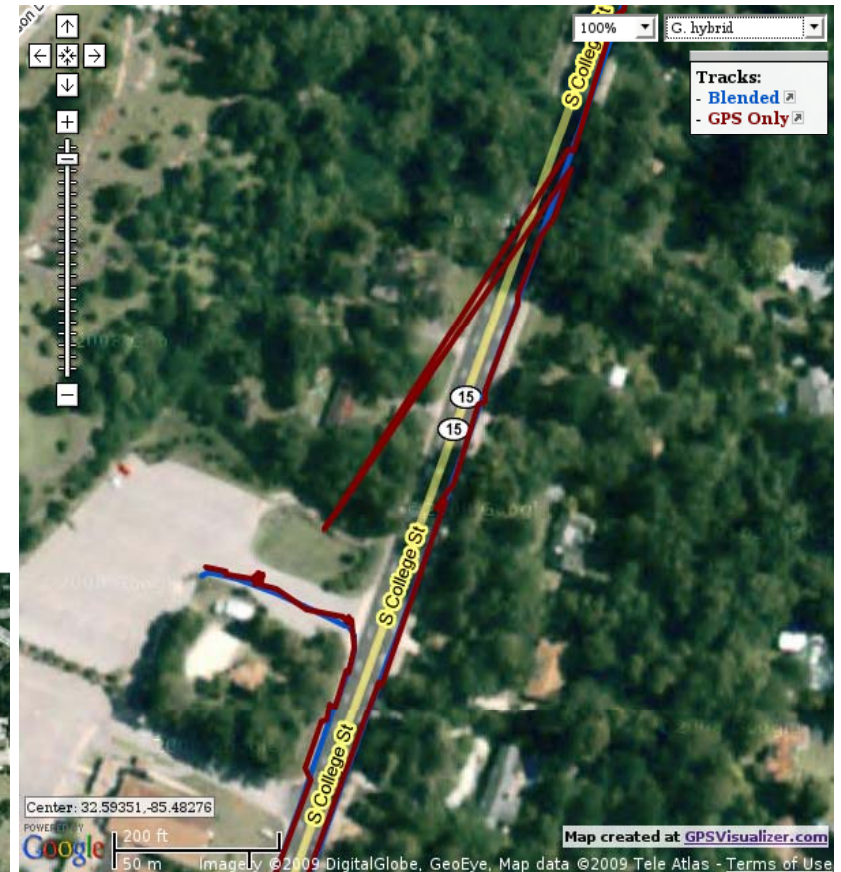
- Pseudorange-only positions suffer large jumps in foliage (red)
- Inertial Navigation System (INS) aids position solution (yellow)
- Fault Detection and Exclusion (FDE) further improves performance in degraded environments by detecting signal errors (green)





# GPS/INS with FDE

- Integration and Fault Detection performed in real-time
- Removes faults in individual GPS signals (blue)
- Uses remaining signals to navigate



- NovAtel GPS
- Crossbow IMU



Motivation – create an accurate simulation of satellite and receiver positions

## Simulation Capabilities:

Collect Ephemeris Data

Plot satellite positions with time

Plot receiver position with time

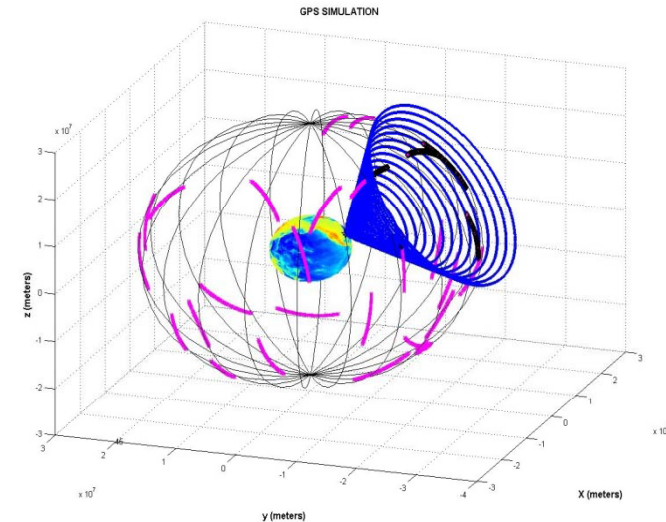
- Given receiver speed and heading

Detect Satellite visibility

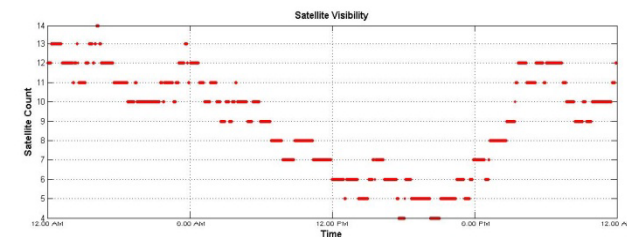
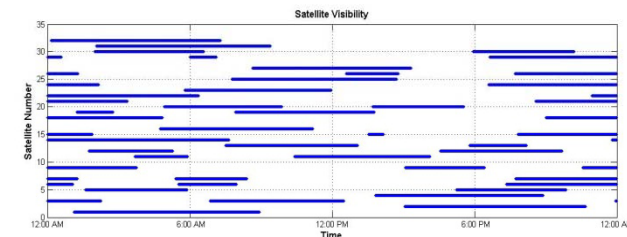
- Given receiver envelope mask angle

Receiver position estimation

- Using known pseudo-ranges of satellite and receiver positions



Satellite Positions



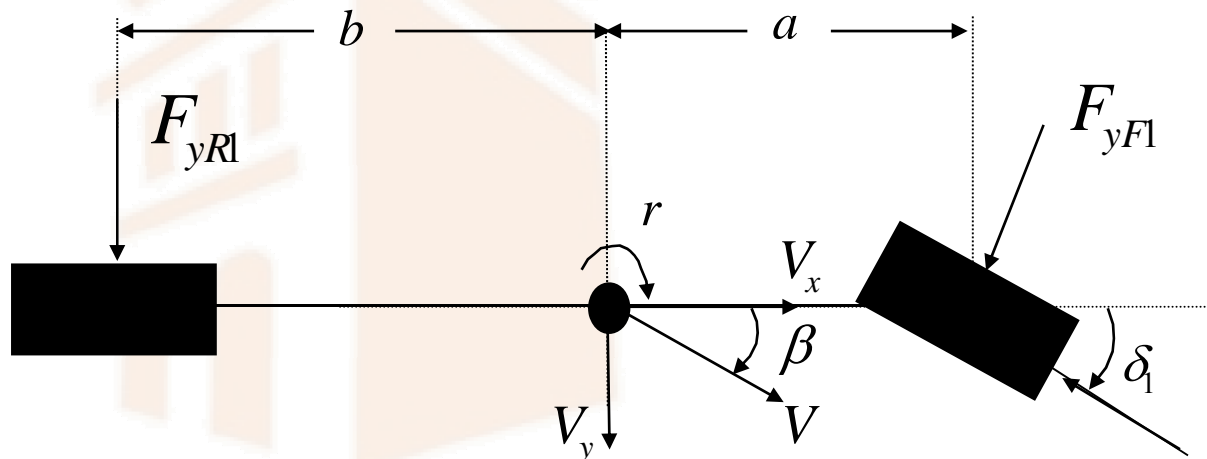
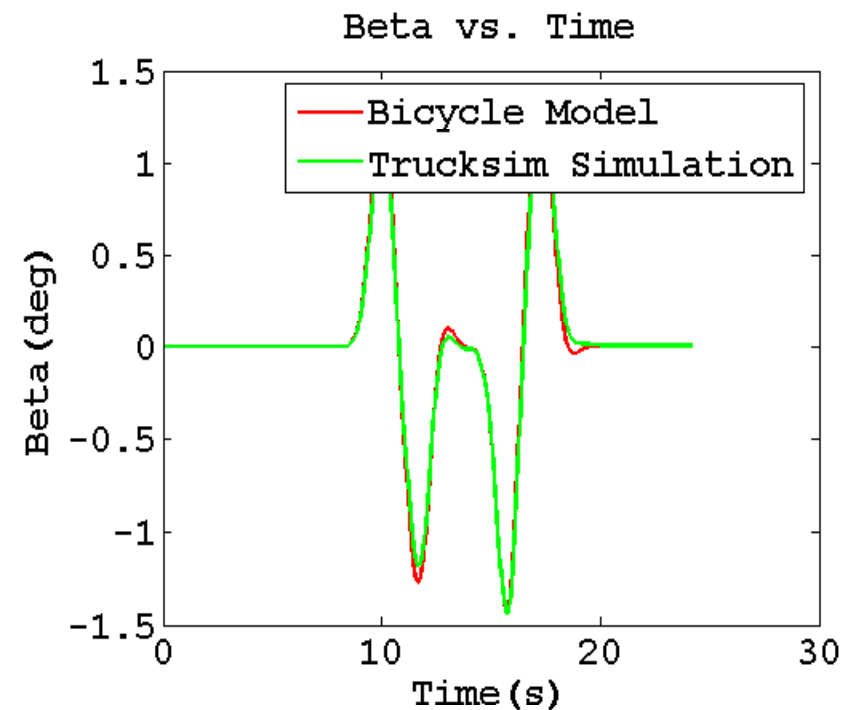
Satellite Visibility

- Dynamic vehicle models have been developed
  - Wheel Slip
  - Steer Angle
  - Tire Parameters
  - Roll, Pitch, Yaw
- Vehicle Models validated against Carsim
- Initial terrain modeling methods developed
- Preliminary model converted to C++ for integration into GDRS simulation environment
- Computer has been set up for simulation environment at Auburn

## Model

- Simple Single-track
- Bicycle Model
- 2 DOF (Yaw,  $y$ )
- Assumptions
  - No weight transfer
  - Equal inner/outer slip angles ( $\alpha$ ) & steer angles ( $\delta$ )
  - Same tires inner/outer

## Validation



# Vehicle Modeling – Next Steps

- Test vehicle models in simulation environment
- Implement terrain modeling in simulation environment
- Acquire parameters from vehicle experimentally
- Compare simulation results to actual vehicle test data



- Looking to use relative position to landmarks (object registration) to perform non-GPS based leader follower capability
  - Vision and LIDAR systems can provide range and bearing measurements to landmarks measured using vision or LIDAR to augment a GPS/INS navigation system.
  - Landmarks positions are measured relative to current vehicle position
  - Landmarks are then used to determine position when GPS is absent or degraded
- Typical SLAM approach – 1 vehicle sees the same landmark many times
- Modify approach to allow multiple vehicles to see the landmark 1 time
  - Only maps are shared between the vehicles (not sensor data)

- Goals
  - Develop algorithms for the leader vehicle to “see” natural or man-made landmarks (i.e. signs, trees, etc).
  - Perform without a visual line of sight to the leader
  - Extracted features contain color information and contours

- Feature Extraction

- Use the Shi and Tomasi corner detection algorithm

$$G = \sum_{x=p_x-w_x}^{p_x+w_x} \sum_{y=p_y-w_y}^{p_y+w_y} \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$

- Large eigenvalues indicate a corner
    - Small eigenvalues indicate a smooth surface
    - One large and one small eigenvalue indicates an edge
- Machine Learning
  - K -means Clustering
    - Iteratively assigns each corner to a cluster
    - Assumption: that all of the corners of an object will be grouped in the same cluster
- Extract a 50 x 50 pixel region around

- Goals

- Use a database created by the leader vehicle to aid in navigation
- Locate the objects or landmarks that the leader extracts



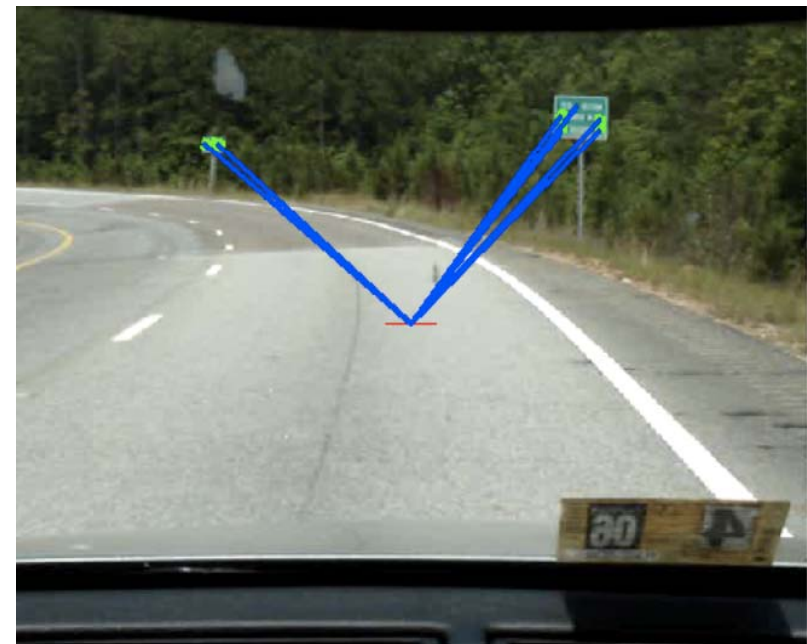
- Approach

A sign extracted by the leader

- Characterize the landmark according to color statistics and edges
- Perform a search for any locations that match the data of the landmark extracted from the leader

# Vision Navigation – Results

Algorithm on lead vehicle extracts two signs

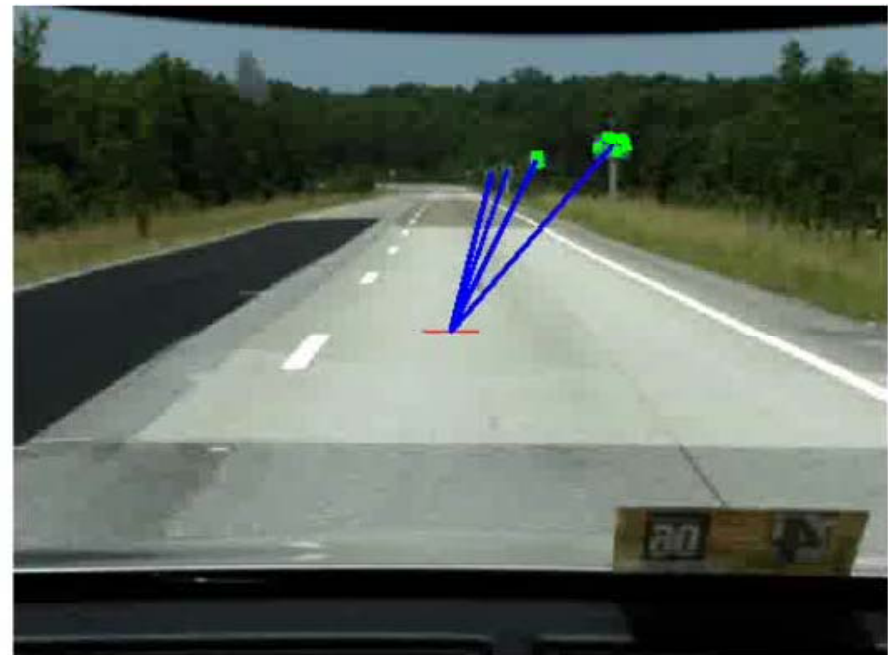


Following vehicle detects signs



# Vision Navigation – Video

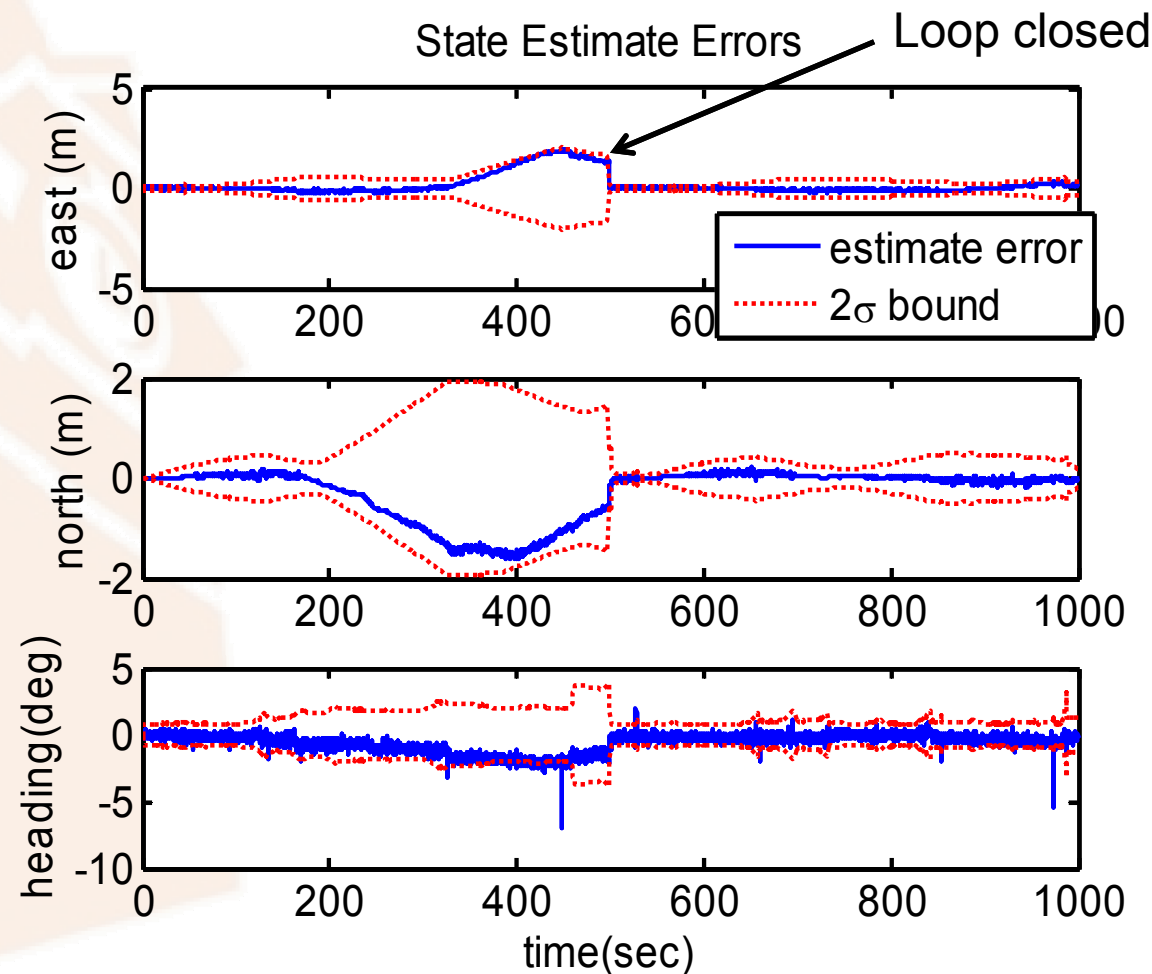
Lead vehicle extracts features



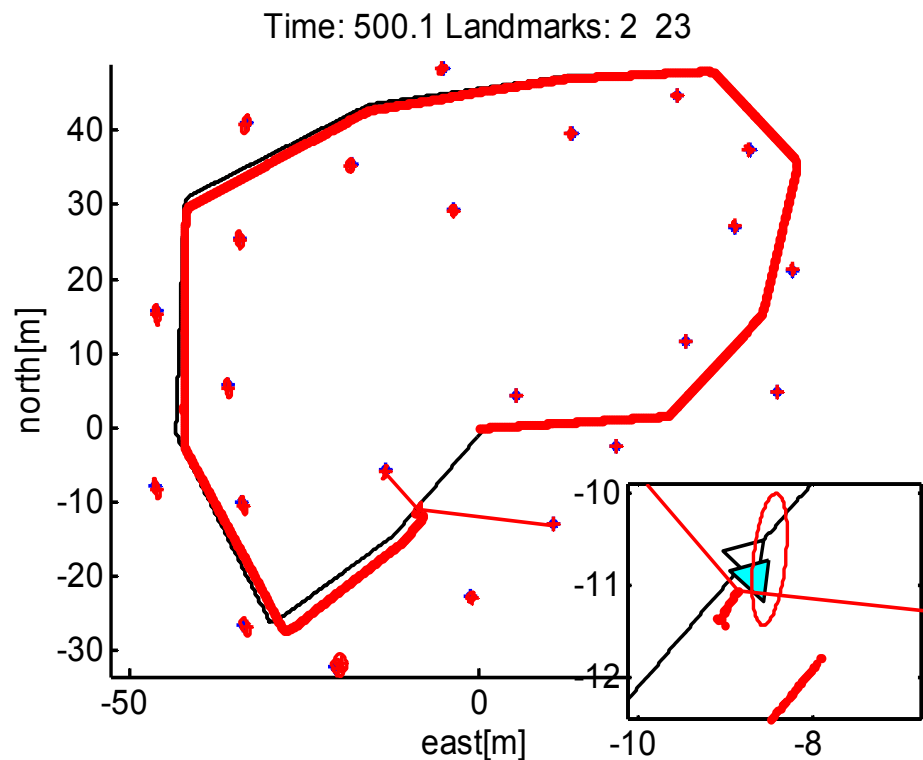
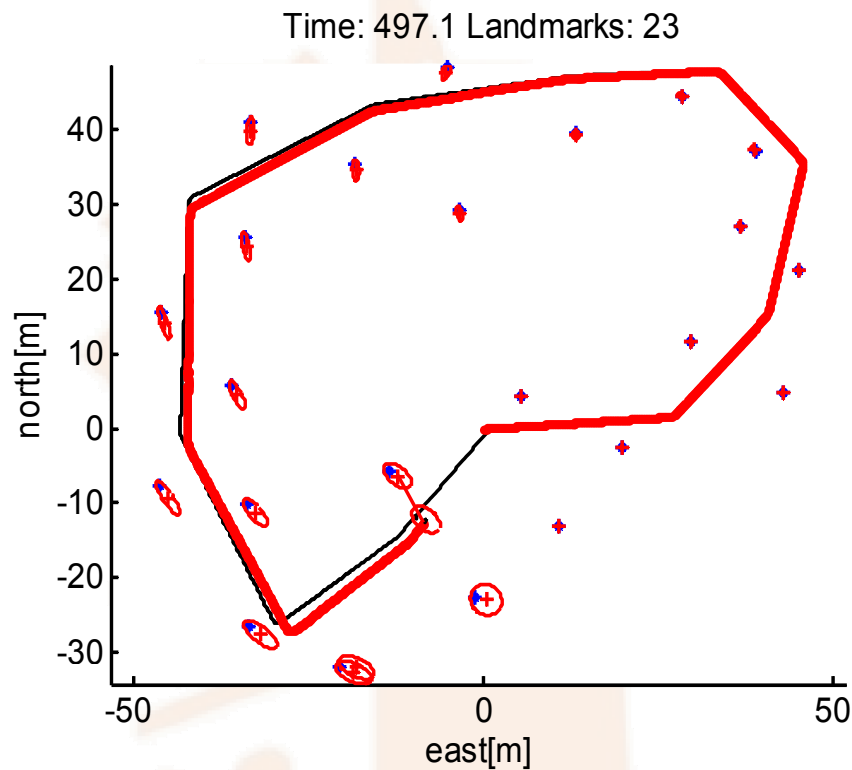
Following vehicle detects signs

# Landmark Navigation Benefits

- Slows dead-reckoning error growth
- Bounds error when traveling a cyclical path



- Simulated cyclical path using odometry and landmark measurements



# What's Next

- Integration of DRTK with Perception Sensors
  - Provide Robustness when GPS not available
  - Provide DRTK with limited GPS satellites
- Low-cost DRTK/FDE Implementation
  - Implement using on-board sensors (i.e. DAGR)
- FCS LSI Needs/Requests for Research
- Vector Tracking
  - Novel GPS tracking algorithms developed at Auburn
    - Provides instantaneous GPS reacquisition
    - Improves noise resistance (jamming, multi-path, etc.)
    - Improves tracking in heavy foliage
  - Extend to provide DRTK in harsh GPS environments
- Collaboration in Future ATOs?

