



# Research on the Reliability of Interconnected Solder Joints of Copper Pillars under Random Vibration

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## Abstract

In this paper, the reliability of copper pillar micro-bump under random vibration is investigated. Three kinds of copper pillar solder joints with different morphologies were obtained by changing the hot press bonding process, and the random vibration fatigue simulation of flip-flop interconnect solder joints was carried out by using Ansys to obtain the stress–strain distribution law of the solder joints and predict the vibration fatigue life of the solder joints. It is found that the outermost solder joints of flip-flop bonding are most likely to fail; the fatigue life of copper pillar solder joints is predicted based on the three interval method, the Miner linear cumulative damage criterion and the high cycle fatigue formula; reliability experiments are conducted, and it is found that the drum solder joints are most prone to cracking, followed by hourglass and columnar shapes and that all cracks are caused by the substrate side of copper pillar. Cracks are sprouted from the contact surface between the copper pillar and solder on the substrate side and expand internally in the intermetallic compound (IMC) layer, while the presence of voids aggravates the generation of cracks.

**Keywords** Copper pillar bump · Flip chip · Random vibration · Vibration fatigue life

## 1 Introduction

With the development of three-dimensional integration technology, the application of electronic devices has become more and more extensive, and the environment in which it works has become diverse and harsh, such as in the automotive, aerospace, medical and other industries, to improve the effectiveness of the package, which poses a new challenge to the reliability of microelectronic packaging [1, 17, 20]. In some cases, vibration can be a major factor in the failure of electronic devices [21]. Under the action of vibration, the

electronic components will undergo dynamic bending deformation, thus the solder joints between the substrate and the chip are subjected to repeated stress–strain, causing elastic and plastic deformation of the solder joints, which ultimately leads to the formation of cracks. A crack will increase the electrical resistance at the bonding interface until a break occurs and the device will become non-functional. The failure of solder joints subjected to shock and vibration is the main failure mechanism in electronic products, and the vibration reliability of solder joints has always been a concern in the microelectronics industry [15].

Vibration reliability of solder joints has already been investigated by many researchers. Steinberg [19] presented extensive research and methodology on the analysis and reliability of electronic equipment under vibration and drop/shock loads. Wong et al. [22] explained the failure to be due to the simultaneous axial and shear deformation and coupling moments experienced at the solder interconnections. Due to the development of auto-driving cars, vibration reliability is getting more and more attention, and there are many researches on the development of new methods and techniques. Yu et al. [24] developed an evaluation method based on vibration testing and finite element analysis (FEA) for predicting the fatigue life of

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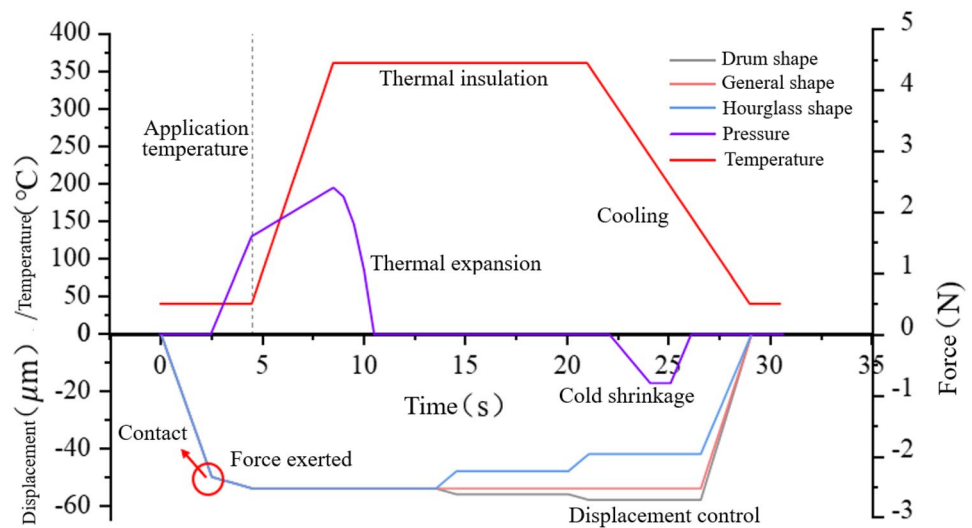
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**Fig. 2** Hot pressing process curve

and lifting height, and the three morphologies obtained are shown in Fig. 3. Test vehicle shown in Fig. 4 consisted of a PCB, substrate, chip, and solder balls.

