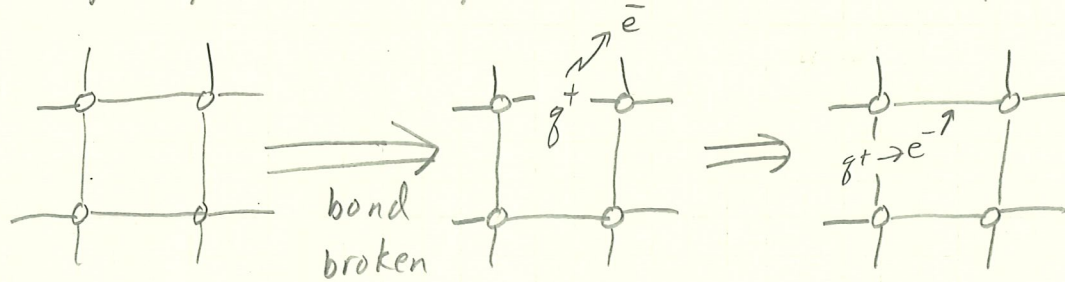


$n \equiv$ density of conduction (or free) electrons

$$[n] = \bar{e}/\text{cm}^3$$

For intrinsic Si: $n_i = n$

For single crystal (monocrystalline) Si: 4 covalently bonded atoms



Energy $\geq E_g$ results in the creation of an electron-hole pair

$\rightarrow$ electrons can move anywhere

$\rightarrow$ holes can only move about the crystal lattice

Electrons and holes are charge carriers

$\downarrow$
 $-q$

$\downarrow$
 $+q$

$$\Rightarrow q = 1.62 \times 10^{-19} \text{ C}$$

$p \equiv$ hole density, $[p] = \text{holes}/\text{cm}^3$

For intrinsic Si: $n_i = n = p$

$n_i^2 = pn \rightarrow$ whenever there is thermal equilibrium w/o external stimulus (voltage, current, light)

Electrical resistivity $\equiv \rho = 1/\sigma$, $\sigma \equiv$ conductivity

a. Drift Currents

charged particles move (drift) in response to an applied

→ results in a drift current, j electric field

$$j = Qv, [j] = A/cm^2$$

$$Q \equiv \text{charge density}, [Q] = C/cm^3$$

v = charge velocity in the electric field

↳ also called "carrier drift velocity"

$$[v] = cm/s$$

positive charges move in direction of the E field

negative charges move in opposite direction of the E field

For low electric fields: $v \propto E$ of interest to this class

$$\therefore \vec{v}_n = -\mu_n \vec{E}$$

$$\vec{v}_p = \mu_p \vec{E}$$

where $\vec{v}_n$ = velocity of electrons

$\vec{v}_p$ = velocity of holes

μ_n = electron mobility, $1350 \text{ cm}^2/V$ for intrinsic Si

μ_p = hole mobility, $500 \text{ cm}^2/V$ for intrinsic Si

Notice $\mu_n > \mu_p$: e^- 's can move freely through crystal while holes can only move about the crystal through the covalent bond structure

Electron and hole drift current densities, j_n^{drift} and j_p^{drift}
 $[j_n^{drift}, j_p^{drift}] = A/cm^2$

1-D vectorless equation versions:

$$j_n^{drift} = Q_n v_n = (-q n)(-\mu_n E) = q n \mu_n E$$

$$j_p^{drift} = Q_p v_p = (+q p)(+\mu_p E) = q p \mu_p E$$

Total drift current density $\equiv j_T^{drift}$

$$j_T^{drift} = j_n^{drift} + j_p^{drift} = q(n\mu_n + p\mu_p)E = \sigma E$$

σ = electrical conductivity = $q(n\mu_n + p\mu_p)$, $[\sigma] = (\Omega \cdot cm)^{-1}$

$\rho = 1/\sigma \equiv$ resistivity

Note: $\rho = \frac{E}{j_T^{drift}} ; \Omega \cdot cm = \frac{V/cm}{A/cm^2}$



$$R = \frac{V}{I} \rightarrow \text{Ohm's law}$$

3. Doping

Doping is the process of adding impurities to the intrinsic semiconductor material