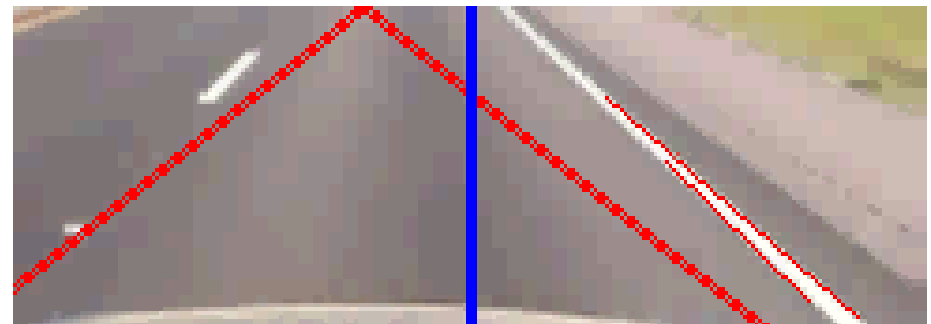
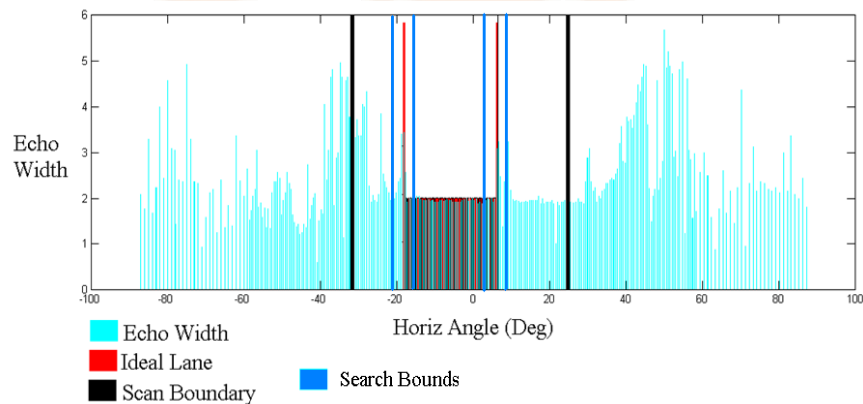
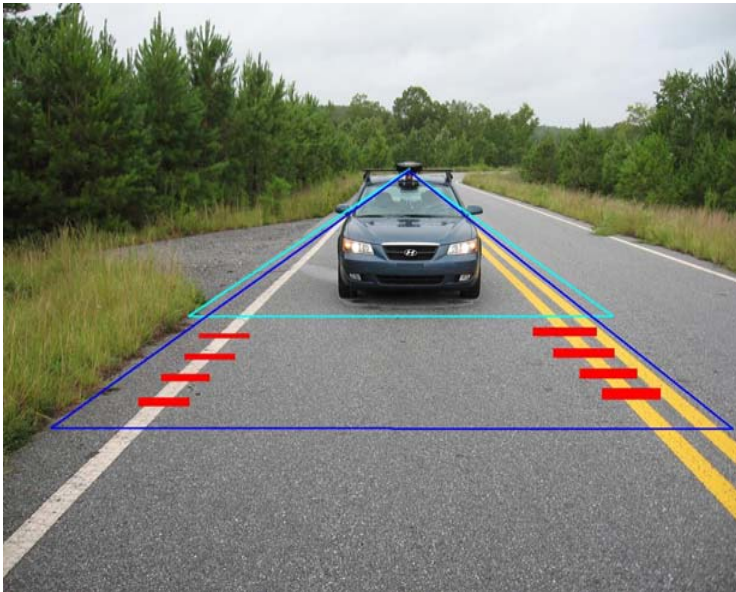


# Integration of DRTK with Perception Sensors

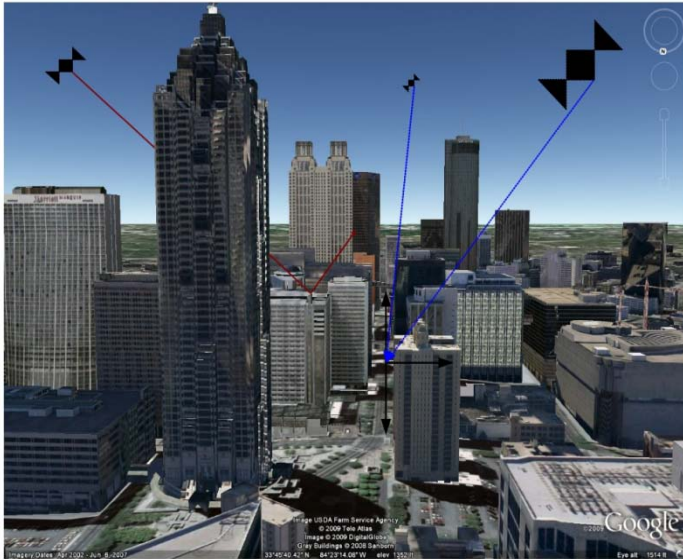
- Provide relative navigation for leader-follower systems with limited, poor, or reduced GPS coverage
- Use relative position to landmarks measured using vision or LIDAR to augment or constrain the GPS/INS DRTK navigation system
  - Lane marking or road edges
  - Object registration
- Exploring 2 approaches
  - Feature based SLAM
  - Scan-matching SLAM



# LiDAR and Vision based Lane Detection



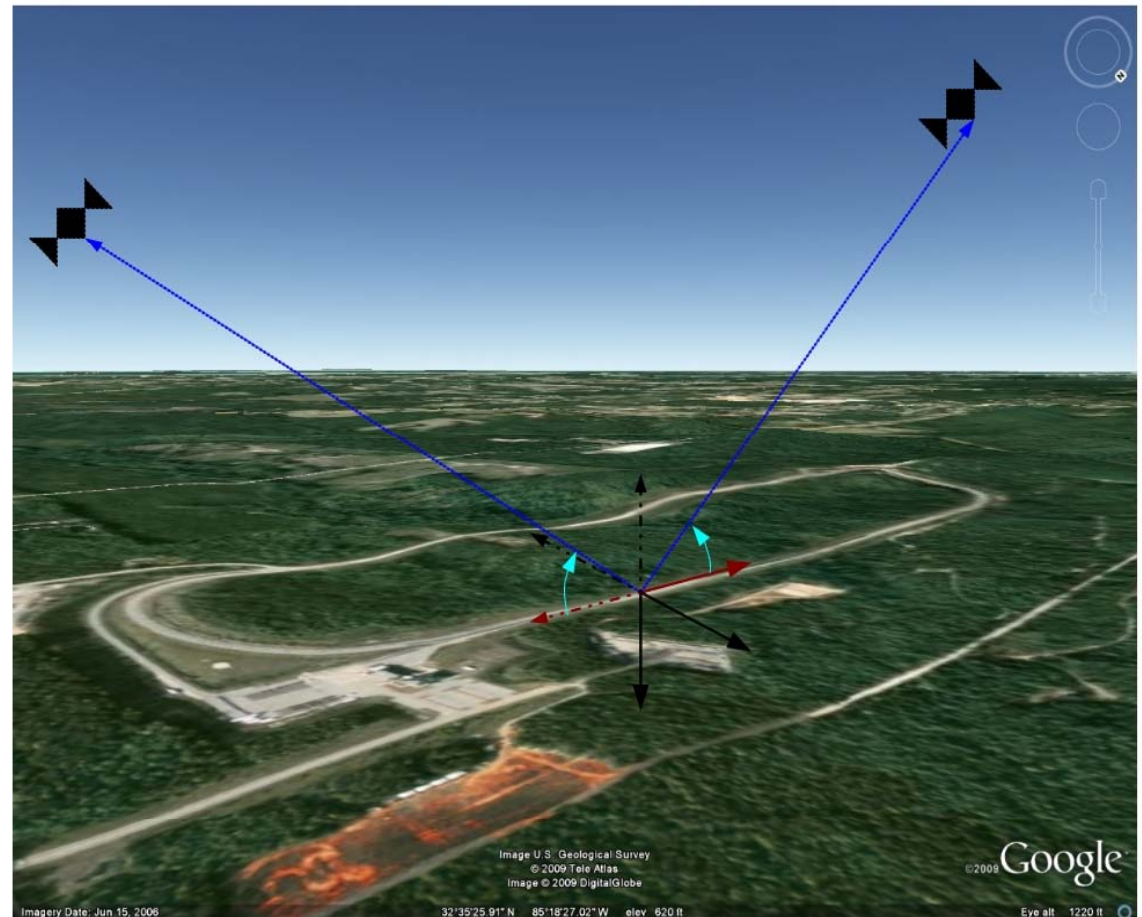
# Positioning w/ Limited GPS Satellites



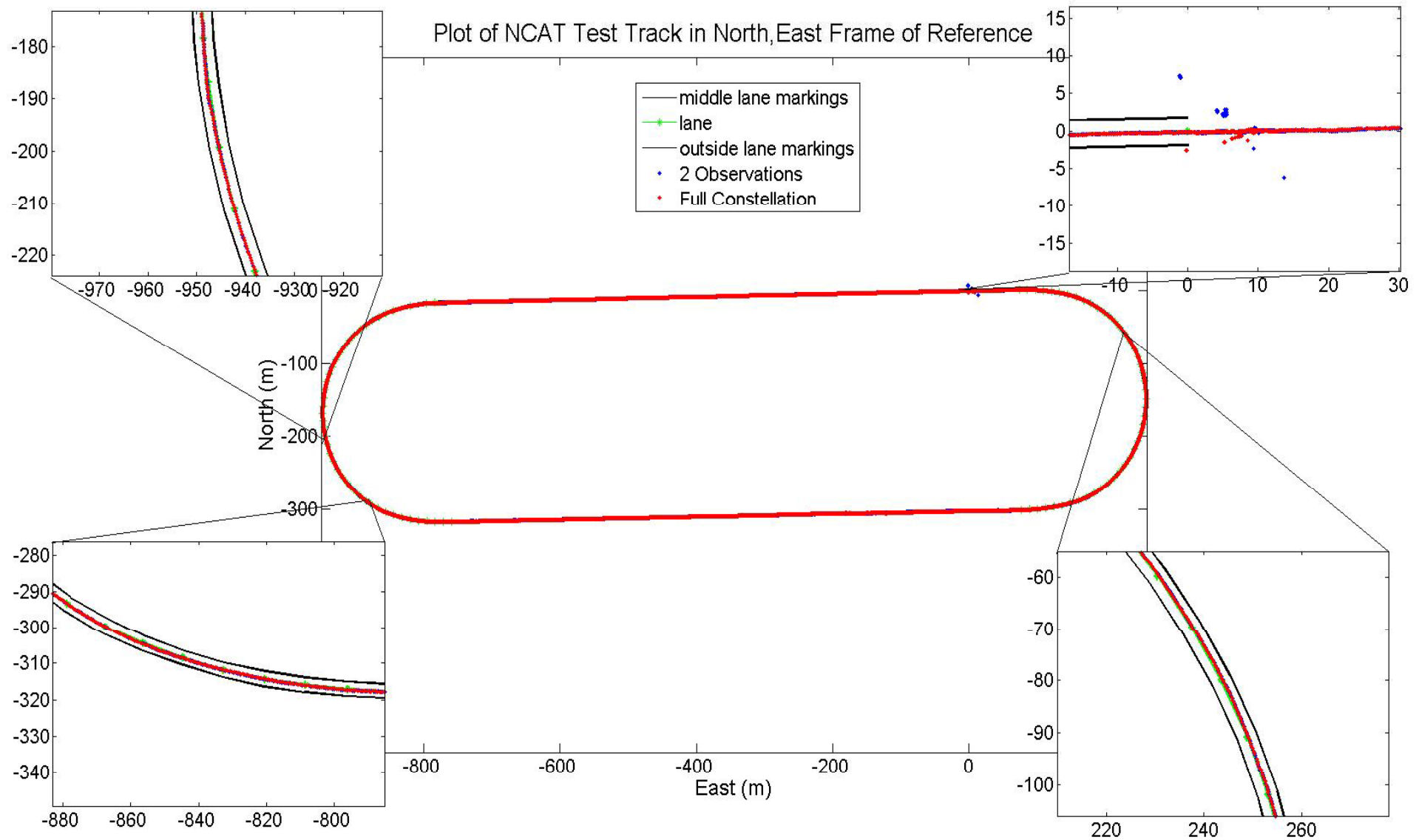
Urban Environment where only a few GPS Satellites may be available

Validated at Auburn's NCAT Test Track using:

- Lateral Constraint
- Vertical Constraint
- 2 GPS Satellites



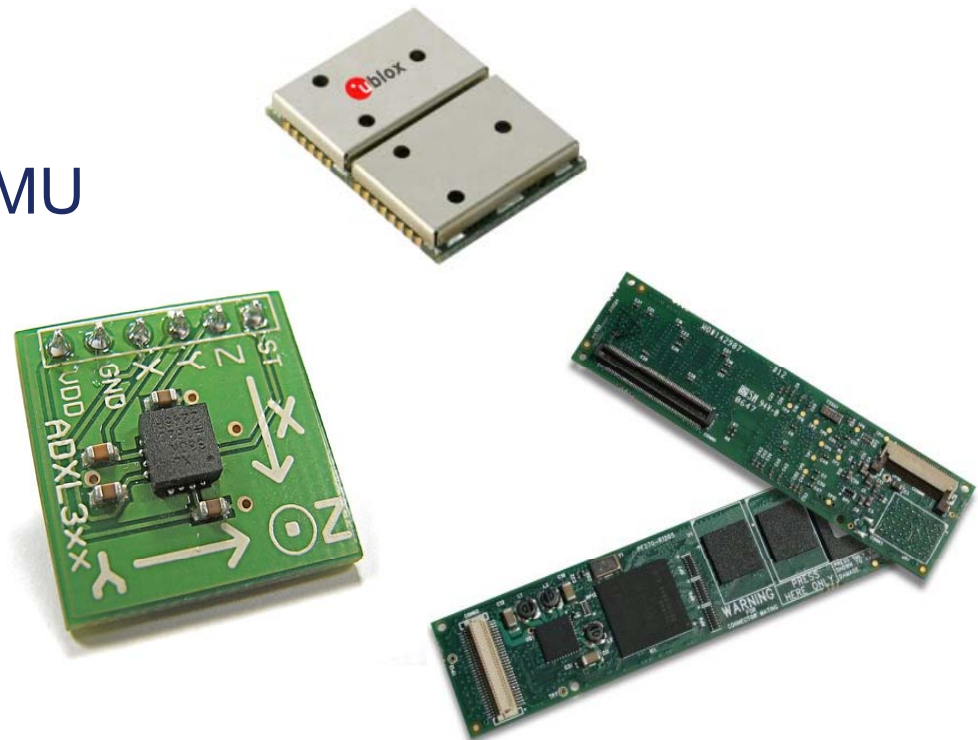
# Positioning Results





# Low-cost FDE/DRTK Integration

- Develop onto a low-cost GPS/INS module or using DAGR
  - Use on-board GPS (DAGR) and IMU or vehicle sensors (wheel speed, steer angle, etc).
- Alternatively use low-cost OEM receiver
  - Gumstix computer
  - uBlox GPS receiver
  - Analog Devices MEMS IMU
  - Prototype Cost ~ \$600





# Needs/Requests from FCS LSI

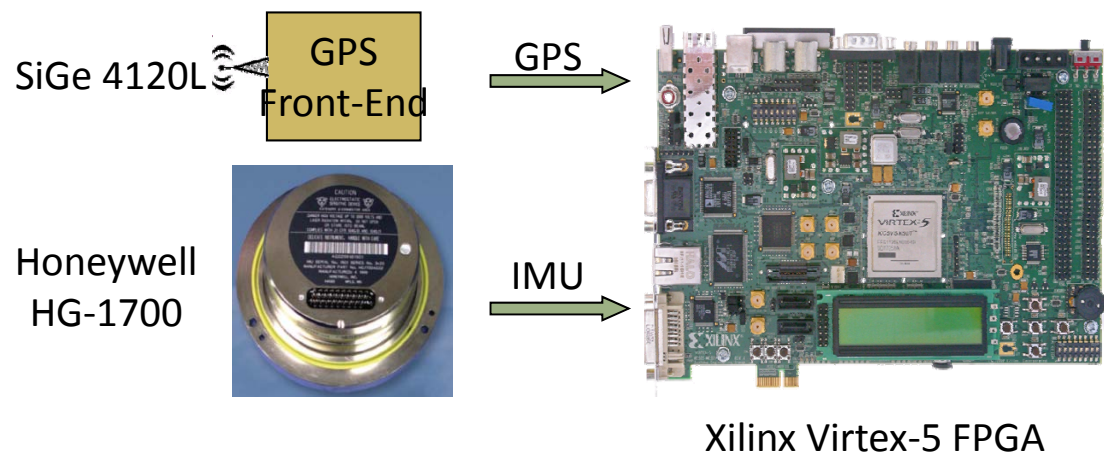
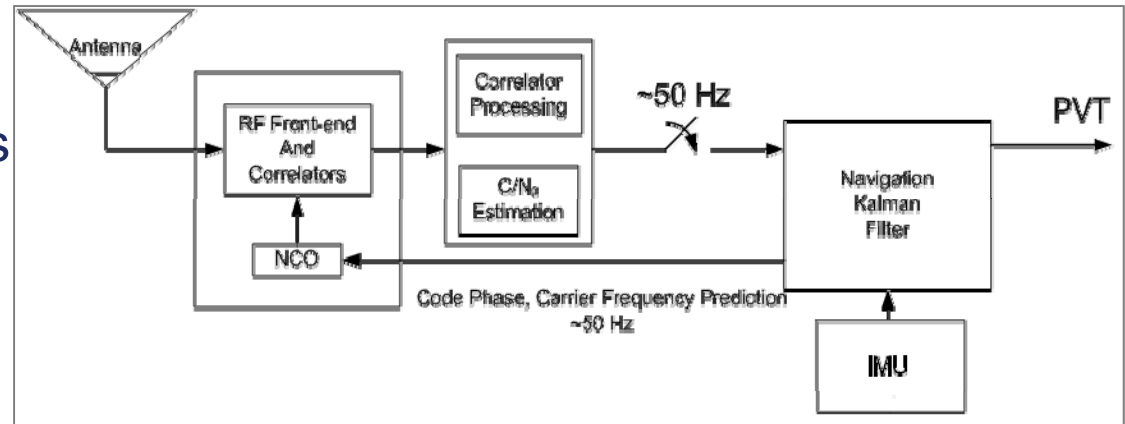
- DRTK on GB-GRAM
  - Use on-board GPS (DAGR) and IMU (wheel speed, steer angle, etc).
- DRTK with CRPA Antenna
  - Effects on accuracy and robustness
  - Effects on integer ambiguity solution
- Tele-op/indirect driving issues (especially at high speeds)
  - Effect of displays (resolution, 2D vs 3D information, field of view)
  - Effect of latency
  - Additional information to aid operator (visual, haptics, contour topography, birds eye view, etc.)
  - Local low-level control (allow operator to provide higher level commands)



# Auburn University's Vector Tracking and Deeply Integrated GPS/INS

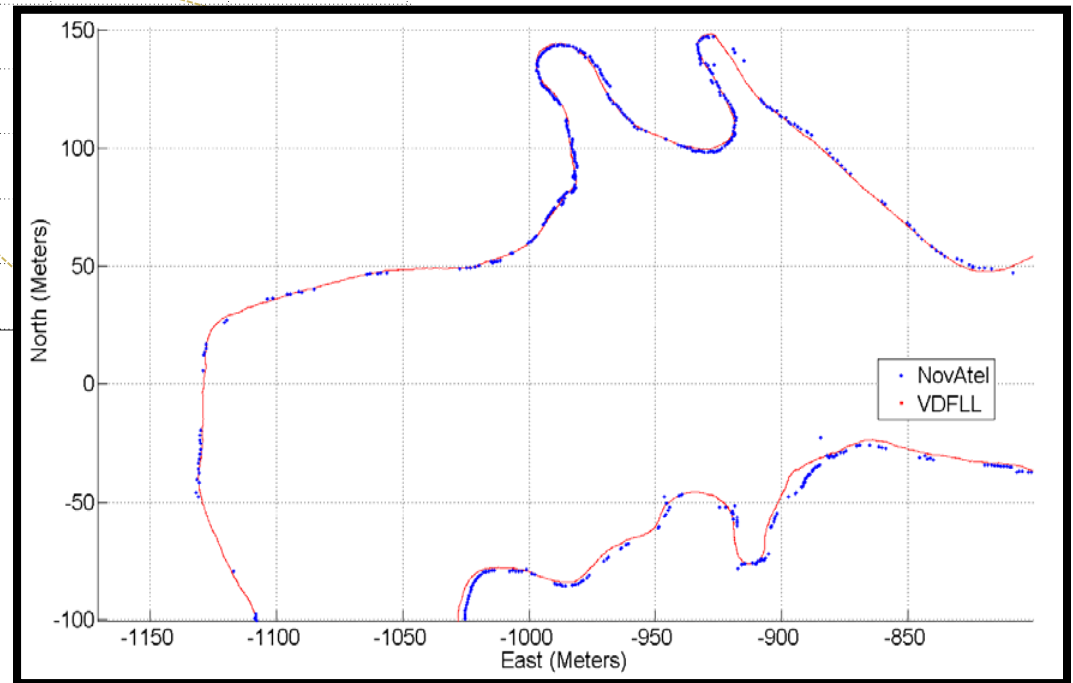
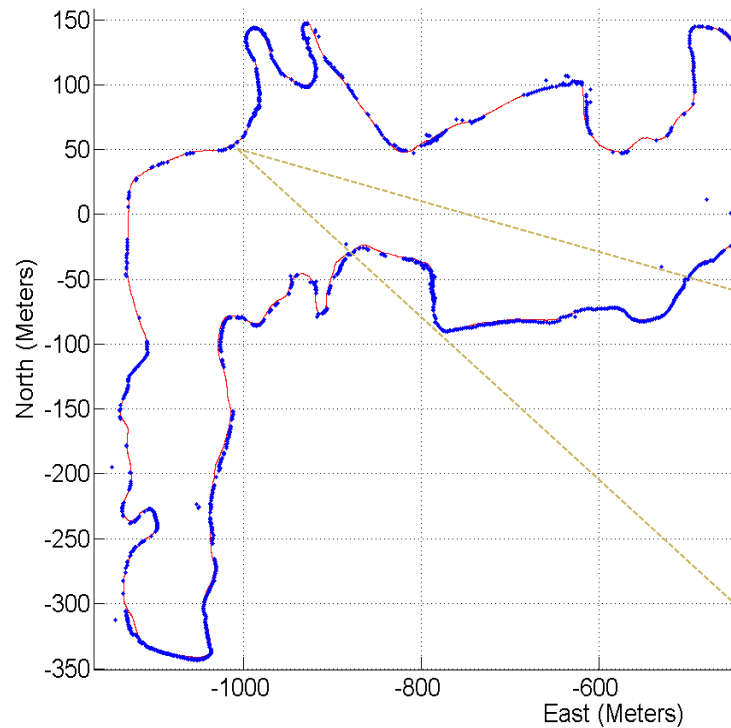
# Vector Tracking