## 2.2 Finite Element Analysis

To study the stress–strain distribution of the solder joints under the action of random vibration, finite element software is used to carry out random vibration simulation on the flip chip and PCB, and the overall finite element model of the random vibration device is shown in Fig. 5. In this paper, to simplify the model and save calculation time, the simulation model only has a flip chip. There are 281050 meshes and 1387432 nodes in total. The PCB is constrained by four positioning holes around it. The material used for the chip is Si. The solder joint material is Sn3.5Ag. Substrate and PCB materials are FR-4. The specific properties parameters of each material are shown in Table 1. The parameters are taken from the room temperature. All the material properties are linear elastic models, and all materials are considered isotropic.

The modal analysis is first performed through the Modal module of Ansys software. Then in the Random Vibration module in Ansys, the PSD function is added to apply random vibration load to the flip chip, and the PSD load is added at the four positioning holes of the constraints with the

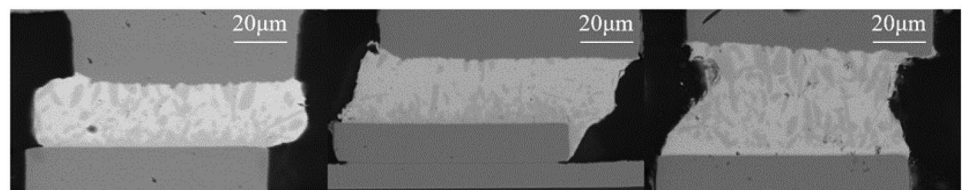
direction perpendicular to the chip. The minimum frequency of the random vibration is 50 Hz, the maximum frequency is 2000 Hz, the maximum power spectral density is  $0.3G^2/Hz$ , the total root-mean-square (RMS) value of the acceleration is  $207.1 m/s^2$ , and the gravitational acceleration is  $9.8 m/s^2$ . Specific PSD is shown in Fig. 6.

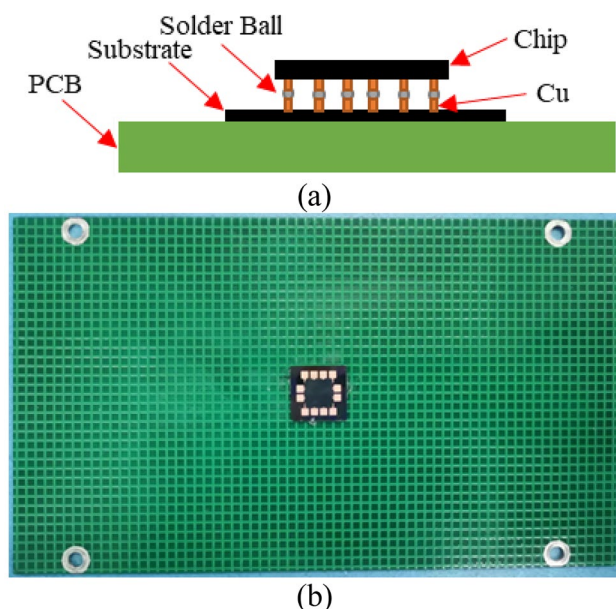
The fatigue life of the copper pillar solder joints was predicted using the three-interval method, the linear cumulation damage criterion, and the high cycle fatigue formula. The three-interval method is a method proposed by Steinberg [19] by collating and rearranging a large amount of experimental data. The three-interval method assumes that the instantaneous acceleration or strain at a point on the device during a random load to which the device is subjected is a time-dependent random process, and that this process obeys a normal distribution. The three-interval method is shown in Eqs. (1)–(5):