Donor Impurities - one extra e^- in outer shell: donate e^- 's

Acceptor Impurities - one less e^- in outer shell: donate holes

Si: a Column IV element: 4 valence e^- 's in outer shell

1. Class II materials (such as P, As, Sb) have 5 valence electrons in outer shell $\rightarrow$ Donor Materials

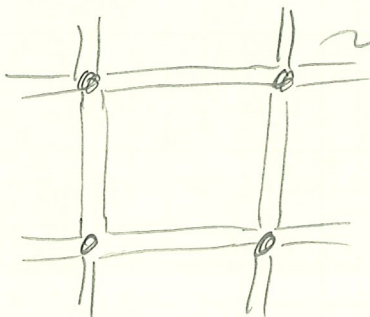
Class III materials (such as B, Al) have 3 valence electrons in outer shell $\rightarrow$ Acceptor Materials

$\rightarrow$ With a donor impurity $\rightarrow$ it requires very little thermal energy for the donor atom to give up its extra e^- for conduction.

* Results in a fixed $+q$ charge which stays fixed in the crystal lattice

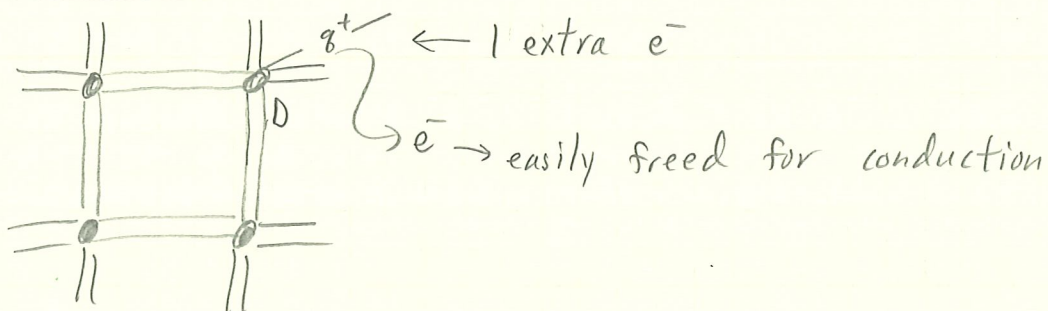
$\rightarrow$ With an acceptor impurity $\rightarrow$ it is easy for a nearby e^- to move into this vacancy, creating another vacancy (hole) in the bond structure. This hole can move through the crystal lattice. When an e^- moves out and the hole moves to that atom, it has a $+q$ charge. Each acceptor atom that accepts an e^- has a $-q$ immobile charge in the crystal lattice.

Intrinsic Si

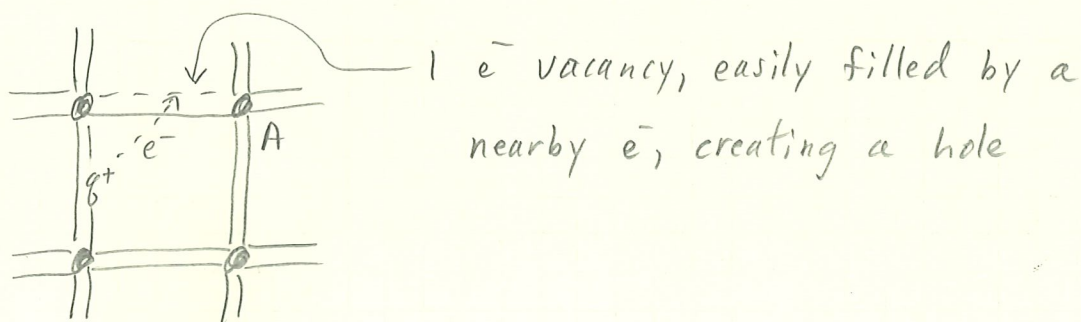


each Si atom has $4e^-$ in outer shell and forms 4 covalent bonds to fill outer e^- shell.