- No tracking loops are used, signal tracking and navigation state estimation are combined into one algorithm
- Provides near instantaneous signal reacquisition after short GPS blockage
- Provides improved tracking in noisy environments
- Implementing on a Xilinx Virtex-5 FPGA
  - Real-time capable
- Ability to interface with multiple sensors
  - INS, LIDAR, vision
- Need to modify algorithms to provide carrier outputs for DRTK



# Baja Course: NovAtel and VDFLL Comparison

Comparison of Coverage:  
Standard GPS Receiver ~ 70%  
VDFLL 100%



Heavy Foliage Test Course



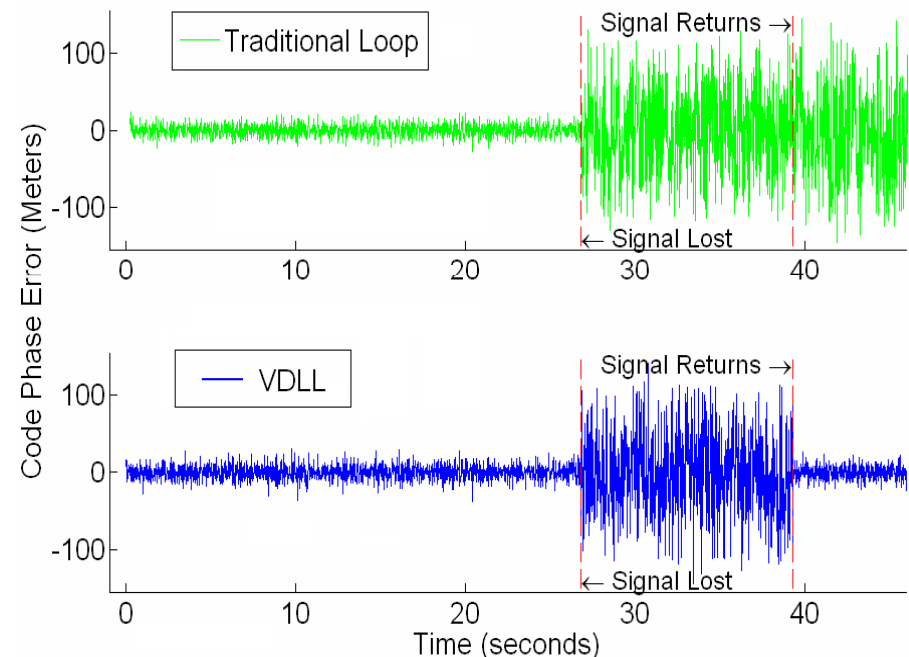
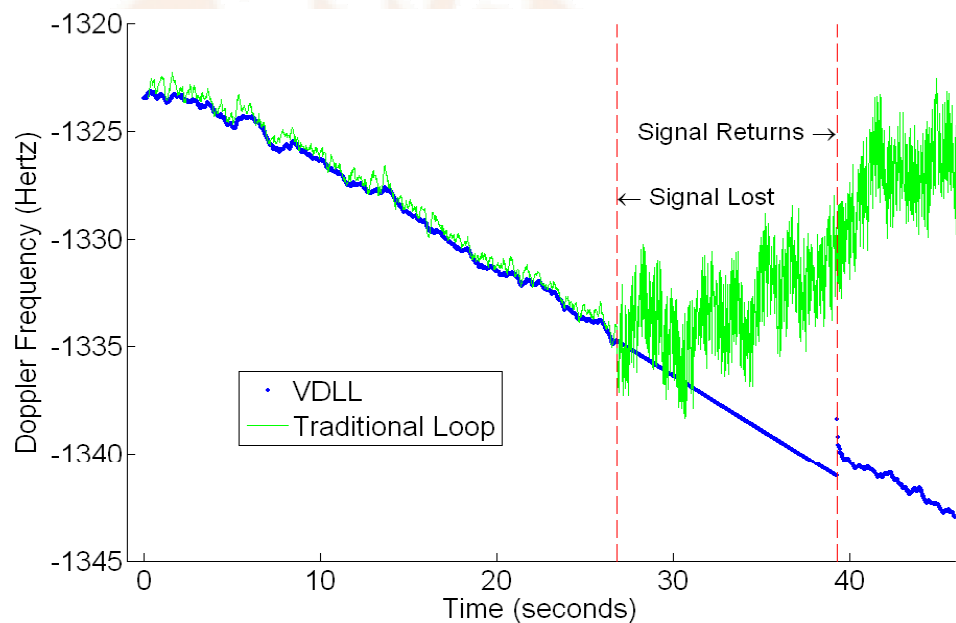
# Downtown Atlanta w/ Vector Tracking





# Vector Tracking Signal Tracking

- Vector tracking benefits include
  - Correlation among channels allows for tracking signals with lower C/N0s
  - Instant signal reacquisition after outage
  - Solution inherently aids tracking



The VDFLL tracks the correct Doppler when the signal is lost (left) and instantly reacquires the code phase when the signal returns.



# FHWA – Lane Level Navigation

# Lane Detection and Lateral Distance Estimation

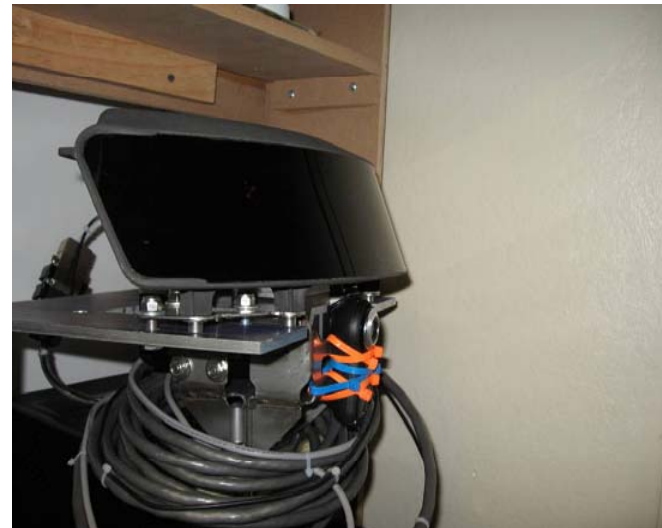
## Lateral Distance Estimation

- Sensor fusion with camera and LiDAR for robustness of lateral distance measurement
- Used for lane level localization in multipath environments



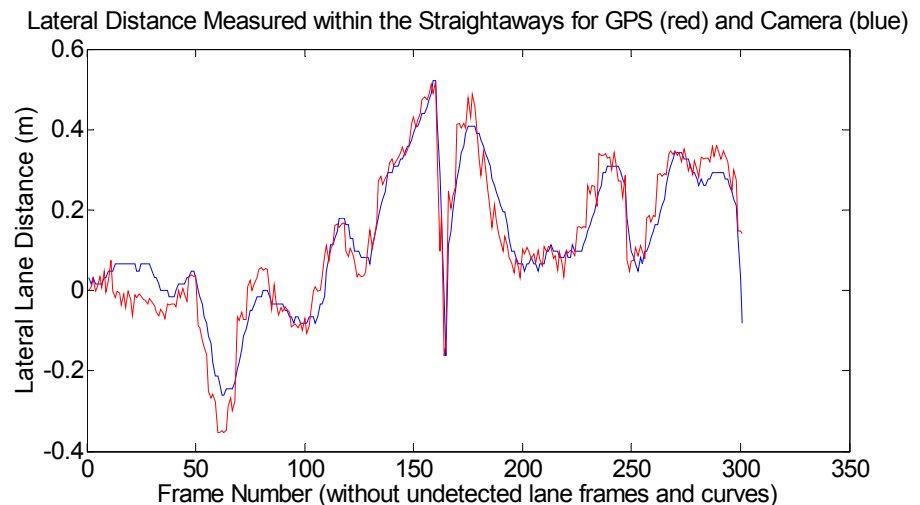
## Lane Detection Sensors

- Logitech QuickCam Pro 9000
- IBEO ALASCA XT laser scanner
- both sensors have a update rate of 10Hz



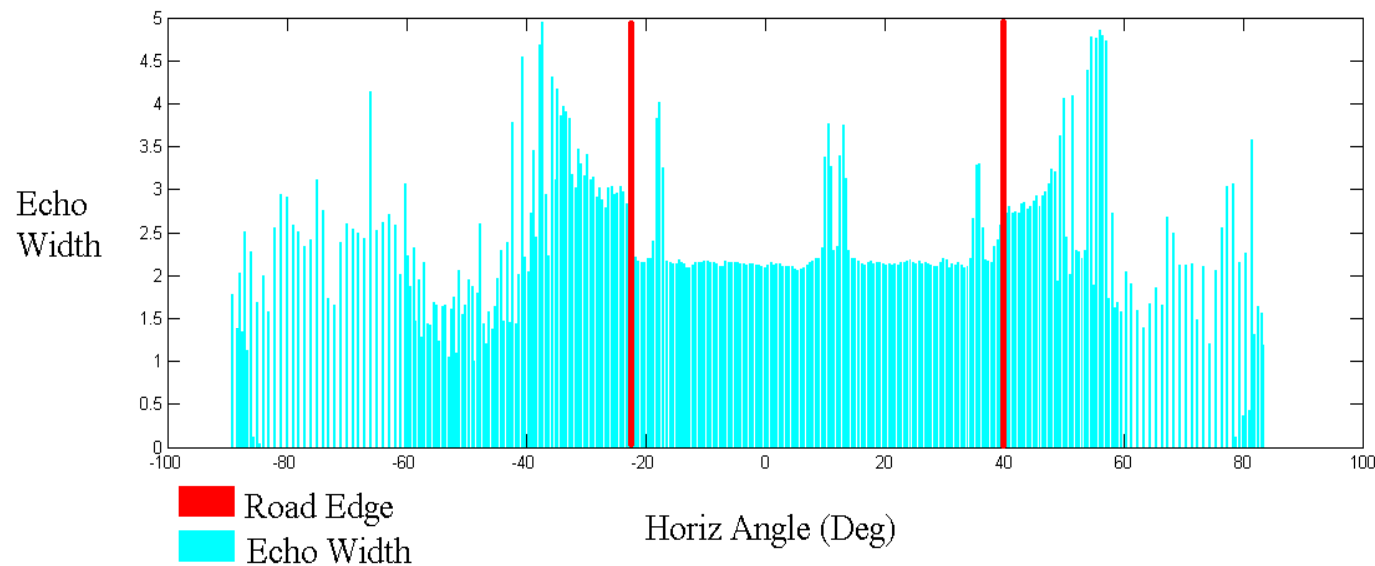
# Lane Detection with Camera

- Thresholding / Edge Detection
- Hough Transform
- Least Squares Interpolation
  - Interpolate 2<sup>nd</sup> order polynomial as model for lane
- Kalman filter
  - states are the coefficients of the polynomial
- Polynomial Bounds
  - Lines for subsequent frames lie within polynomial boundary curves
- <10 cm accuracy on straight roads



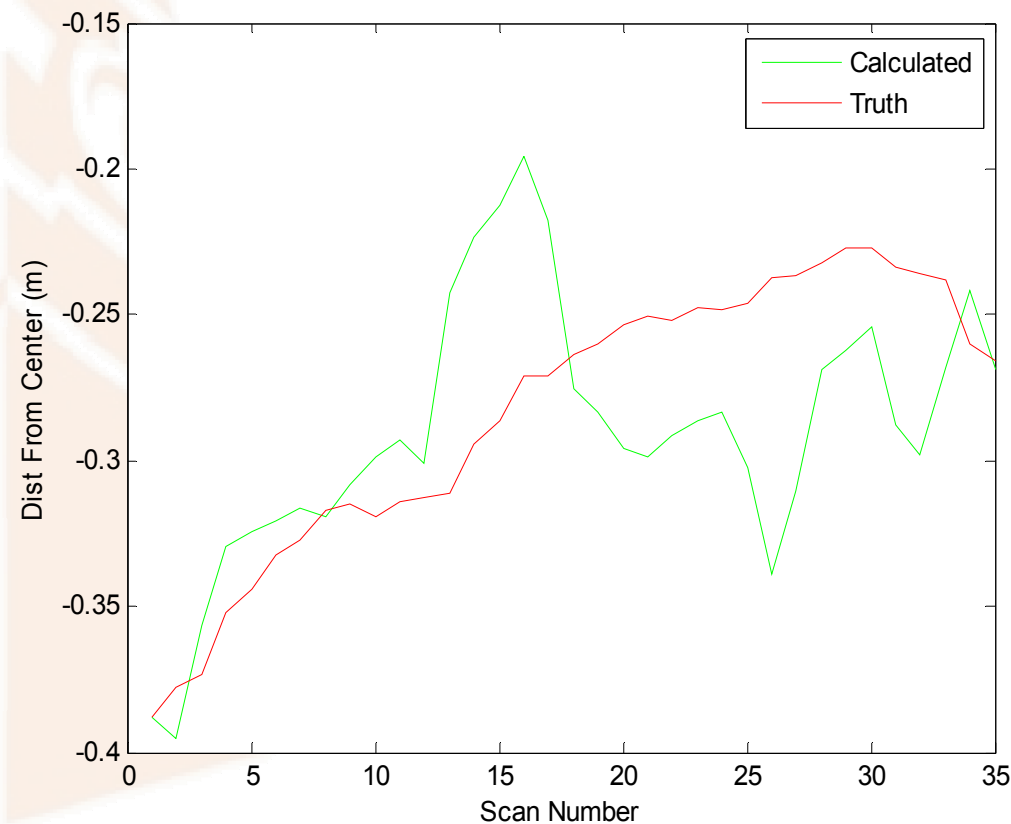
# Detecting Lane Markings

- Detect lines using increased Echo Width
- Find minimum RMS error

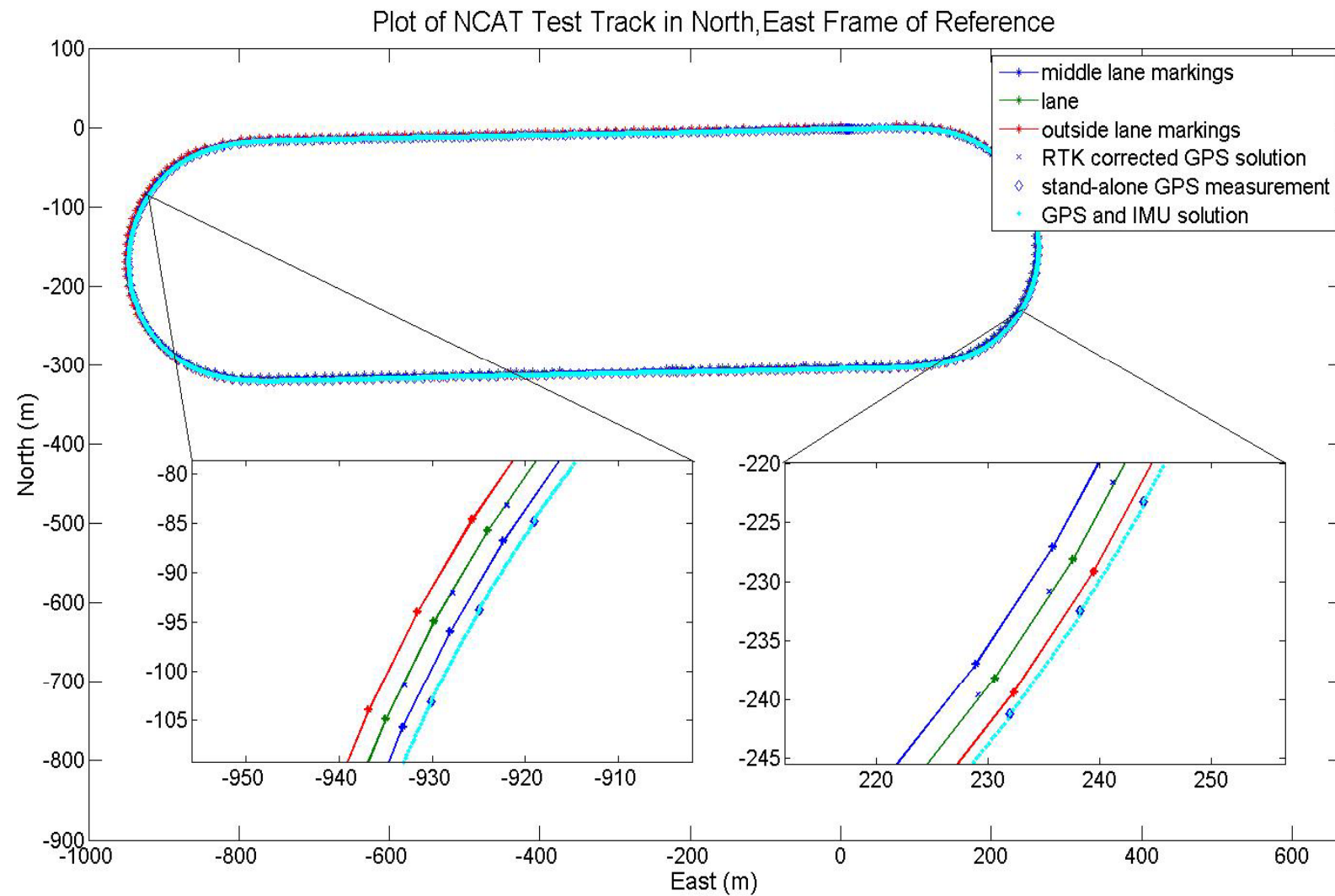




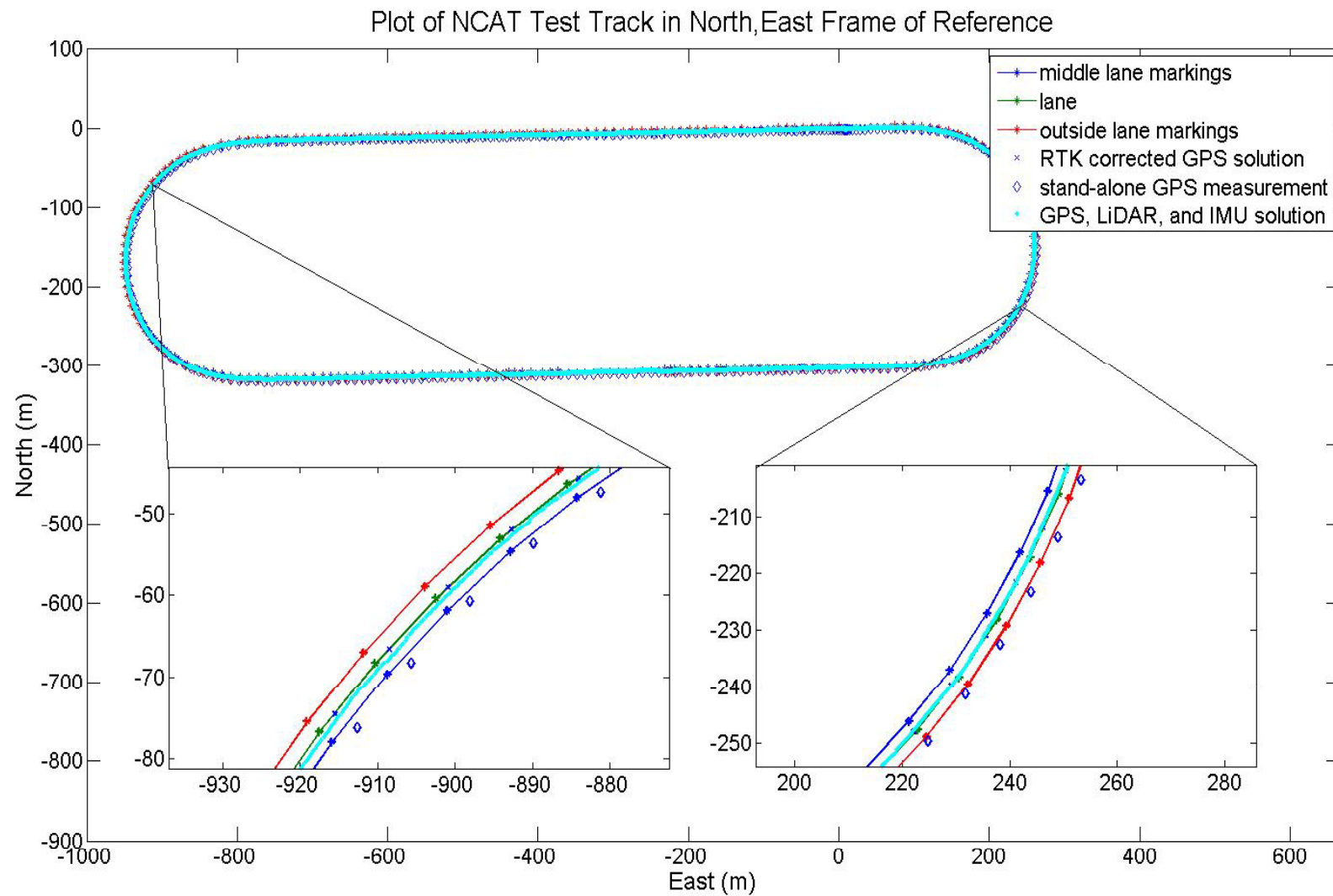
- Best on Straights
- STD of Error = .0435m
- Avg Error = .0355m



# GPS / INS

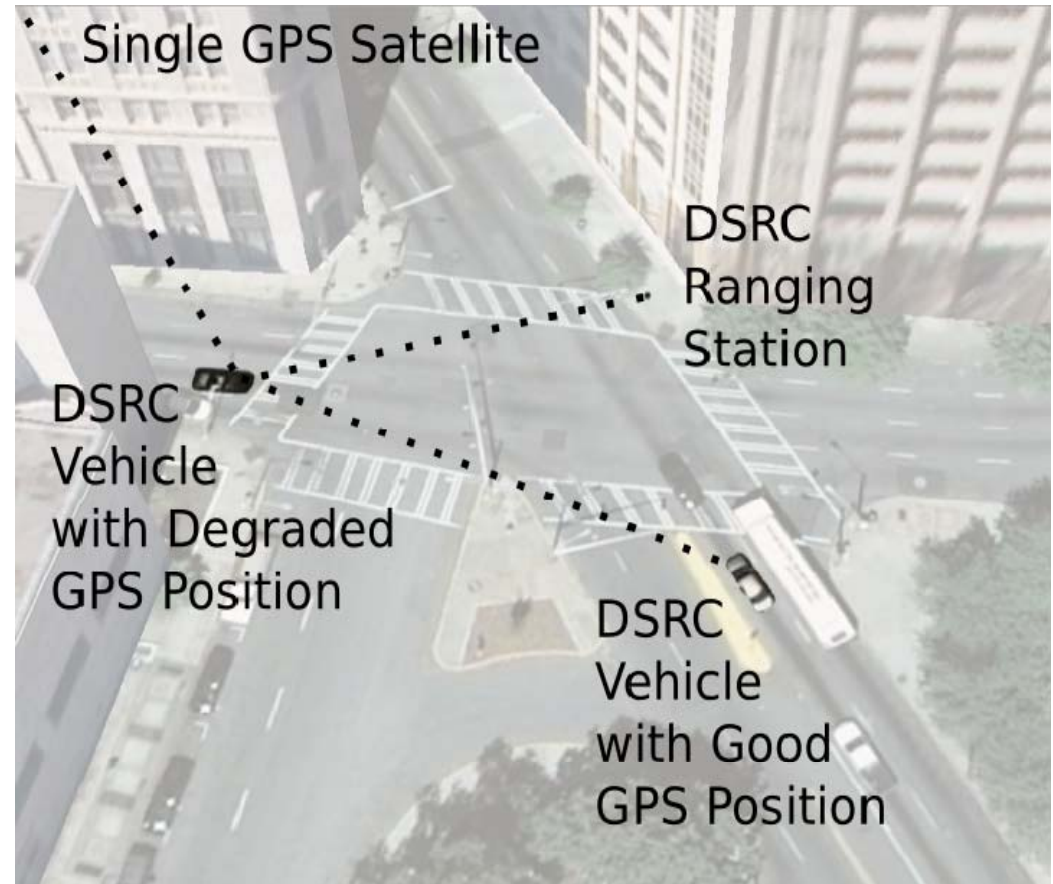


# GPS / Camera / LiDAR / INS



# Positioning With Additional Ranges

- Some scenarios provide poor GPS position
- Augment navigation with ranges to known positions
- Provides more seamless operation