$$n_1 = N_0^+ T_s (3600 sec/hr) (0.6831) \quad (1)$$

$$n_2 = N_0^+ T_s (3600 sec/hr) (0.271) \quad (2)$$

$$n_3 = N_0^+ T_s (3600 sec/hr) (0.0433) \quad (3)$$

**Fig. 3** Three different morphological samples

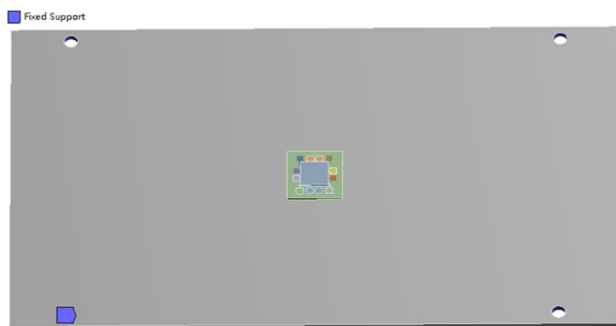


**Fig. 4** Test vehicle **a** schematic diagram of z-axis direction, **b** actual picture

$$N_0^+ = \frac{1}{2\pi} \left[ \frac{\frac{\pi}{2} P_1 f_1 Q_1}{\Omega_i^2} + \frac{\frac{\pi}{2} P_2 f_2 Q_2}{\Omega_i^2} + \dots \right]^{\frac{1}{2}} \quad (4)$$

$$Q_i = \sqrt{f_i} \quad (5)$$

For a mildly damper system with multiple peaks, each peak can be analogized to a system with a single degree of freedom to obtain Eq. (4), and according to a study by Hongfang Wang of Shanghai Jiao Tong University, the transfer rate of each peak can be calculated based on Eq. (5). In Eqs. (1)–(4),  $n_i$  is the cumulative number of cycles under  $i\sigma$  strain level ( $i=1,2,3$ ),  $T_s$  is the random vibration time,  $N_0^+$  is the average number of passes through the axes with a positive slope per unit time in a graph with time as the horizontal axis and acceleration or strain as the vertical axis,  $P$  is the power spectral



**Fig. 5** Random vibration modeling and constraint

**Table 1** Basic material properties [9, 12]

| Material                     | Cu   | Sn3.5Ag | Si   | FR-4                    |
|------------------------------|------|---------|------|-------------------------|
| Poisson's ratio              | 0.34 | 0.35    | 0.28 | 0.39(XZ&YZ<br>0.11(XY)) |
| Density (kg/m <sup>3</sup> ) | 8960 | 6540    | 2329 | 1910                    |
| modulus of elasticity (GPa)  | 130  | 30.52   | 170  | 26.37(X,Y)11.8(Z)       |

density at peak frequency,  $f_i$  is the first ( $i=1,2,3$ ) natural frequency of a PCB assembly,  $Q$  is the transmittance,  $\Omega$  is the angular frequency.

The Miner linear cumulative damage criterion:

$$D_v = \frac{n_1}{N_1} + \frac{n_2}{N_2} + \frac{n_3}{N_3} \quad (6)$$

where  $D_v$  is the fatigue damage factor, often taken as 0.7,  $N_i$  is the number of fatigue cycles under  $i\sigma$ .