Donor atom in Si



Acceptor atom in Si



Due to doping impurities : if $n > p$: material is called n-type
 if $p > n$: material is called p-type

The carrier with the larger population is called the "majority carrier"

The " " " smaller " " " " "minority carrier"

N_D = donor impurity concentration (atoms/cm³)

N_A = acceptor " " (atoms/cm³)

Note : the semiconductor material is still charge neutral

$$\therefore q(N_D + p - N_A - n) = 0$$

Also : $pn = n_i^2$ still

$$\sigma \cong q\mu_n n \cong q\mu_n (N_D - N_A) \text{ for n-type material}$$

$$\sigma \cong q\mu_p p \cong q\mu_p (N_A - N_D) \text{ for p-type material}$$

2. Nonuniform Doping

→ results in gradients in the e^- and hole concentrations

∴ resulting in diffusion currents

D_n = electron diffusivity, cm^2/s

D_p = hole diffusivity, cm^2/s

Einstein's relationship: $\frac{D_n}{\mu_n} = \frac{kT}{q} = \frac{D_p}{\mu_p}$

$\frac{kT}{q} = V_T \equiv$ thermal voltage

$V_T \approx 25\text{mV}$ at room temperature

Diffusion current density: j_p^{diff} and j_n^{diff}

$$j_p^{\text{diff}} = (+q)D_p\left(-\frac{\partial p}{\partial x}\right) = -qD_p\frac{\partial p}{\partial x} \quad (\text{A}/\text{cm}^2)$$

$$j_n^{\text{diff}} = (-q)D_n\left(-\frac{\partial n}{\partial x}\right) = +qD_n\frac{\partial n}{\partial x} \quad (\text{A}/\text{cm}^2)$$

3. Total Current = drift current + diffusion current

Total electron current density = j_n^T

Total hole current density = j_p^T

$$j_n^T = q\mu_n n E + qD_n \frac{\partial n}{\partial x} = q\mu_n n \left(E + V_T \frac{1}{n} \frac{\partial n}{\partial x}\right)$$

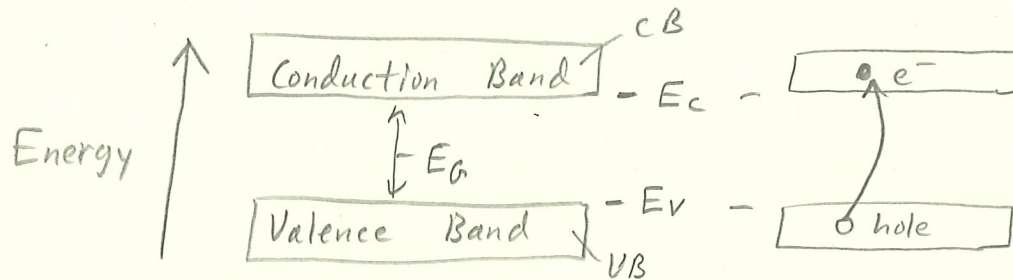
$$j_p^T = q\mu_p p E - qD_p \frac{\partial p}{\partial x} = q\mu_p p \left(E - V_T \frac{1}{p} \frac{\partial p}{\partial x}\right)$$

3. Energy Band Model for a semiconductor

Conduction Band: E_c = lowest energy level in conduction band

Valence Band: E_v = highest energy level in valence band

Energy Bandgap: $E_g = E_c - E_v$

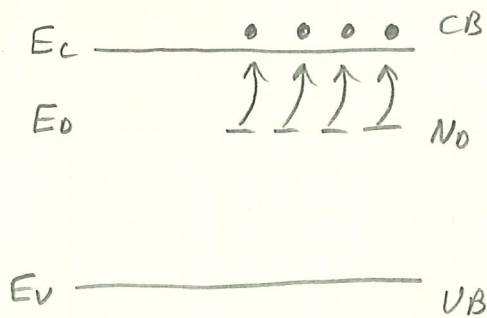


An electron-hole pair is created when an e^- moves from the valence band to the conduction band

→ for example, due to thermal energy

a. For n-type semiconductor

E_d = donor energy level → near conduction band edge

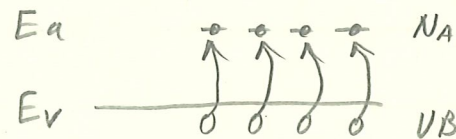


E_d is so close to E_c that almost all e^- 's at E_d have moved to CB and are available for conduction

b. For p-type semiconductors

E_a = acceptor energy level $\rightarrow$ near valence band edge

E_c _____ CB



E_v is so close to E_a that almost all acceptor sites are filled, leaving holes in the valence band for conduction.

c. Compensated Semiconductors : both donor and acceptor impurities

$\rightarrow e^-$'s seek the lowest energy state, and fill all available acceptor sites.

$\rightarrow$ remaining free e^- population $= n = N_D - N_A$