# Vehicle Modeling



# Roll FBD: Sprung Mass

R = Reaction Forces

rc = roll center

$F_b$  = Damper Force

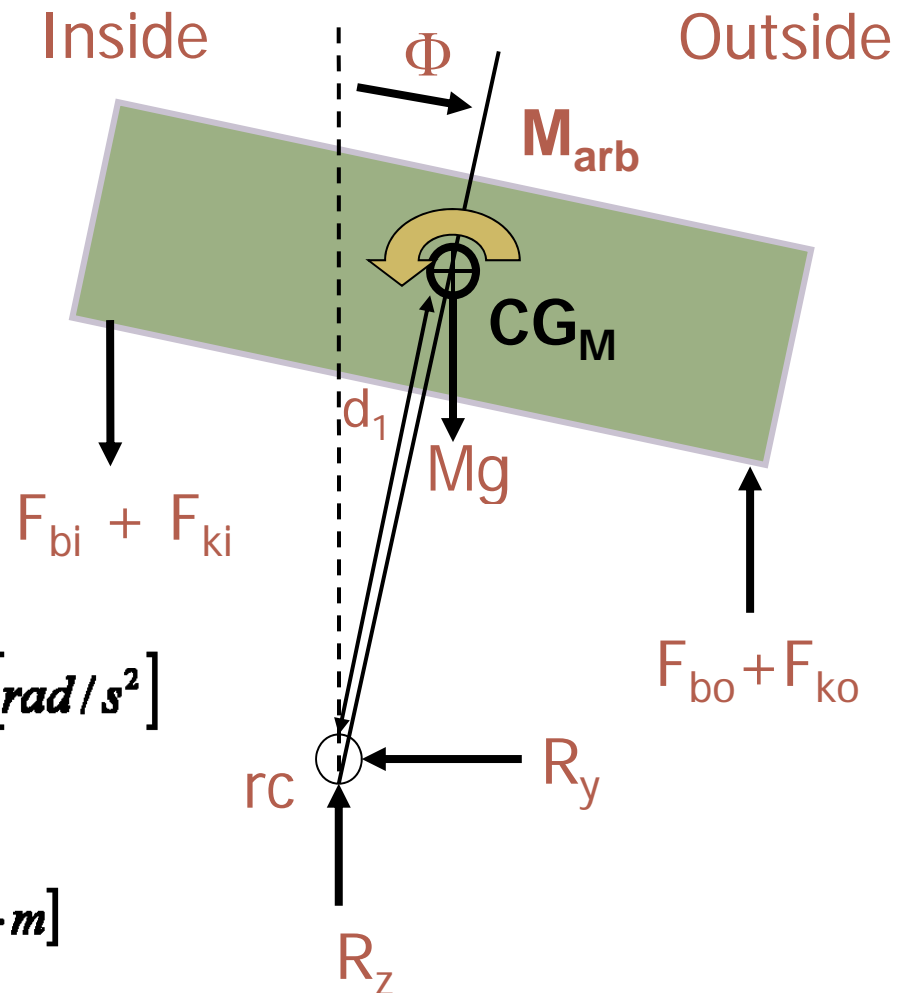
$F_k$  = Spring Force

$$\Sigma M_x = I_x \cdot \ddot{\Phi}$$

$$\ddot{\Phi} = \left( \frac{1}{I_x} \right) \cdot \left[ \begin{array}{l} -RSM - RDM + (R_z \cdot d_1 \cdot \sin(\Phi)) \\ + (R_y \cdot d_1 \cdot \cos(\Phi)) \end{array} \right] \cdot [rad/s^2]$$

$$RSM = \left[ \begin{array}{l} (0.5 \cdot k_{sf} \cdot S_{kf}^2) + (0.5 \cdot k_{sr} \cdot S_{kr}^2) \\ + k_{arbf} + k_{arbr} \end{array} \right] \cdot \Phi \cdot [N \cdot m]$$

$$RDM = (0.5 \cdot b_f \cdot S_{bf}^2) + (0.5 \cdot b_r \cdot S_{br}^2) + (0.5 \cdot b_{bf} \cdot S_{bf} \cdot S_{br})$$



# Roll FBD: Un-Sprung Mass

- Lateral Weight Transfer

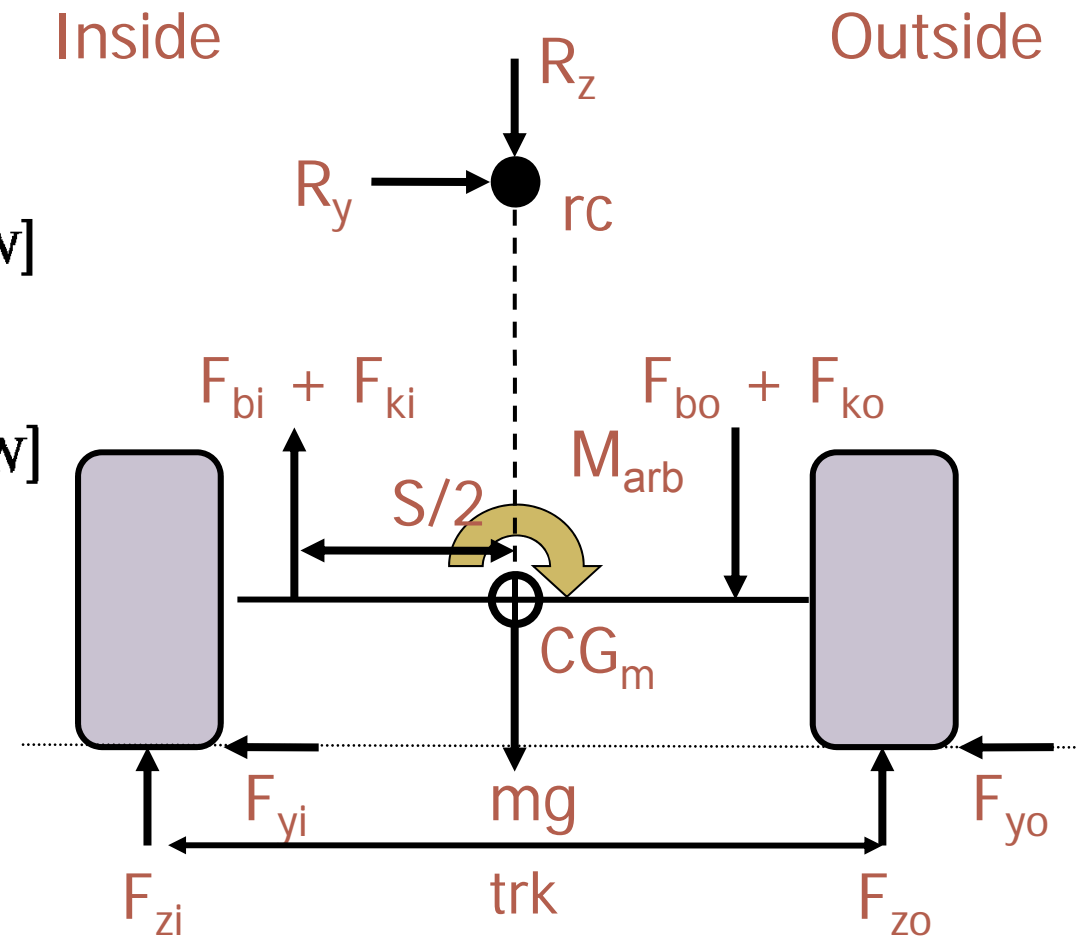
$$dF_z = [F_{zo} - F_{zi}] \cdot [N]$$

$$dF_{zf} = \frac{2}{trk_f} \cdot \left[ M_{arbf} + S_{kf} \cdot F_{kf} + S_{bf} \cdot F_{bf} + R_{yf} \cdot (h_{rcf} - h_{cgm}) + F_{yf} \cdot h_{cgm} \right] \cdot [N]$$

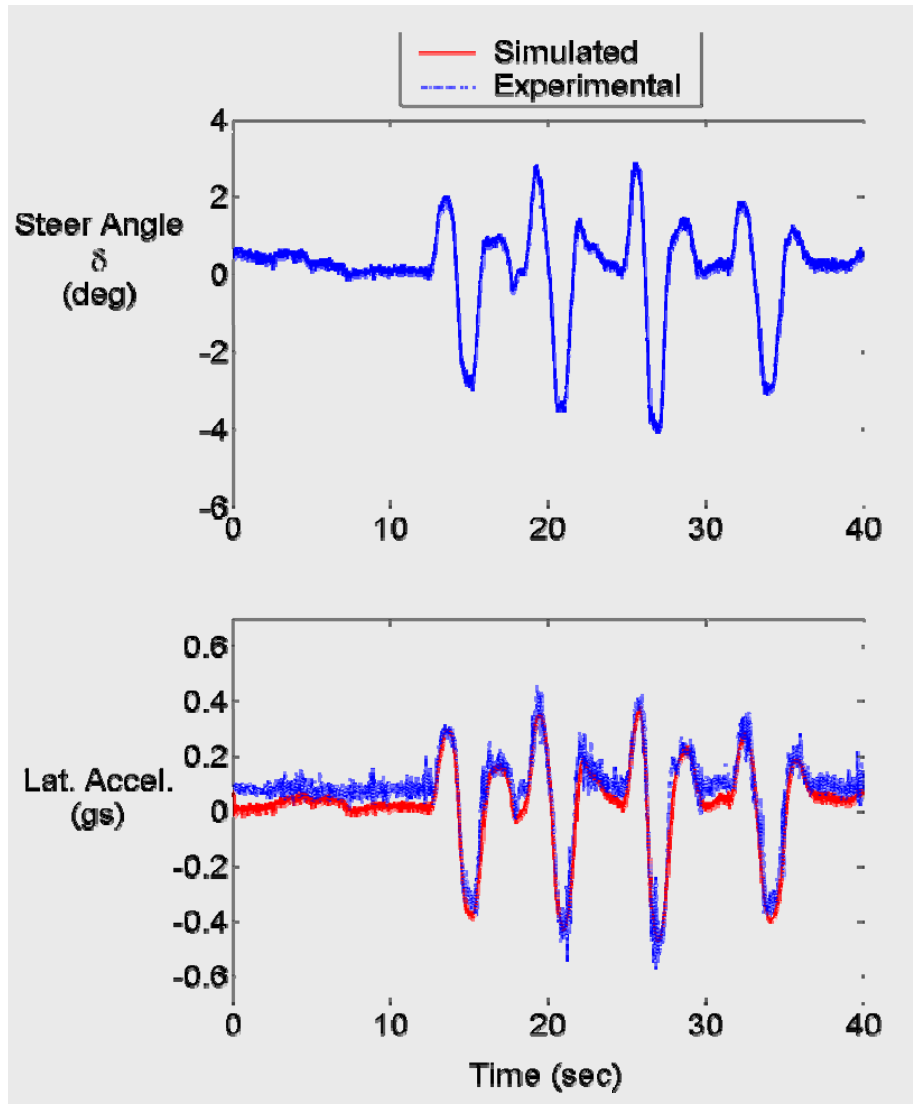
$$dF_{zr} = \frac{2}{trk_r} \cdot \left[ M_{arbr} + S_{kr} \cdot F_{kr} + S_{br} \cdot F_{br} + R_{yr} \cdot (h_{rcr} - h_{cgm}) + F_{yr} \cdot h_{cgm} \right] \cdot [N]$$

$F_z$  = Normal Force

$F_y$  = Tire Lateral Force



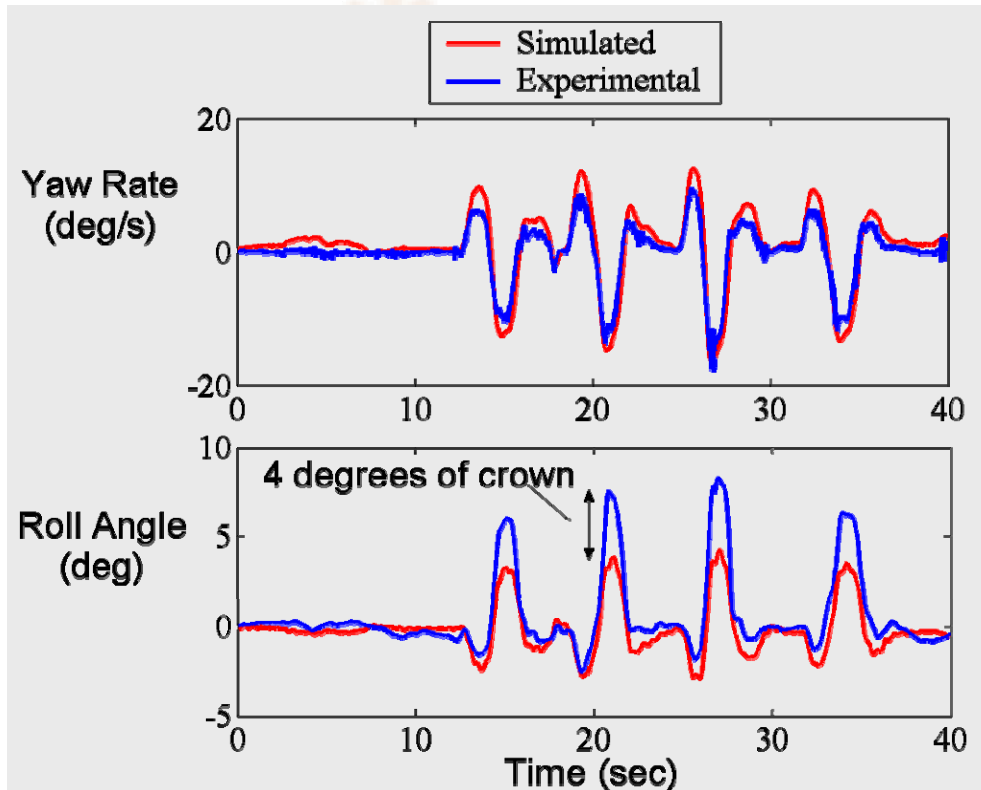
# GAVLAB Blazer Data



- Lane Change Maneuver
- Velocity  $\sim 40$  mph
- Steer Rate  $\sim 6$  deg/s
- Data collected at Auburn NCAT facility



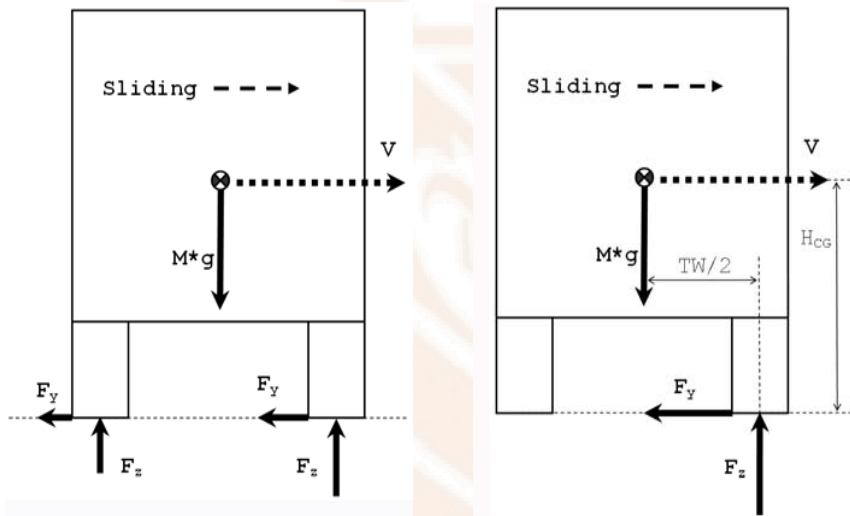
# GAVLAB Blazer Data (2)



- Simulation Matches Well
- Vehicle Model for the Blazer is same as used for the NHTSA Data
  - No Tuning Between the Two Blazers
- Crown of 4 degrees visible in the roll angle measurement

# NHTSA's Static Stability Factor (SSF) Test

$$SSF = \frac{TW}{2 \cdot H_{CG}}$$



$$\sum F_y = M \cdot a_y = F_y$$

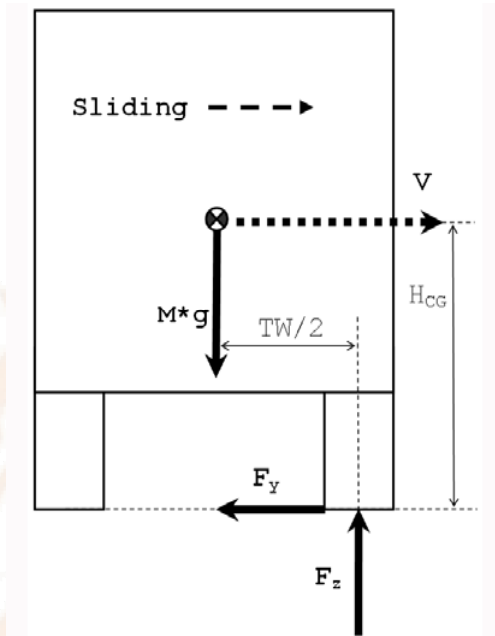
$$\sum F_z = M \cdot a_z = M \cdot g - F_z$$

$$\sum M_{CG} = \frac{TW}{2} \cdot F_z - H_{CG} \cdot F_y = 0$$

- The standard test for vehicle rollover resistance comparison for the National Highway Traffic Safety Administration (NHTSA)
- Calculated when  $F_{z_{inner}} = 0$
- Pros:
  - Simple calculation of the lateral acceleration (g's) needed for tripping a stationary vehicle
  - Good for vehicle comparisons
  - Includes the two largest rollover contributors
- Cons:
  - Ignores dynamic behaviors
  - Overlooks all other vehicle properties



# Improved Rollover Prediction Formula



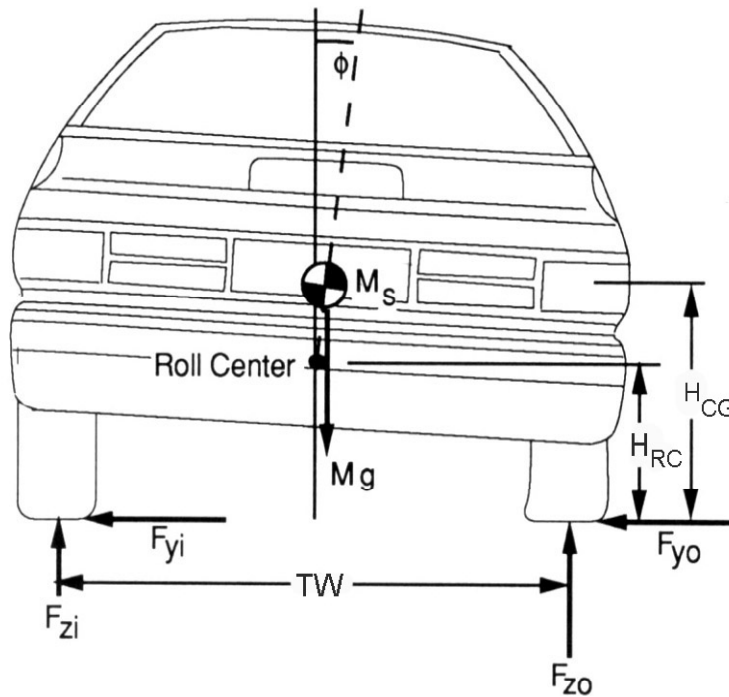
$$SSF = \frac{a_y}{g} = \frac{TW}{2 \cdot H_{CG}}$$

$$a_{y_{Rollover}} = V \cdot r = \frac{V^2}{R} = \frac{TW \cdot g}{2 \cdot H_{CG}}$$

$$V_{Rollover} = \frac{TW \cdot g}{2 \cdot r \cdot H_{CG}} = \sqrt{\frac{TW \cdot R \cdot g}{2 \cdot H_{CG}}}$$

- The SSF can be expanded to estimate the rollover lateral acceleration and velocity
- Requires estimates of track width, CG height, radius of curve or a measurement of yaw rate
- Still ignores other vehicle properties and dynamic behaviors
- $SSF < 1$  for rollover to occur typically
- Can also be used to calculate:
  - $H_{CG \text{ Rollover}}$
  - $TW_{\text{Rollover}}$
  - $r_{\text{Rollover}}$
  - $R_{\text{Rollover}}$

# Inclusion of Suspension Effects



From Gillespie: Fundamentals of Vehicle Dynamics

$$a_y = \kappa \cdot \frac{TW \cdot g}{2 \cdot H_{CG}}$$

$$V_{Rollover} = \kappa \cdot \frac{TW \cdot g}{2 \cdot r \cdot H_{CG}} = \kappa \cdot \sqrt{\frac{TW \cdot R \cdot g}{2 \cdot H_{CG}}}$$

From Gillespie:

$$a_y = \frac{TW \cdot g}{2 \cdot H_{CG}} \cdot \frac{1}{1 + R_{\phi} \cdot \left(1 - \frac{H_{RC}}{H_{CG}}\right)}$$

For passenger cars:

$R_{\phi} = .1 \text{ rad/g (roll rate)}$

$H_{RC}/H_{CG} \sim 0.5$

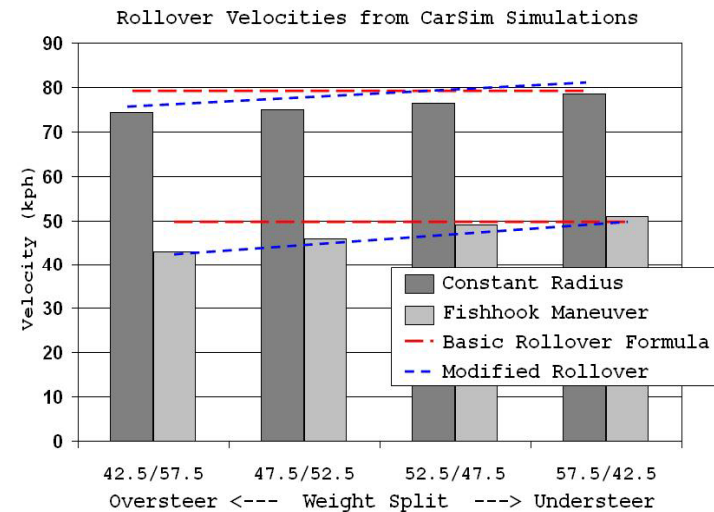
For SUVs:

$R_{\phi} = .15 \text{ rad/g (roll rate)}$

$H_{RC}/H_{CG} \sim 0.4$

# Empirical Trends Noticed with Changes in Weight Split

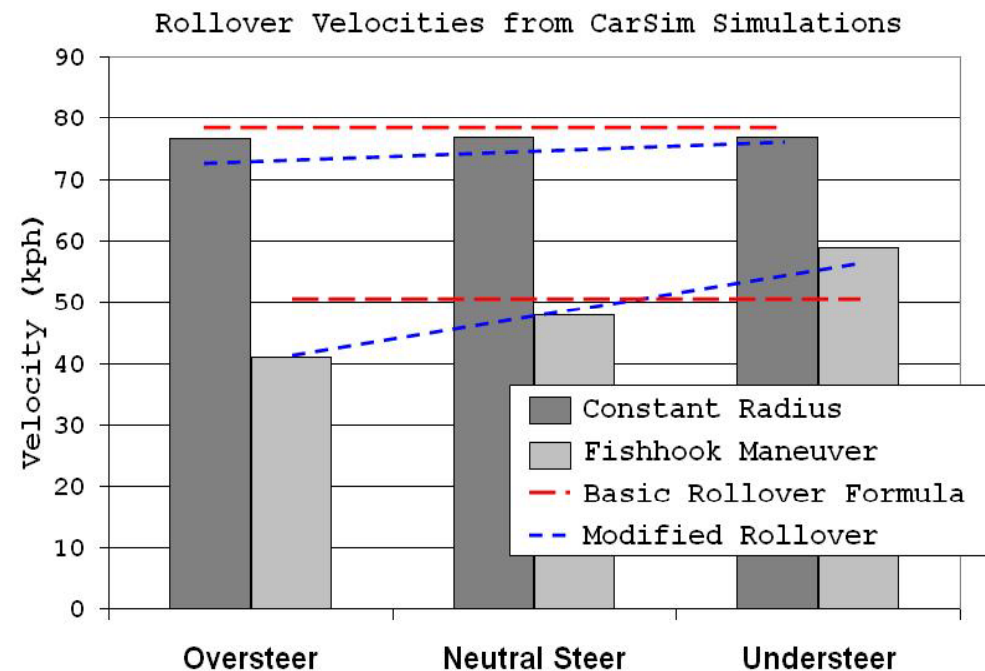
- Using simulation in CarSim of the CR and Fishhook maneuvers, rollover velocities were recorded for different weight splits
- A trend was observed, and a scale factor using the understeer gradient was added to the rollover prediction equations



Constant Radius						
WS (F/R)	$K_{US}(deg/g)$	CarSim	Eq. (3.15)	% err.	Eq. (3.41)	% err.
42.5 / 57.5	-0.139	74.2	79.7	7.4 %	71.6	3.6 %
47.5 / 52.5	-0.0464	74.7	79.7	6.7 %	72.8	2.5 %
52.5 / 47.5	0.0464	76.2	79.7	4.6 %	74.0	2.9 %
57.5 / 42.5	0.139	78.2	79.7	1.9 %	75.0	4.3 %
Fishhook						
42.5 / 57.5	-0.139	43	49.6	15.3 %	42.9	0.2 %
47.5 / 52.5	-0.0464	46	49.6	7.8 %	44.4	3.6 %
52.5 / 47.5	0.0464	49	49.6	1.2 %	46.9	4.5 %
57.5 / 42.5	0.139	51	49.6	2.8 %	49.6	2.8 %

# Empirical Trends Noticed with Changes in Cornering Stiffness

- The same test procedures were performed with changes in cornering stiffness
- Similar trends in the rollover velocity can be shown
- Generally, the accuracy of the modified rollover prediction formula still holds true



Constant Radius						
Config.	$K_{US}(deg/g)$	CarSim	Eq. (3.15)	% err.	Eq. (3.41)	% err.
Oversteer	-1.82	76.6	79.7	4.1 %	71.0	7.9 %
Neutral Steer	0.0	76.8	79.7	3.8 %	73.3	4.8 %
Understeer	1.82	76.7	79.7	4.0 %	75.7	1.3 %
Fishhook						
Oversteer	-1.82	41	51.6	25.9 %	41.4	1.0 %
Neutral Steer	0.0	48	51.6	7.5 %	47.5	1.0 %
Understeer	1.82	59	51.6	14.3 %	56.0	5.3 %



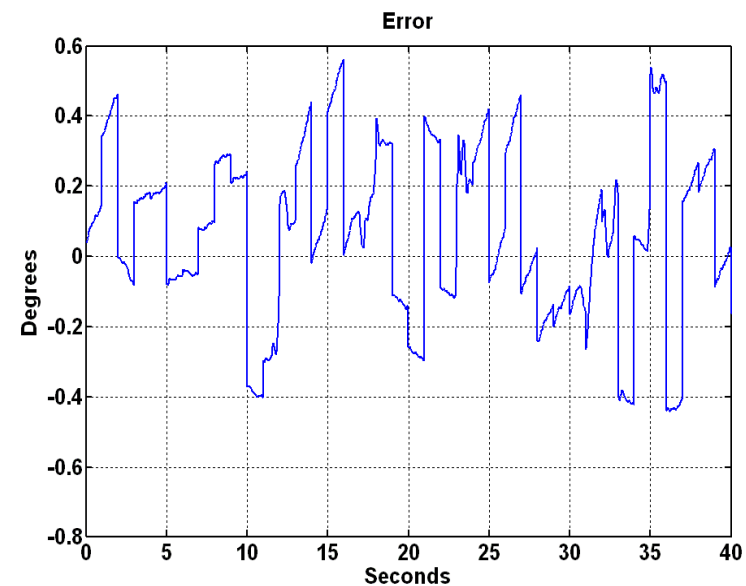
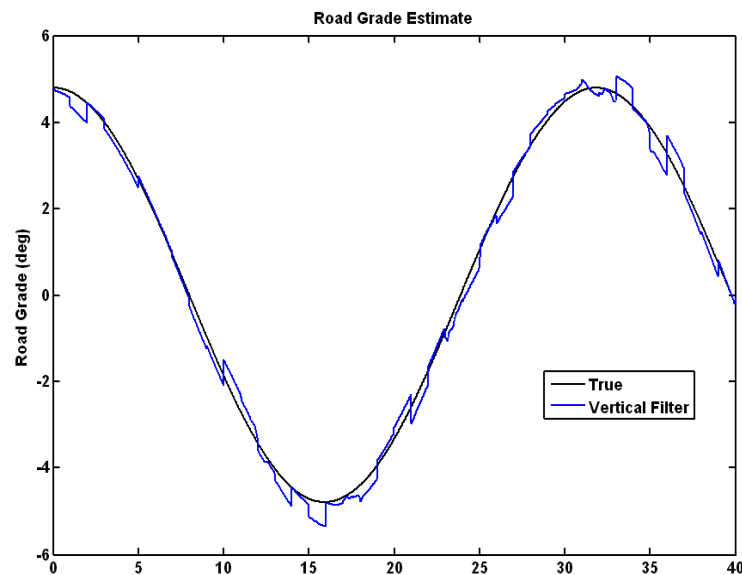
# Vehicle State Estimation



# Road Grade Estimation

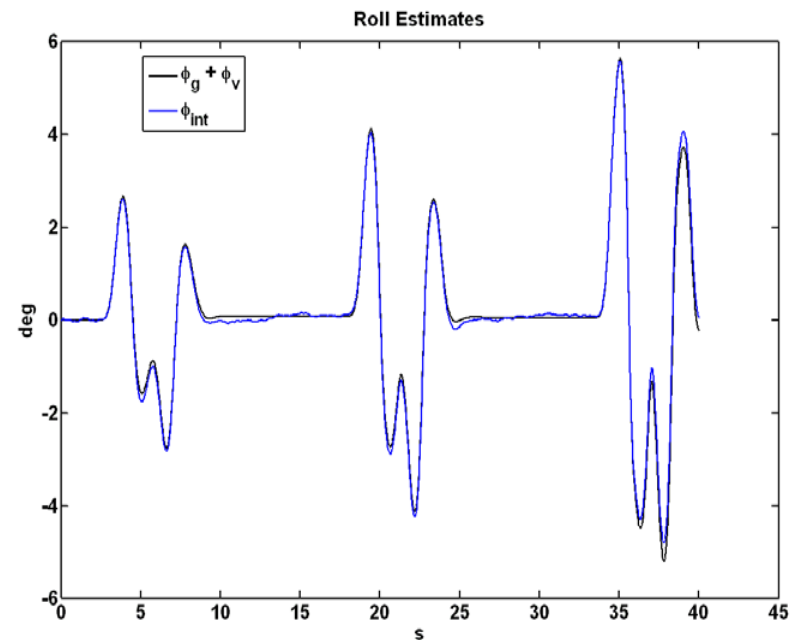
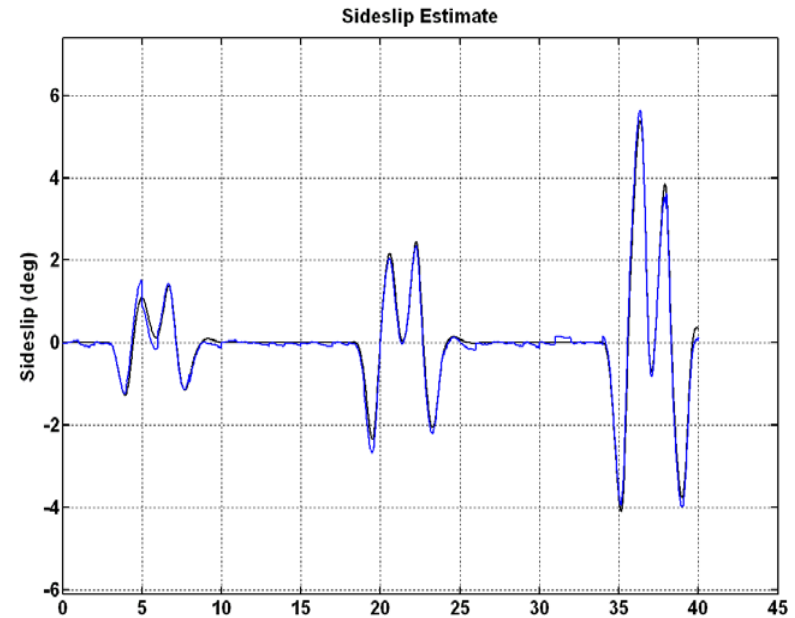
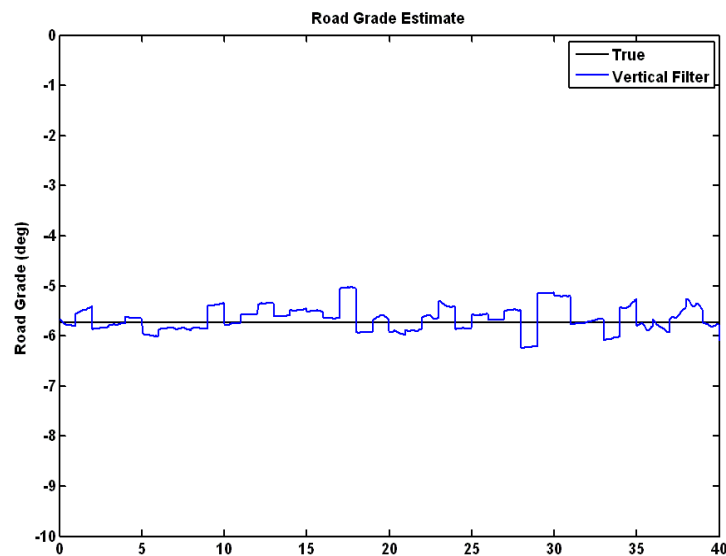
- GPS Velocity Based
  - Road Grade is generally much larger than the vehicle's suspension pitch.
  - Input from vertical accelerometer
  - GPS Velocity Accuracies  $1\sigma \approx 5\text{cm/s}$
  - $\Theta \approx \text{atan}(V_z/V_x)$
  - $V_x$  can be estimated the same way, or using wheel speed sensors.

$$\begin{bmatrix} \dot{V}_z \\ \dot{b}_z \end{bmatrix} = \begin{bmatrix} 0 & -1 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} V_z \\ b_z \end{bmatrix} + \begin{bmatrix} 1 \\ 0 \end{bmatrix} a_z + \omega$$
$$y = [1 \quad 0] \begin{bmatrix} V_z \\ b_z \end{bmatrix} + \eta$$

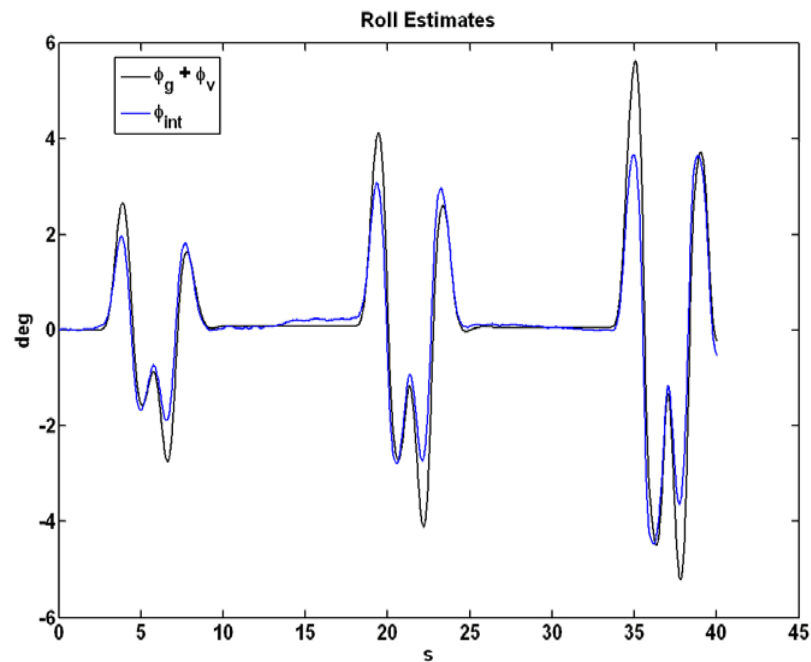


# Sideslip Estimation

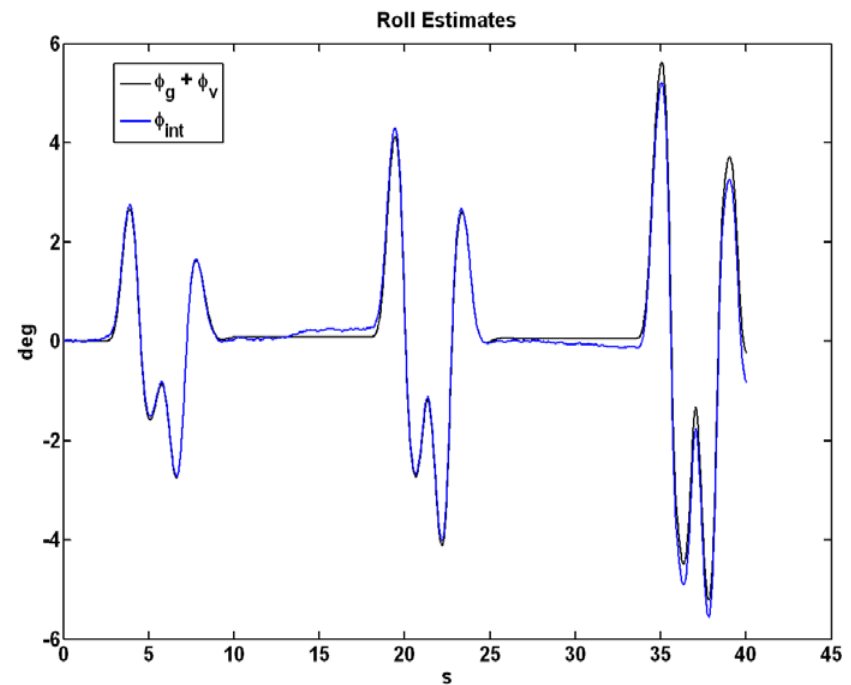
- GPS/INS Based (Single Antenna)
  - When driving straight vehicle heading = vehicle course (assuming no bank).
  - $C$  is set to  $[1 \ 0]$ , and the gyro bias is estimated.
  - When turning,  $C$  is set to  $[0 \ 0]$  and the yaw gyro is integrated to obtain a heading estimate  $\psi^*$ .



# Roll Estimation

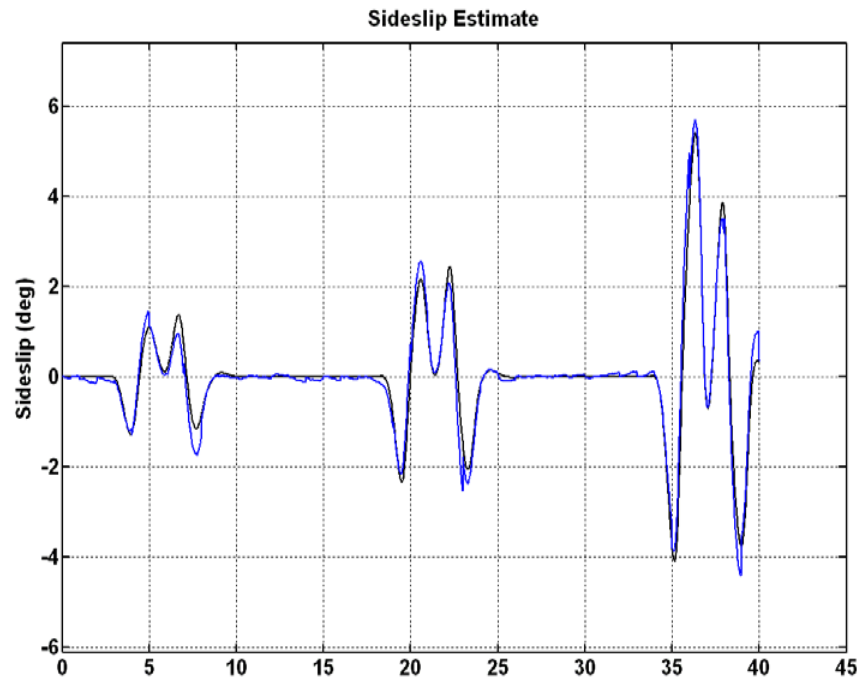


- Without Road Grade Information

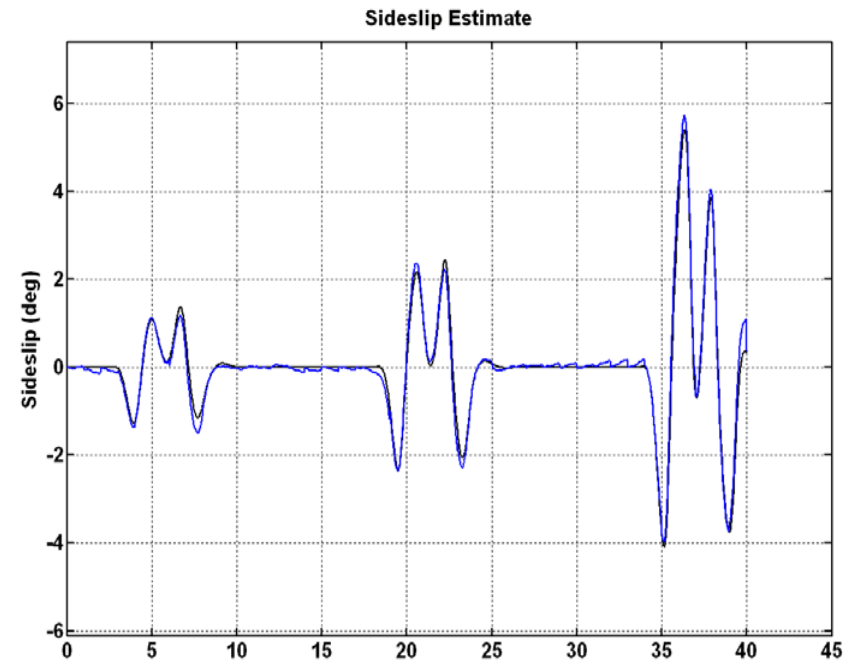


- With Road Grade Information

# Sideslip Estimation



- Without Road Grade Information



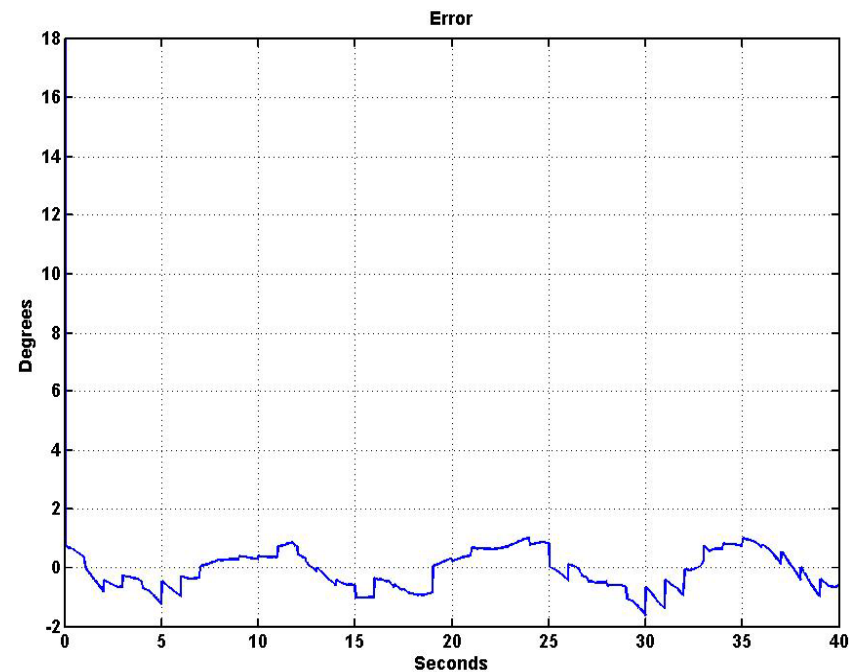
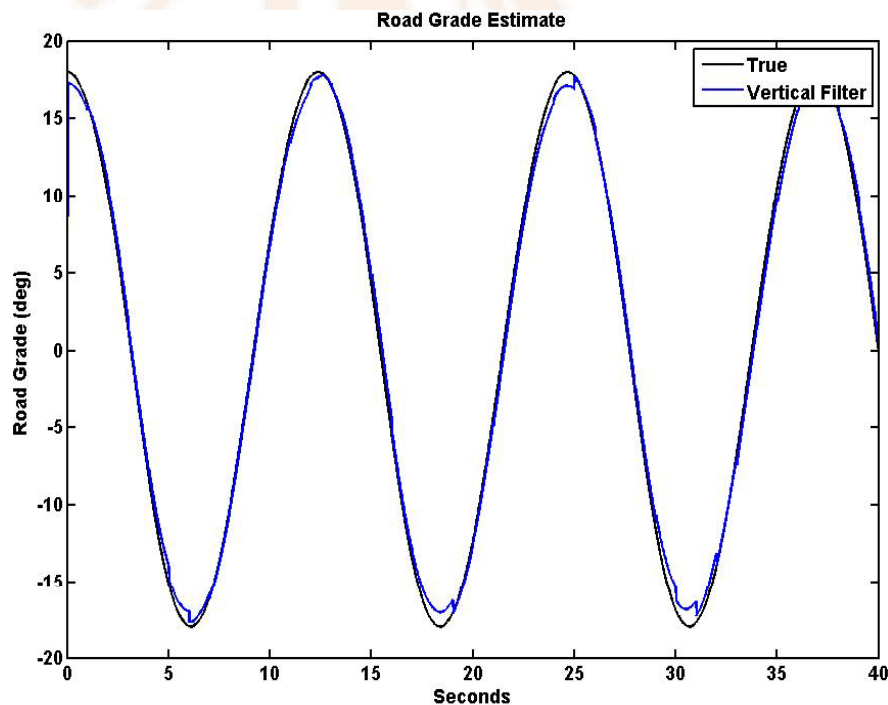
- With Road Grade Information