The high cycle fatigue formula:

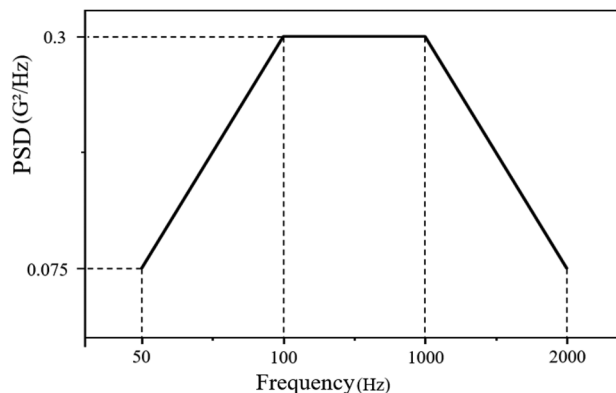
$$\varepsilon_i = 3.5 \frac{\sigma_u}{2E} N_i^{-0.12} \quad (7)$$

where  $\varepsilon_i$  is the maximum equivalent elastic strain at  $i\sigma$ ,  $\sigma_u$  is the tensile strength of the material, the tensile strength of the solder joint material Sn3.5Ag is taken as 25 MPa at room temperature [11] and  $E$  is the modulus of elasticity of the material.

The equivalent strain amplitude in the strain singularity region of the solder joint is averaged through Eqs. (8) and (9):

$$\varepsilon = \frac{\sum \varepsilon_i V_i}{\sum V_i} \quad (8)$$

$$\varepsilon = \frac{\sqrt{2}}{3} \sqrt{(\varepsilon_x - \varepsilon_y)^2 + (\varepsilon_y - \varepsilon_z)^2 + (\varepsilon_z - \varepsilon_x)^2 + \frac{3}{2}(\gamma_{xy}^2 + \gamma_{yz}^2 + \gamma_{zx}^2)} \quad (9)$$



**Fig. 6** PSD curves for random vibration simulation

**Table 2** Random vibration test curve power spectral density

| Test frequency (Hz) | PSD<br>((m/s <sup>2</sup> ) <sup>2</sup> /Hz) |
|---------------------|---|
| 50                  | 7.5   |
| 100                 | 30  |
| 1000                | 30  |
| 2000                | 7.5   |

Equation (8) where  $\varepsilon$  is the equivalent strain amplitude,  $\varepsilon_i$  is the strain amplitude of a single mesh, and  $V_i$  is the mesh volume. In Eq. (9)  $\varepsilon_i (i = x, y, z)$ , and  $\gamma_{ij} (i, j = x, y, \text{ and } i \neq j)$  are the positive and shear strains within each mesh.

### 2.3 Test Conditions and Analysis

The random vibration test was performed using an electrodynamic shaker with the test conditions shown in Table 2, the acceleration RMS value is 20.71 g. After the random vibration test, the sample will be sealed with epoxy resin, and grinding samples with 80, 240, 800, 1500 purpose sandpaper. The samples were polished with 0.5  $\mu\text{m}$  diamond polishing solution. Then the microstructure was observed by scanning electron microscopy (SEM). Finally, the composition of the interfacial reaction products was analyzed using energy dispersive X-ray (EDX) analysis.

## 3 Results and Discussion

### 3.1 Stress and Strain Distribution and Fatigue Life Analysis During Random Vibration

The first 12 orders of natural frequency of modal analysis are shown in Table 3, since the highest frequency used for

**Table 3** First twelfth order modal analysis of copper pillar interconnection solder joints on the PCB

| Ordinal number | Natural frequency (Hz) |
|----------------|------------------------|
| 1              | 428.75                 |
| 2              | 775.83                 |
| 3              | 1032                   |
| 4              | 1179.1                 |
| 5              | 1485.2                 |
| 6              | 1762.2                 |
| 7              | 1843.1                 |
| 8              | 2465                   |
| 9              | 2737.7                 |
| 10             | 2899.8                 |
| 11             | 3242                   |
| 12             | 3410.1                 |

the random vibration experiment is 2000 Hz, the modal frequency viewed is  $1.5f_{max} = 3000\text{Hz}$ .