# Road Grade Estimation

- GPS Velocity Based
  - Road Grade is generally much larger than the vehicle's suspension pitch.
  - Input from vertical accelerometer
  - GPS Velocity Accuracies  $1\sigma \approx 5\text{cm/s}$
  - $\Theta \approx \text{atan}(V_z/V_x)$
  - $V_x$  can be estimated the same way, or using wheel speed sensors.

$$\begin{bmatrix} \dot{V}_z \\ \dot{b}_z \end{bmatrix} = \begin{bmatrix} 0 & -1 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} V_z \\ b_z \end{bmatrix} + \begin{bmatrix} 1 \\ 0 \end{bmatrix} a_z + \omega$$

$$y = \begin{bmatrix} 1 & 0 \end{bmatrix} \begin{bmatrix} V_z \\ b_z \end{bmatrix} + \eta$$



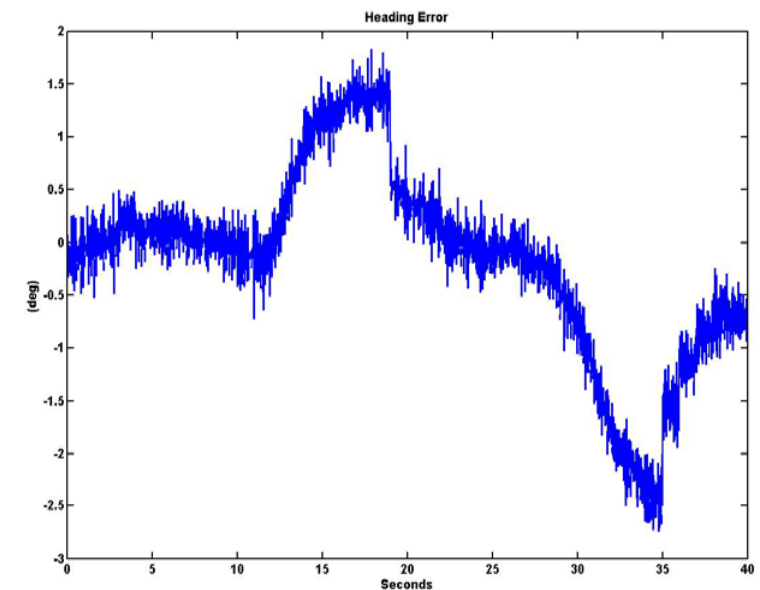
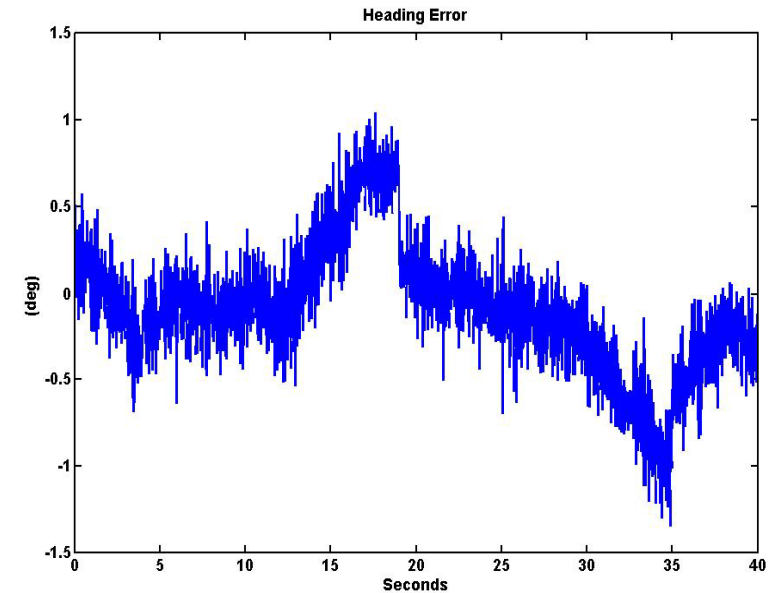
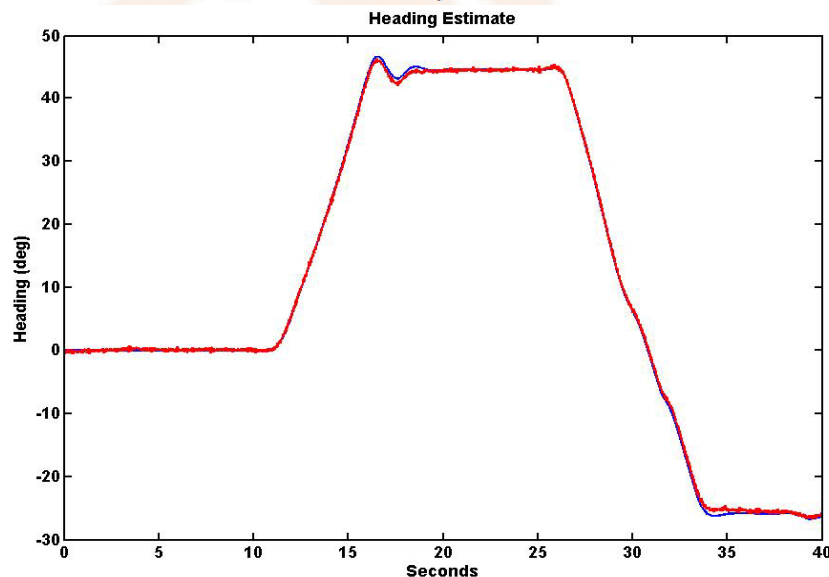


# Heading Estimation

- GPS/INS Based (Single Antenna)
  - When driving straight vehicle heading = vehicle course (assuming no bank).
  - C is set to  $[1 \ 0]$ , and the gyro bias is estimated.
  - When turning, C is set to  $[0 \ 0]$  and the yaw gyro is integrated to obtain a heading estimate  $\psi^*$ .

$$\begin{bmatrix} \dot{\psi} \\ \dot{b}_r \end{bmatrix} = \begin{bmatrix} 0 & -1 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} \psi \\ b_r \end{bmatrix} + \begin{bmatrix} 1 \\ 0 \end{bmatrix} g_r + \omega$$

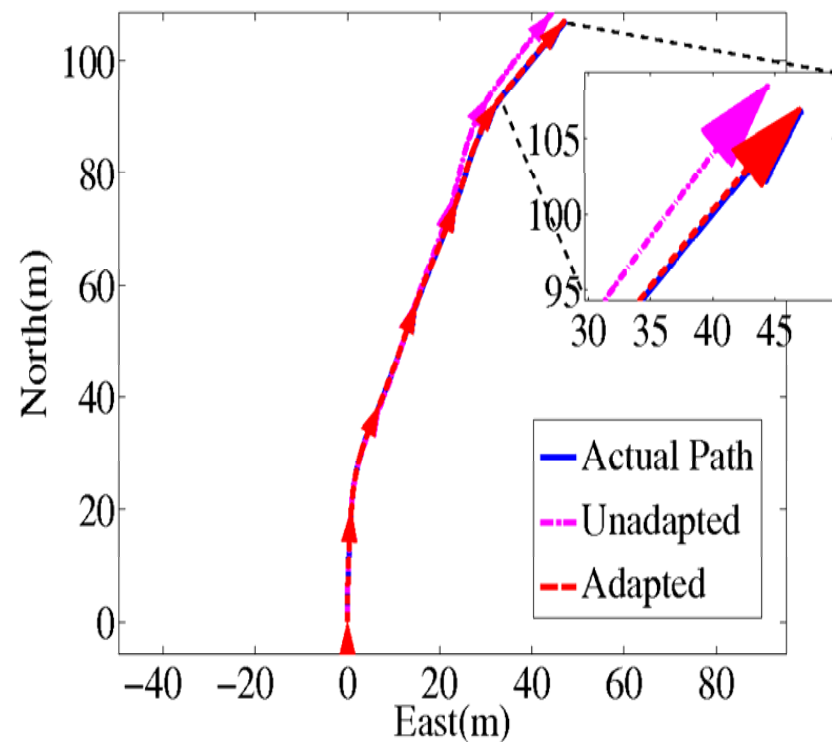
$$y = [1 \ 0] \begin{bmatrix} \psi \\ b_r \end{bmatrix} + \eta = v^{GPS} + \eta$$





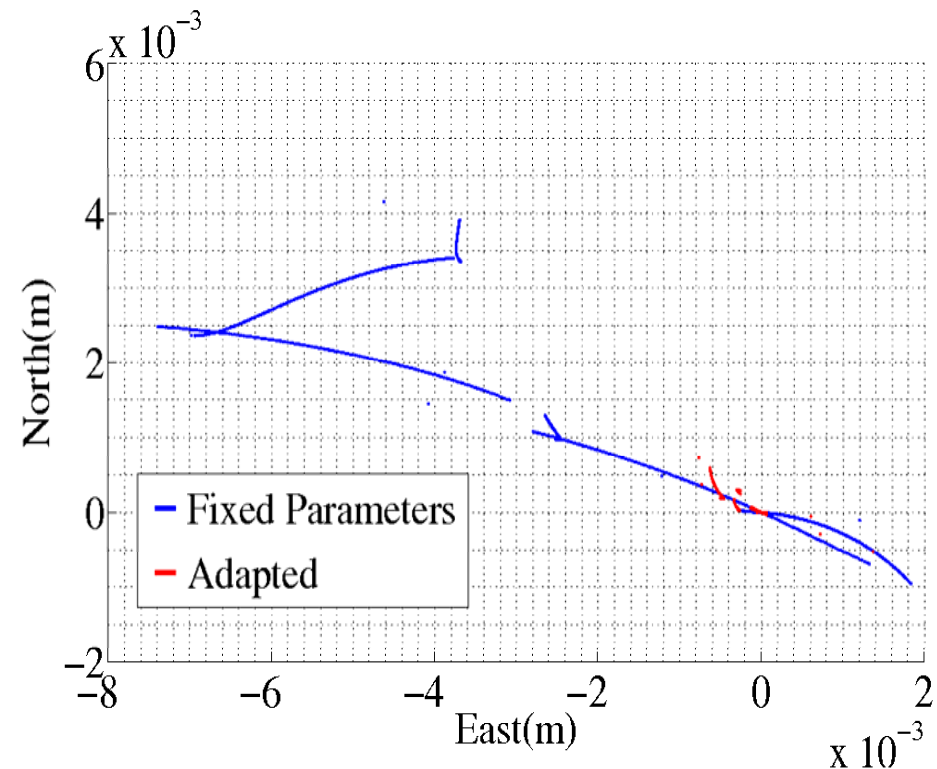
# Neural Network Based Modeling

- Neural Networks can capture Nonlinear Dynamics
- Ability to approximate any continuous function
- A flat tire is a scenario that would alter the structure of the model



# Adaptive Modeling

- Examine error introduced by each estimate
- Using fixed model: 0.0627m mean
- Using adapted model: 0.000217m mean



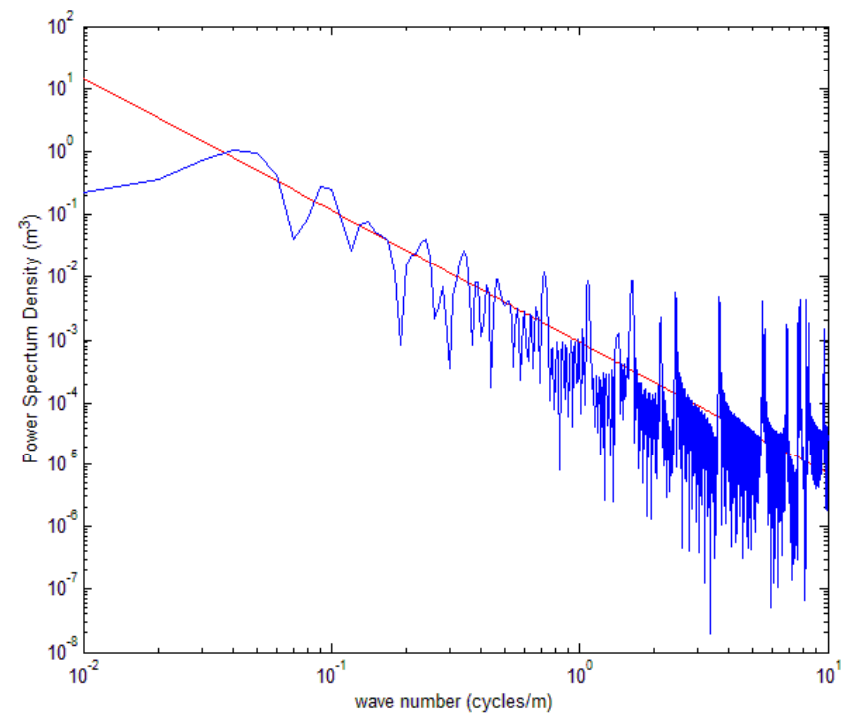
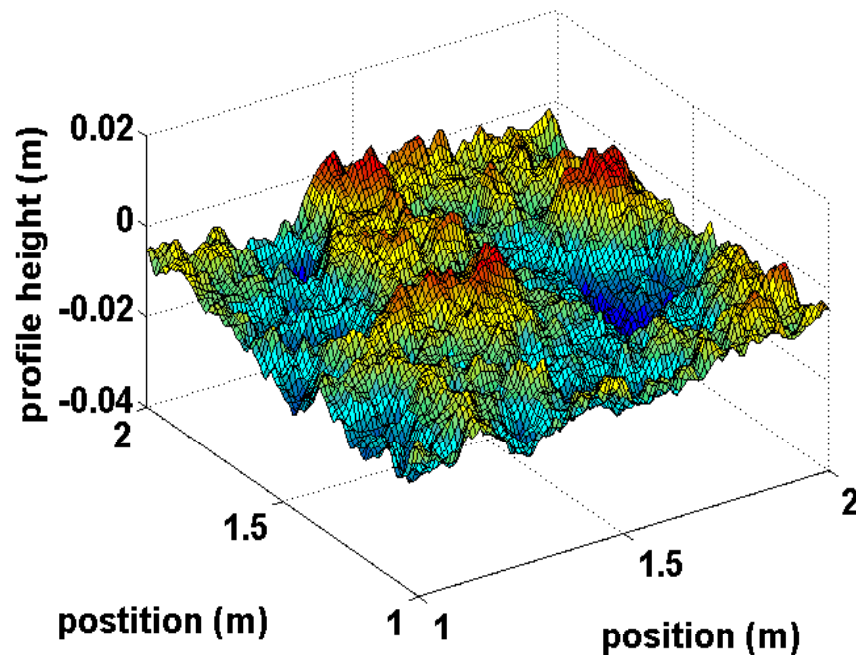


# Terrain Characterization



# Terrain Characterization – Profile Generation

- Methodologies have been developed to determine critical roughness parameters based on Power Spectral Density
- Rough Surfaces can be Generated based on the critical roughness parameters
- Rough terrain can be implemented to induce vehicle vibration into the simulation environment



# Terrain Characterization

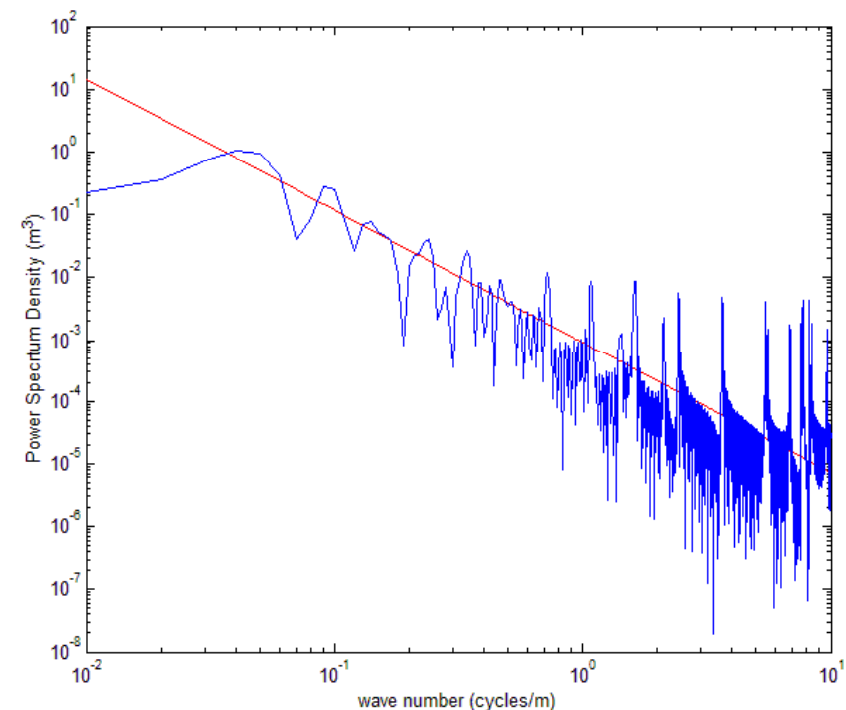
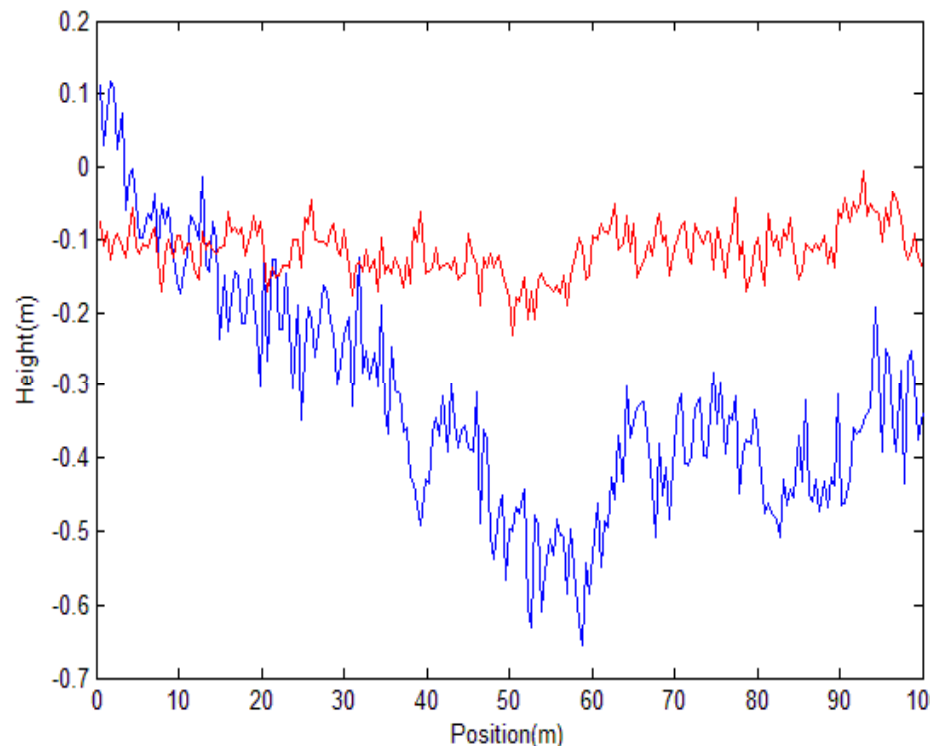
## 2D Terrain Profile Generation

- Fractal profile using Weierstrass-Mandelbrot function
- Fit fractal parameters  $G$  &  $D$

$$\Phi(\omega) = R(\omega)^{-k}$$

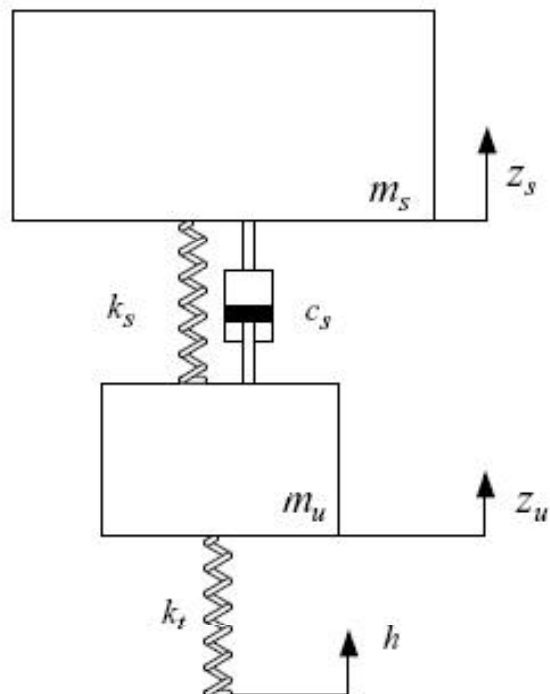
$$\bar{\Phi}(\omega) = \frac{G^{2(D-1)}}{2 \ln \gamma} \frac{1}{\omega^{(5-2D)}}$$

$$h(x) = L \left( \frac{G}{L} \right)^{(D-1)} \sum_{n=1}^{n_{max}} \frac{\cos\left(\frac{2\pi\gamma^n}{L}x + \phi_n\right)}{\gamma^{(2-D)n}}$$



## Vehicle Simulations

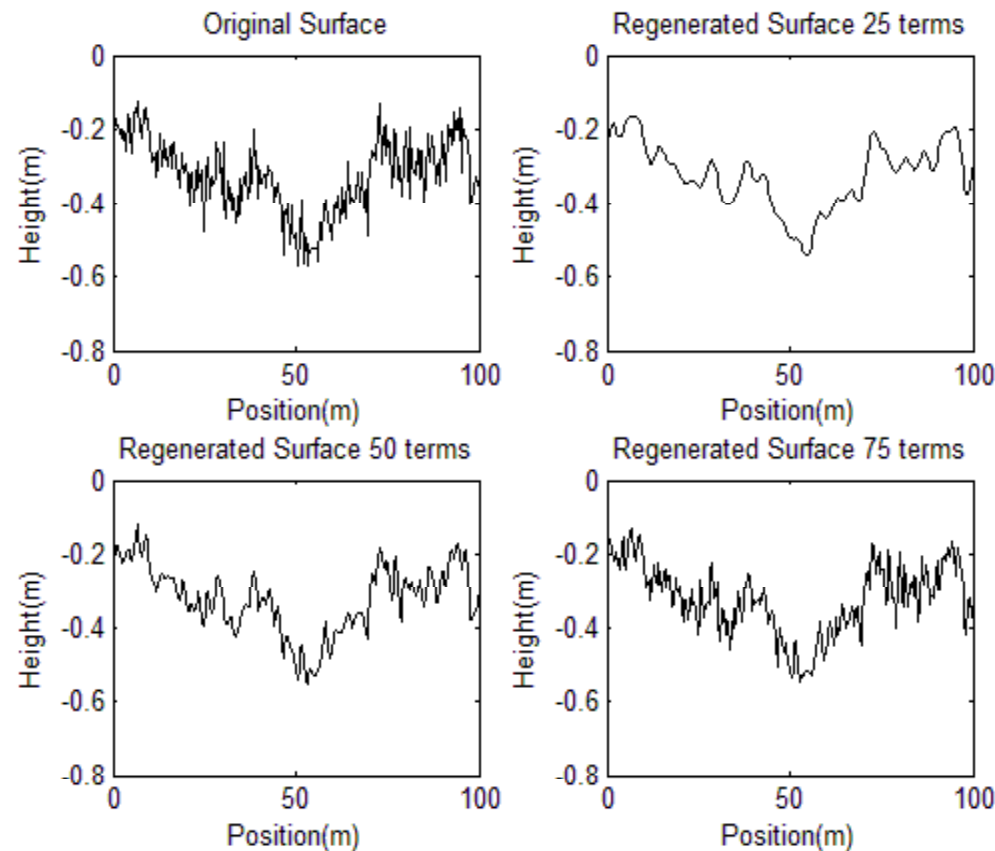
- Matlab/Simulink Quarter Car Model
  - Simple models to help better understand the effect of the terrain on the vehicle
- Carsim
  - More sophisticated models will ultimately be used to capture effects such as pitch and roll



# Terrain Characterization

## Fourier Transform

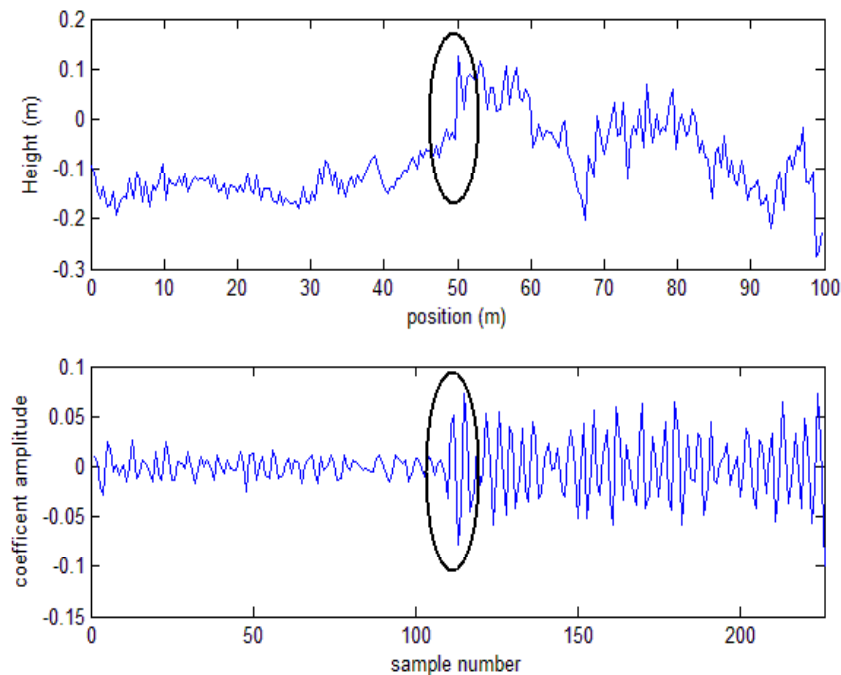
- Can be used to generate a simplified terrain
- Take FFT then take the IFFT with a limited number of terms



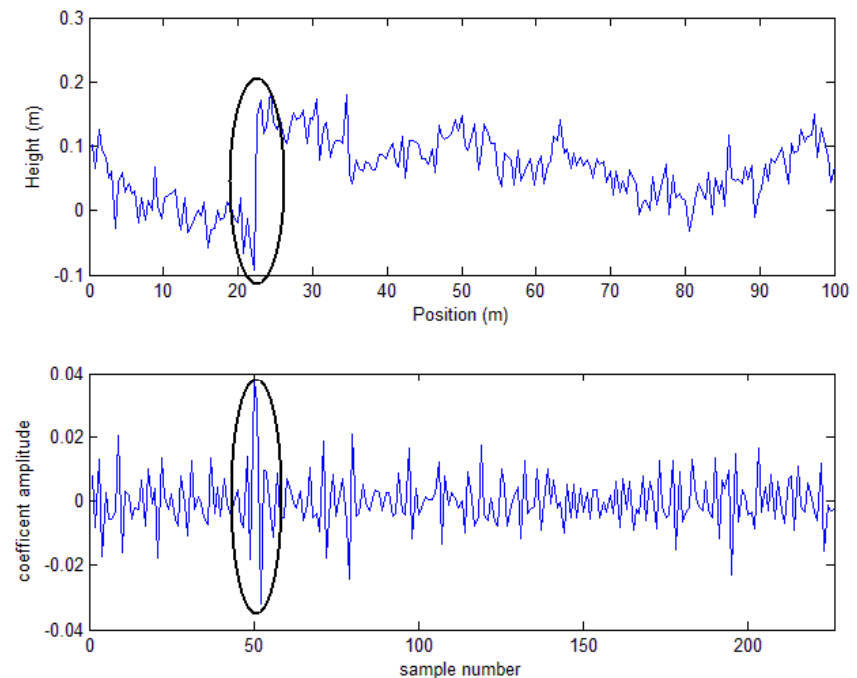
## Wavelet transform

- Analyzes the profile at a resolution matched to each scale
- The high frequency components can be extracted to detect discontinuities and changes in roughness

### Terrain Profile with a change in roughness



### Terrain Profile with a step increase





## Prowler UGV



# Vehicle – Prowler ATV

**Power Train :** Fully Automatic Transmission with Limited Slip 4WD, 4WD Diff Lock, and 2WD

**Construction :** Sealed Tubular Structure with Chrome-Moly Roll Cage and Cargo Racks

**Top Speed :** 63 mph (4WD, Hi Range)

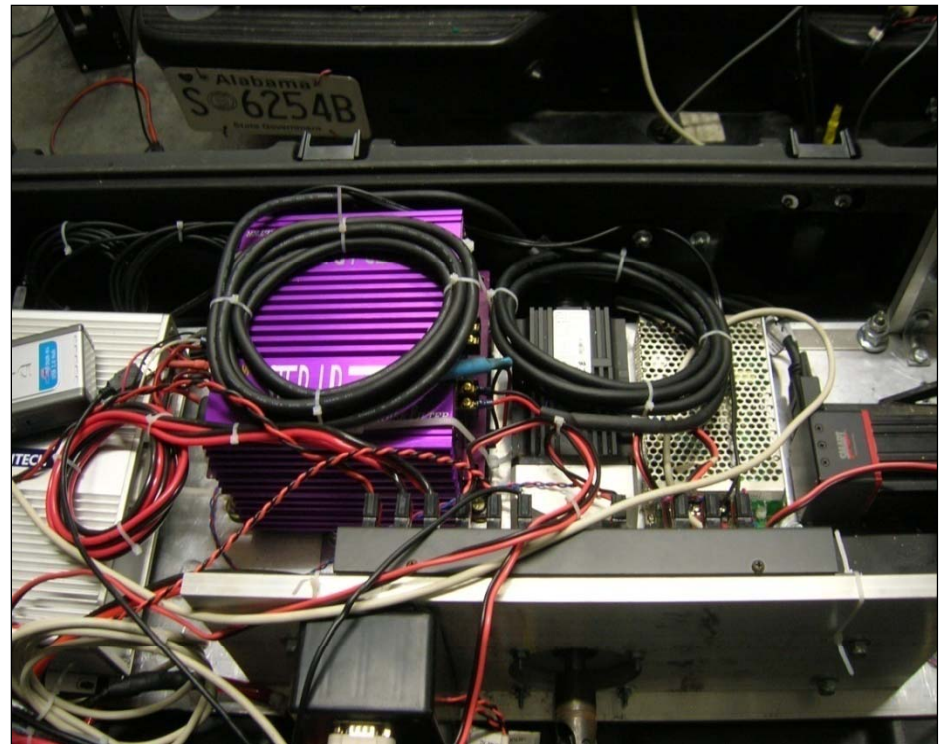
**Suspension :** Independent Double Wishbone with Adjustable Preload Reservoir Shock Absorbers

**Payload :** 1000 lb (1+ : 1 payload to weight ratio exclusive of crew)

**Towing Capacity :** 2250 lb (terrain dependent)



# Prowler ATV Automation



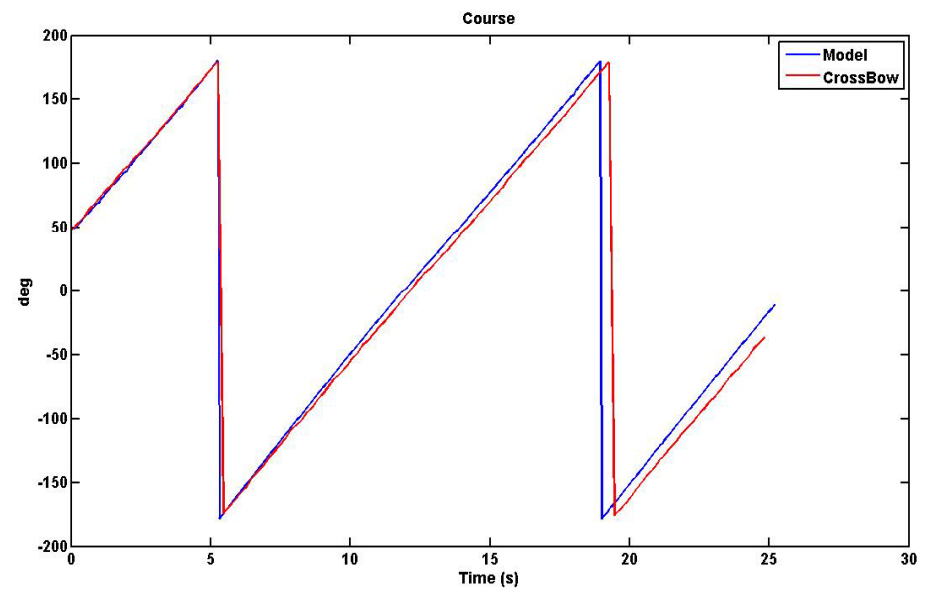
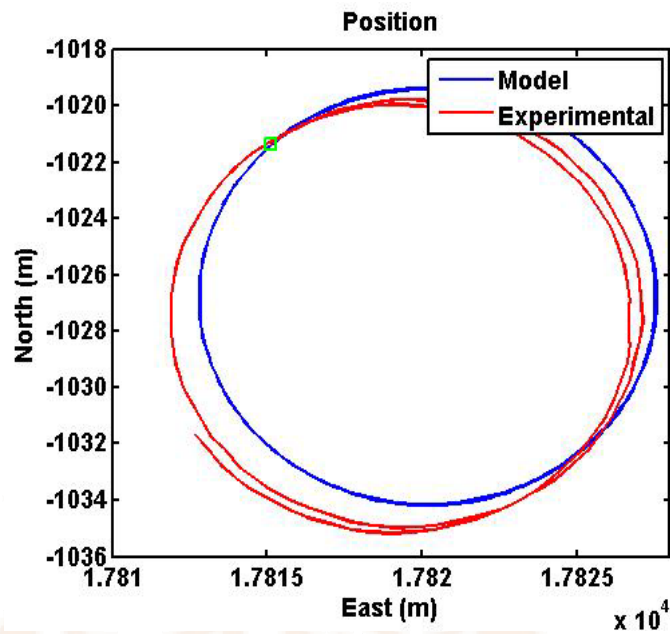


# Prowler Autonomous Control

- Generate desired Waypoints manually
- Create output waypoint file
- Use heading error, yaw rate error, and velocity error to create desired steer angle and throttle position



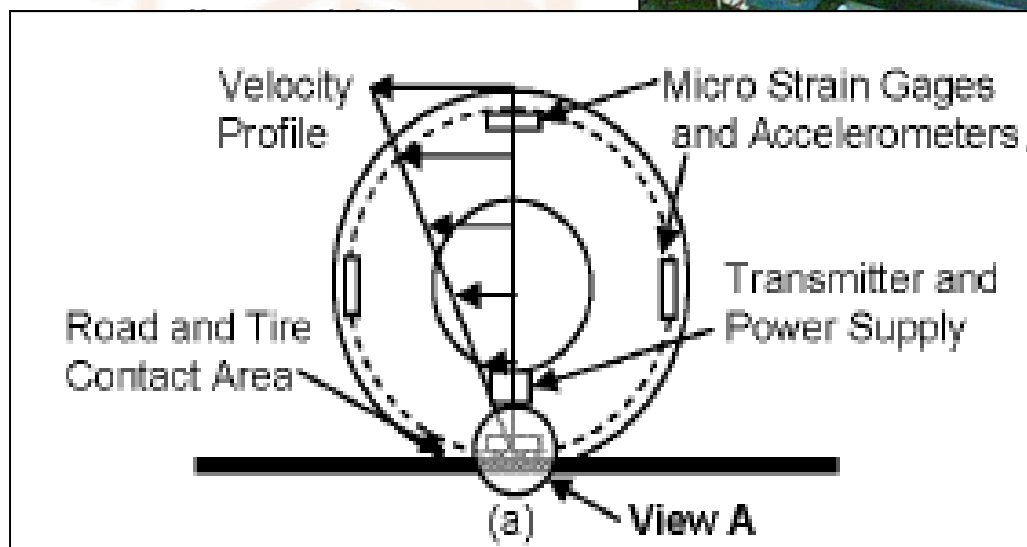
# Model Validation



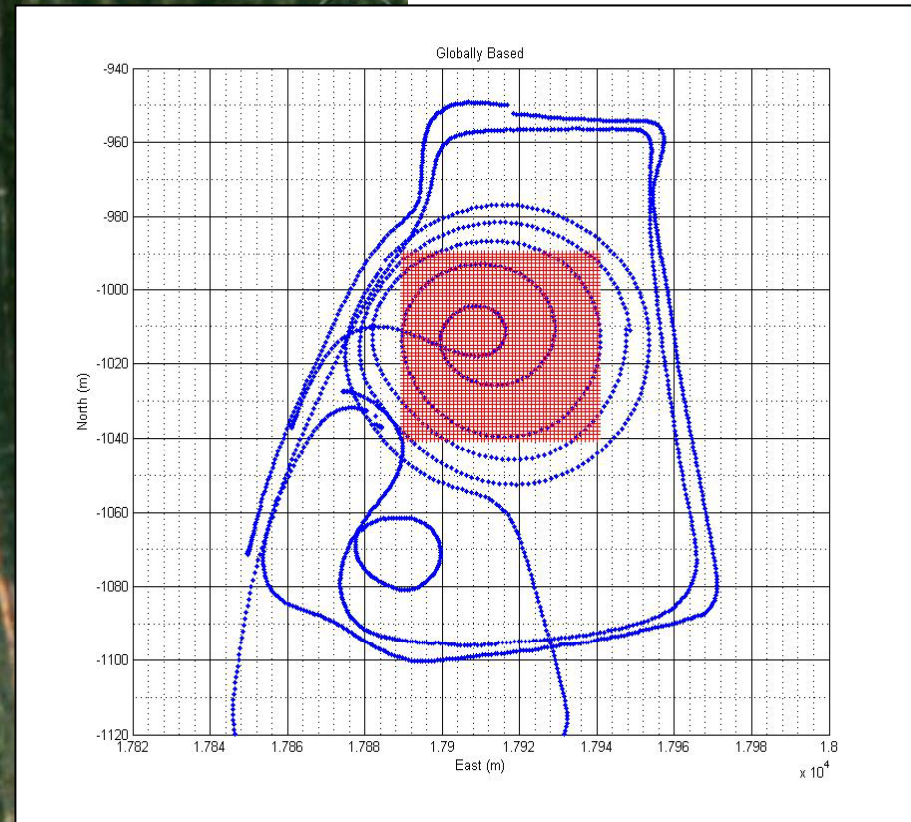
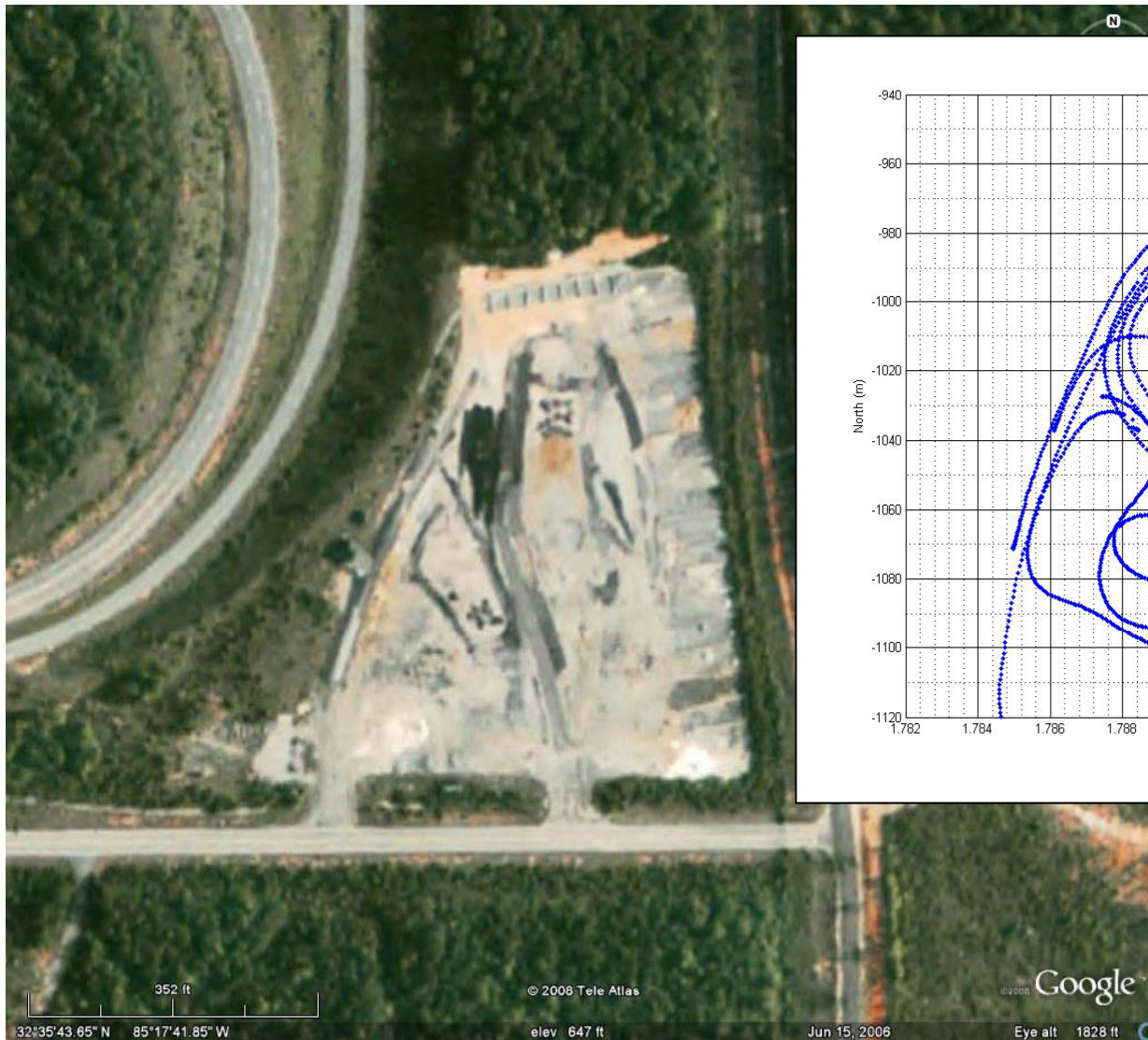


# Tire Test Stand

- Strain Gauges mounted along inner tire surface
- Wireless Data transmission module
- Ability to monitor and model tires more accurately and provide valuable information to



# Experimental Test Grid



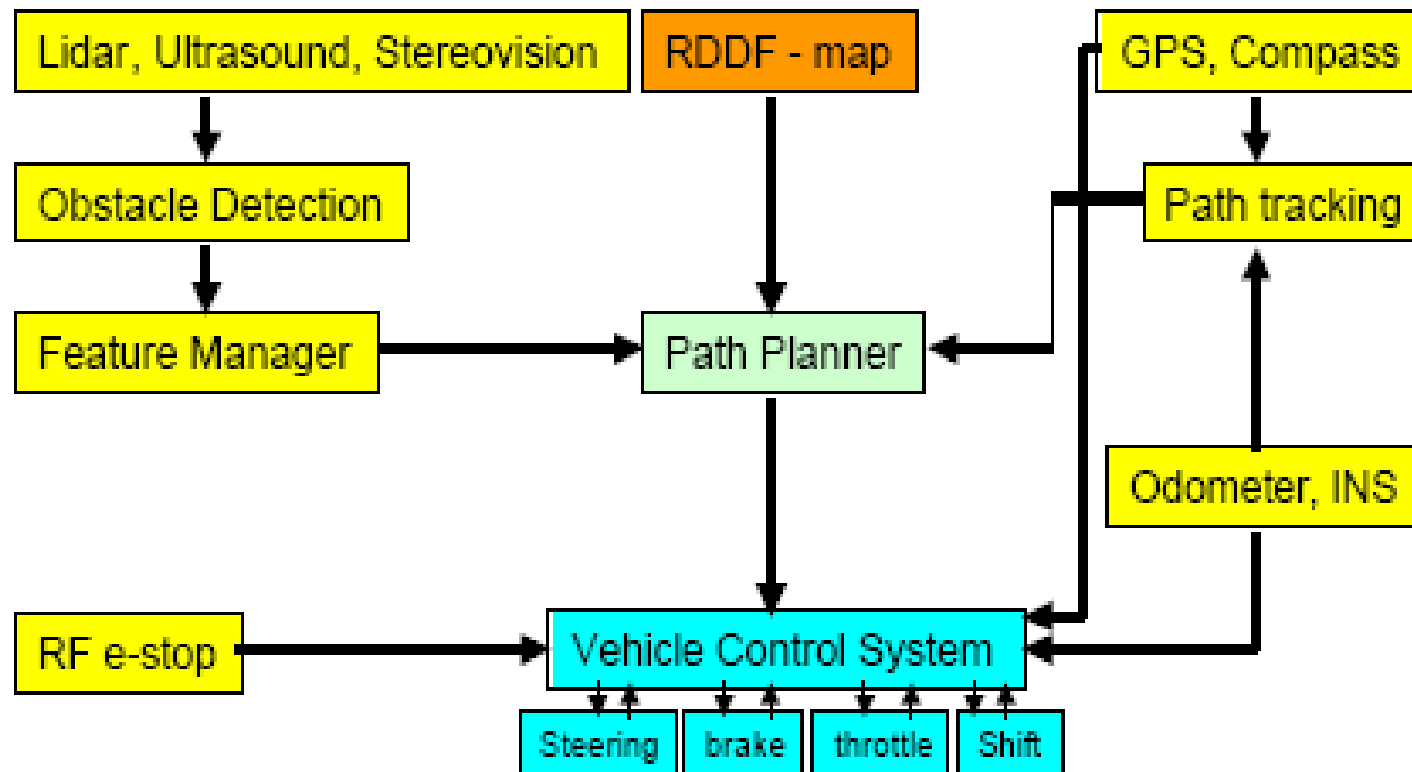


# UGV Fault Diagnostics / Health Monitoring

- Corporate Partner:
  - *Global Technology Corporation (GTC), Atlanta, GA*
- UGV Platform – Prowler ATV
  - Automated and maintained by the Auburn University GAVLAB
- Tire Pressure System (TPS)
  - Wireless sensor network that transmits temperature and pressure from inside of the tire to the primary vehicle computer
- Goal: Fault Diagnostics / Mission Planning
  - Path Planning
  - Vehicle Modeling
  - Automation
  - Online Vehicle Monitoring



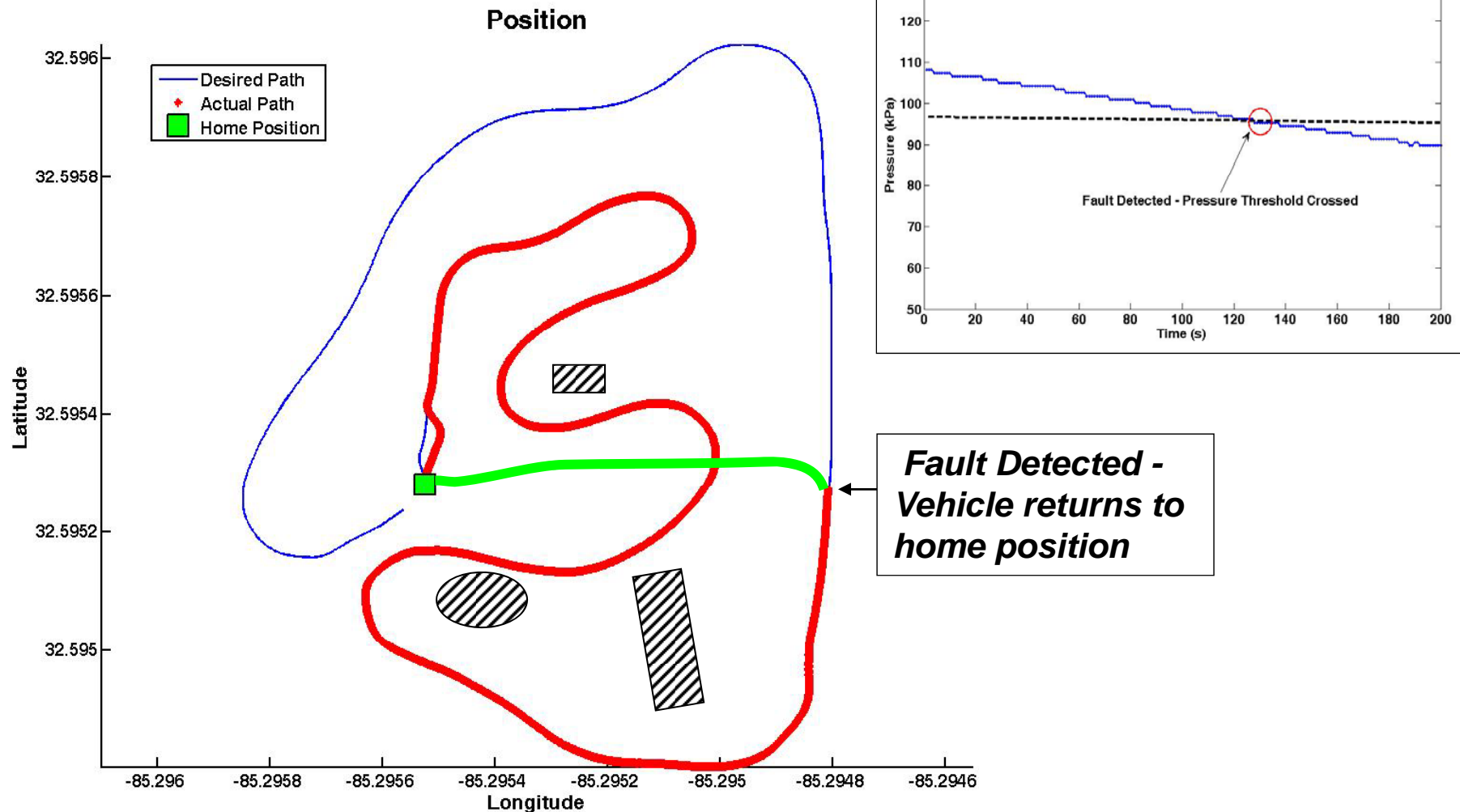
# Fault Tolerant Control with Goal Modification



The purpose of the goal modification module is to adjust the cost functions of the path planner and the low-level control parameters due to detected and identified failure modes.