Figures 7 and 8 show the  $1\sigma$  stress–strain distribution of the flip-flop copper pillar solder joints, and it can be seen that the chip under random vibration is subjected to the outermost solder joints with the largest statistical value of stress–strain, which is due to the constraints on the four corners of the PCB, resulting in the deformation of the PCB in the random vibration, and in this deformation, the center of the chip's solder joints do not vary much with respect to the PCB's position, and the surrounding solder joints vary more with regard to the PCB's position, and so the outermost chip's solder joints have a large stress–strain under random vibration. The enlarged view of the solder joint shows that the maximum stress–strain of the solder joint occurs on the side close to the PCB, and the stress–strain in the middle of the solder joint is relatively small, so that the crack of the solder joint occurs at this position at the very beginning, and the maximum value of the  $1\sigma$  stress is 3.4889MPa and the value of the strain in the direction of the Z-axis under the  $1\sigma$  is 0.00016931mm/mm. In general, the first failure location in the chip under random vibration is the outermost solder joints, and the first crack is on the side of the copper pillar solder joints near the PCB.

In this paper, the three-interval method is used to predict the random vibration fatigue life of the copper pillar flip-flop solder joints, and the equivalent strain of the solder joints from  $1\sigma \sim 3\sigma$  is obtained through simulation. The vibration fatigue life of the copper pillar solder joints can be obtained as 281 h through the calculation of Eqs. (1)–(9).

### 3.2 Influence of Solder Joint Structure on the Vibration Fatigue Life of Solder Joints

#### 3.2.1 Effect of Solder Joint Height on Fatigue Life of Flip Chip

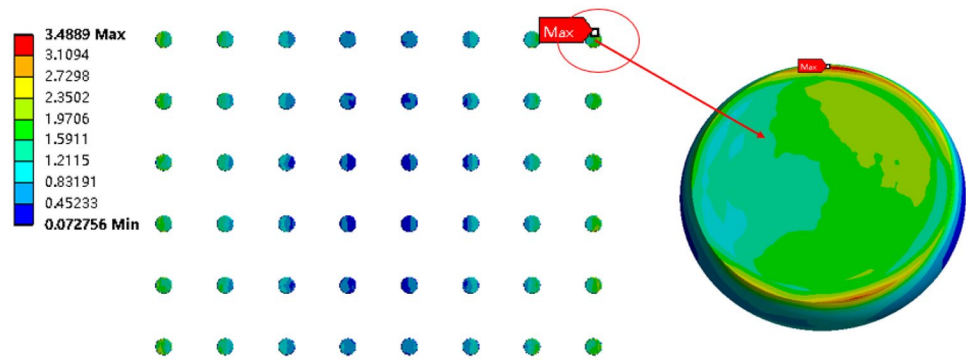
First, the volume of the solder joint is fixed at  $1.845\text{E-}4\text{mm}^3$ , the copper column diameter is 0.1 mm, and the height of the solder joint varies from 0.0185 mm to 0.032 mm. Table 4 shows the results obtained according to the three-interval method.

Figure 9 shows the relationship between the vibration fatigue life of the solder joint and the height of the solder joint. When the height of the solder joint is 0.02 mm, the vibration fatigue life is maximum 356.58 h. When it is less than this height, the vibration fatigue life increases with the increase of the height, and when it is higher than this height, the vibration fatigue life also decreases with the increase of the solder joint. when the height is 0.02 mm, the fatigue life is more than two times of other heights.

Figure 10 shows the strain distribution of different solder joint heights, from the figure can be found with the



**Fig. 7** Cloud view of  $1\sigma$  stress distribution in flip-flop solder joints



increase in the height of the solder joint, the location of the maximum equivalent elastic strain from the bottom of the solder joint gradually shifted to the middle of the solder joint, which may lead to inconsistency in the location of the random vibration solder joint failure, that is, hourglass-shaped solder joints vulnerable to failure in the middle of the solder joint. The maximum strain of the solder joint is shifted to the middle of the solder joint probably because the deformation of the PCB under random vibration will pull on the solder joint, and when the PCB bends upward, it will stretch the solder joint, and because the hourglass-type solder joint is relatively thin in the neck, the stress strain here is larger, and it becomes a failure-prone solder joint.