# UGV Fault Diagnostics – Flat Tire

Work done in collaboration with Globatal



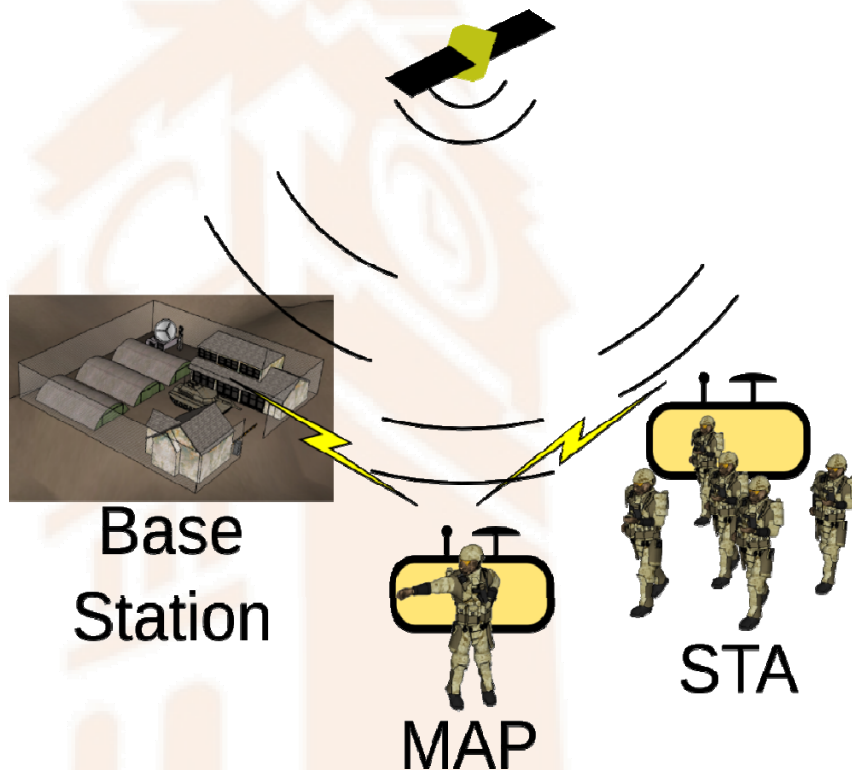


## WiFi/GPS Integration

SBIR with IS4S  
(lead), Auburn,  
SAIC, and  
Rockwell Collins

# Wi-Fi/GPS Concept Overview

- Ad-hoc networking
  - Assured availability

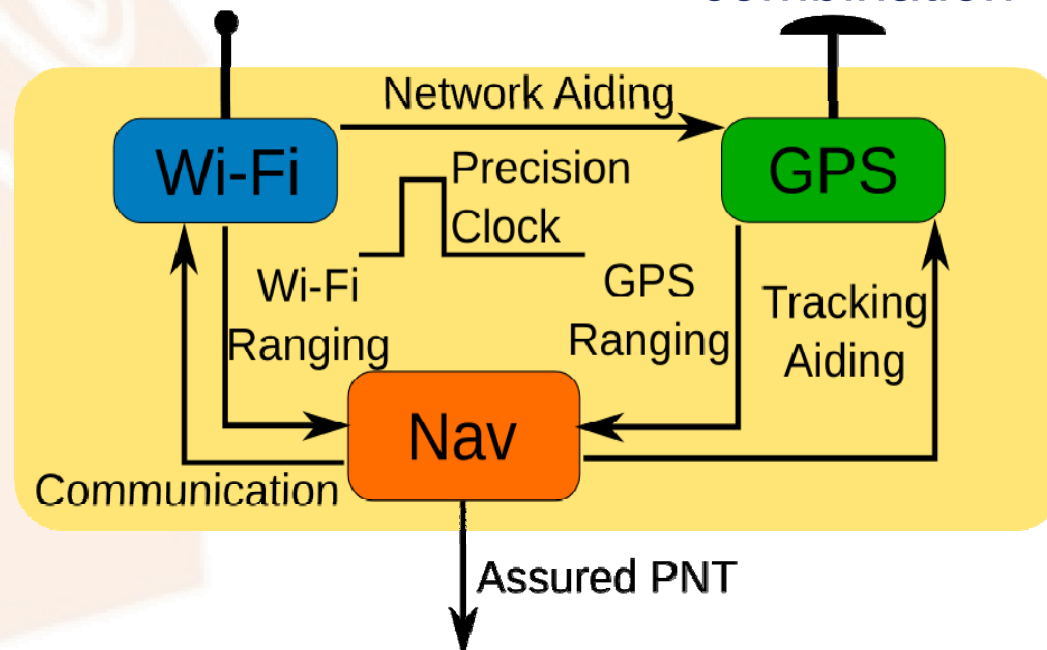


- Base Station
  - Semi-permanent, surveyed
  - Authentication/GPS servers
- Mobile Access Point (MAP)
  - Squad leader, vehicle, temporary structure
  - Wi-Fi/GPS module
  - Quality Clock
- Stations (STA)
  - Soldiers/tactical equipment
  - Wi-Fi/GPS module

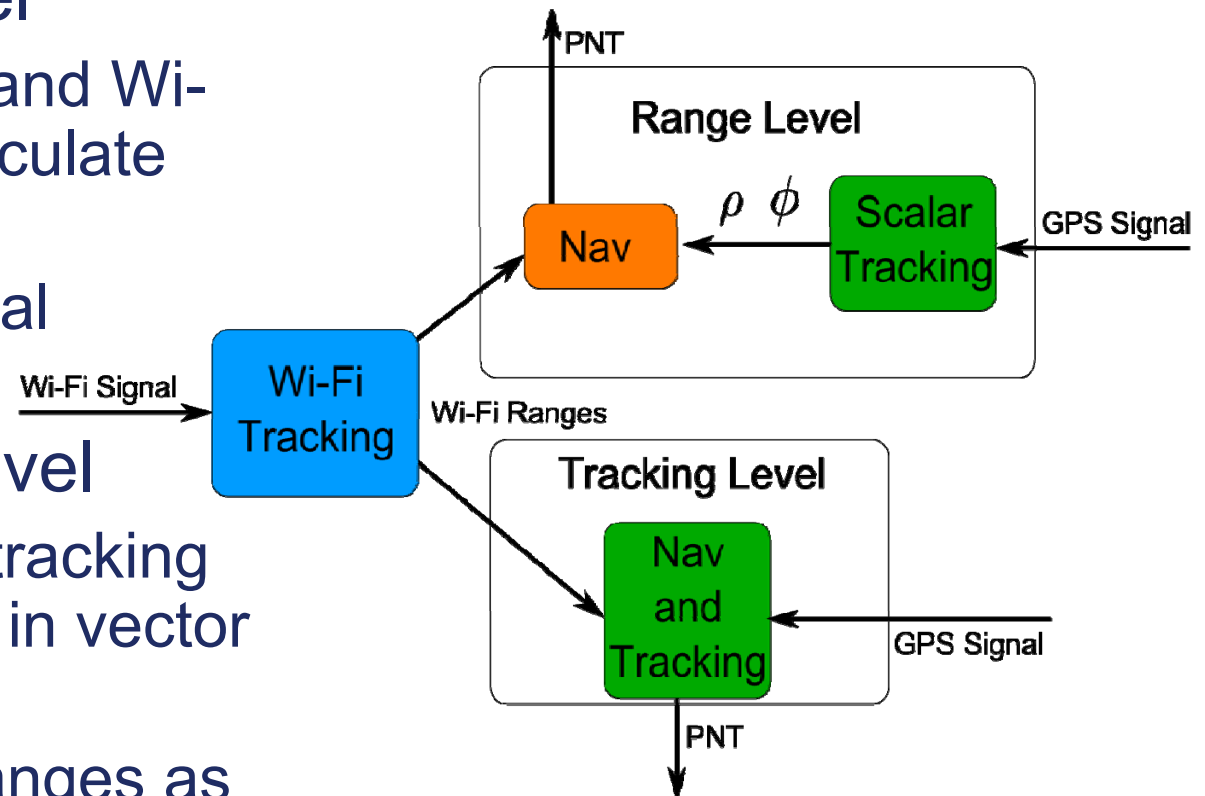


# Wi-Fi/GPS Architecture

- Phase II commercial hardware approach (S1)
  - Wi-Fi driver modification
  - Wi-Fi/GPS range level combination
- Phase II custom hardware approach (S2)
  - FPGA Wi-Fi implementation
  - Wi-Fi/GPS tracking level combination



- S1 - Range Level
  - Combine GPS and Wi-Fi ranges to calculate PNT
  - Uses commercial receiver
- S2 - Tracking Level
  - Combine GPS tracking and positioning in vector formulation
  - Include Wi-Fi ranges as additional measurement to improve PNT and GPS tracking

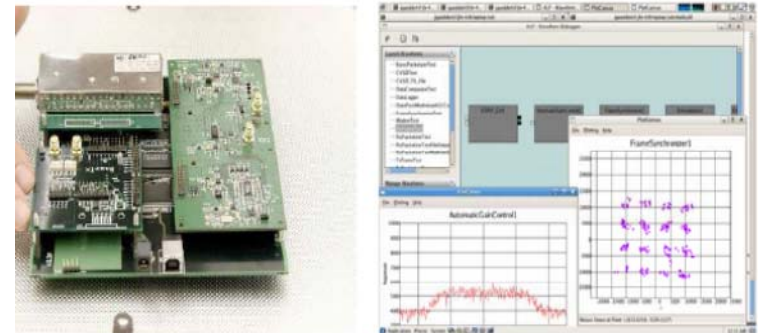


# S1 - ToF Variability MAC Driver Conclusions

- Using instrumented Wi-Fi MAC driver by modifying Ath9k drivers, the average ranging error is **25%** when computing distances from 50 ft to 250 ft.
- This lower bound error is achieved by averaging a total 10 different runs, each with 100,000 ToF samples
- The benefits of this method is the ability to use standard commercial Wi-Fi hardware
- Possible enhancement to reduce ToF variability is measurement through FPGA and Wi-Fi transceiver hardware monitoring
- Improve results using CSAC (Chip-scale atomic clock) precision timestamps on data and ack packets to compute precise two-way time of flight

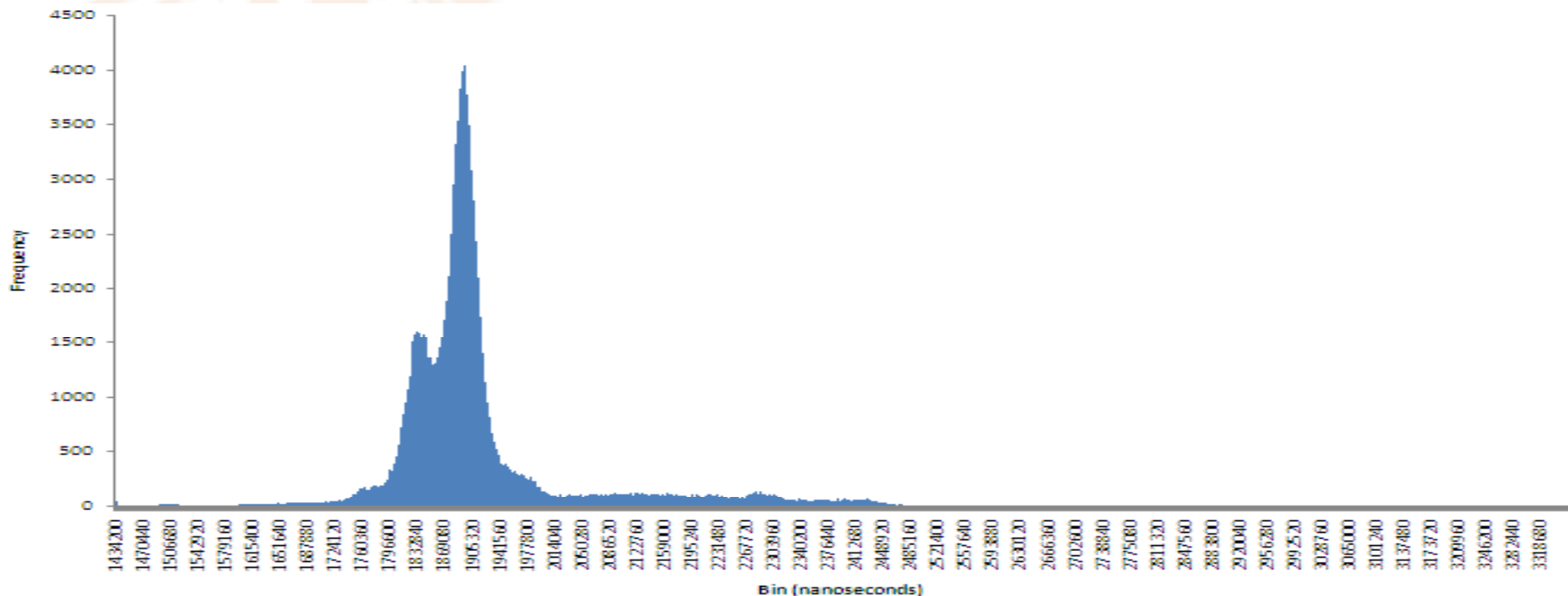
# S2 - ToF Variability Study w/ GNU Radio/USRP

- Improve time-stamping precision per message leveraging the SDR FPGA
- Easily adaptable to alternate spectrum
- Integrate multi-path rejection using per-packet time-of-arrival monitoring
- Integrate navigation & routing in the SDR
- Develop a network publish and subscribe message passing capability
  - For example multicast message sharing
- Use network connectivity to aid GPS receiver initialization
- Integrate Wi-Fi ranges into software GPS receiver to aid PNT solution formulation and increase tracking performance



# S2 - USRP1 Delay Conclusions

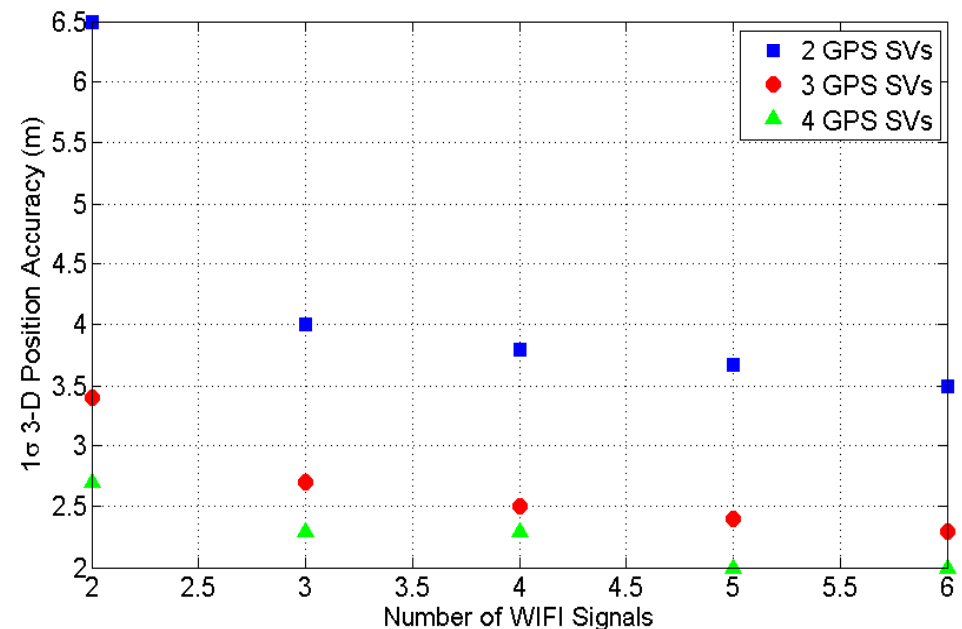
- Multiple packet reception, for two USRP1's in a lab environment
  - 20 feet apart and 0 foot apart
- Delays measured at the USB port, histogram with bin size 60 ns
- Measured over 1 million packet transmissions → error is 10.9 m
- Acquired two USRP2 with large FGPA space, to implement timestamping and TOF measurement in FPGAs



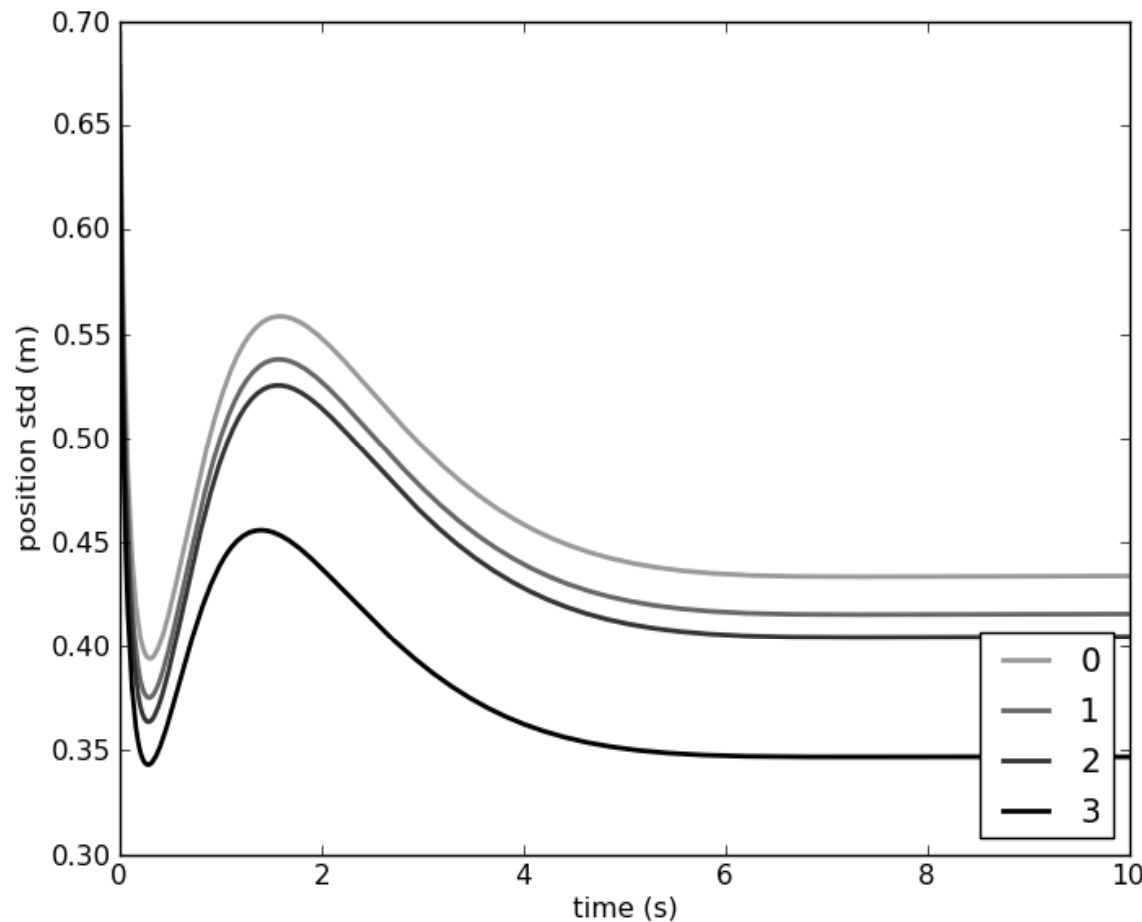


# S1 Range Level Performance

- Expected performance shown from simulation
  - GPS  $1\sigma$  error of 1 m
  - Wi-Fi  $1\sigma$  error of 5 m
  - Note as more GPS satellites are available, the accuracy depends less on the number of Wi-Fi signals
- GPS Simulator simulated GPS and Wi-Fi range errors
  - Simulator will be modified in Phase 2 to integrate the signals



# S2 Simulated Performance



**Positioning accuracy increases with more Wi-Fi nodes**

- Plot shows number of Wi-Fi nodes and expected variance
- Improves positioning and GPS tracking
- Benefit from additional measurements and improved geometry

- Real-time implementation
  - GPS software receiver with additional range measurements
  - Modified Wi-Fi driver testbed
  - Custom Wi-Fi radio system
- Error and benefit analysis for both proposed systems
- Demonstration of integrity with both data and measurement errors
- Extend to additional ranging sources
  - Signals of opportunity