### 3.2.2 Effect of Solder Joint Volume on Fatigue Life of Flip Chip

The fixed solder joint height is 0.023  $\mu\text{m}$ , the copper pillar diameter is 0.1 mm, and the solder joint volume varies from 1.454E-4mm<sup>3</sup> to 2.292E-4mm<sup>3</sup>. Table 5 shows the results obtained according to the three-interval method.

Figure 11 shows the relationship between the fatigue life of the solder joint and the volume of the solder joint, the vibration fatigue life of the solder joints increases and then decreases as the volume of the solder joints increases. When the volume of the solder joint is 2.103E-4mm<sup>3</sup>, the vibration fatigue life is maximum 280.97 h; when the volume of the solder joint is 1.454E-4mm<sup>3</sup>, the vibration fatigue life is

minimum 18.64 h. Therefore, increasing the volume of the solder joint can improve the resistance of the solder joint to vibration to some extent.

### 3.2.3 Effect of Copper Pillar Diameter on Fatigue Life of Flip Chip

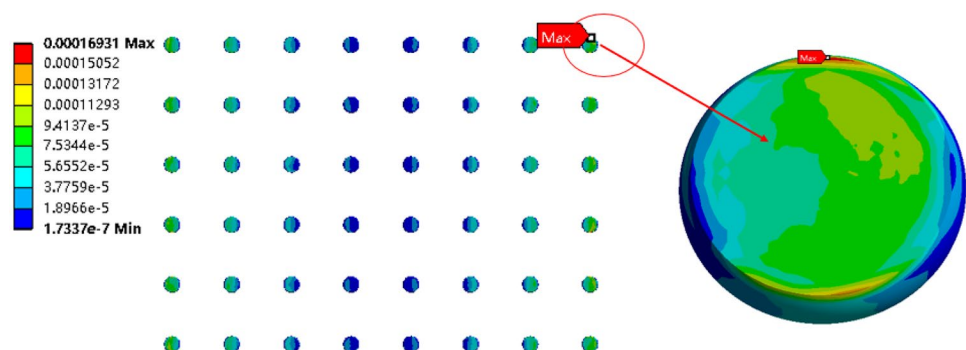
The fixed solder joint volume is 1.845E-4mm<sup>3</sup>, the solder joint height is 0.023 mm, and the copper pillar diameter varies from 0.09–0.11 mm, Table 6 shows the results obtained according to the three-interval method.

Figure 12 shows the relationship between the fatigue life of the solder joint and the diameter of the copper pillar, with the increase of the diameter of the copper pillar, the vibration fatigue life of the solder joint has no obvious law. When the diameter of the solder joint is 0.1 mm, the maximum vibration fatigue life of the solder joint is 182.57 h, and when the diameter of the copper pillar is 0.11 mm, the minimum vibration fatigue life of the solder joint is 32.98 h.

## 3.3 Reliability Test of Different Structure Solder Joints

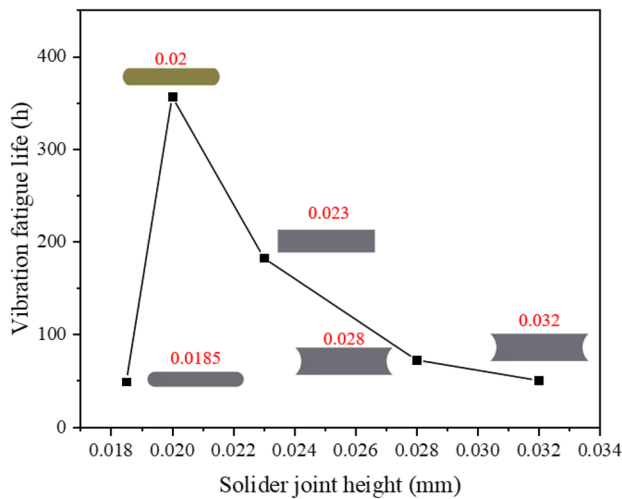
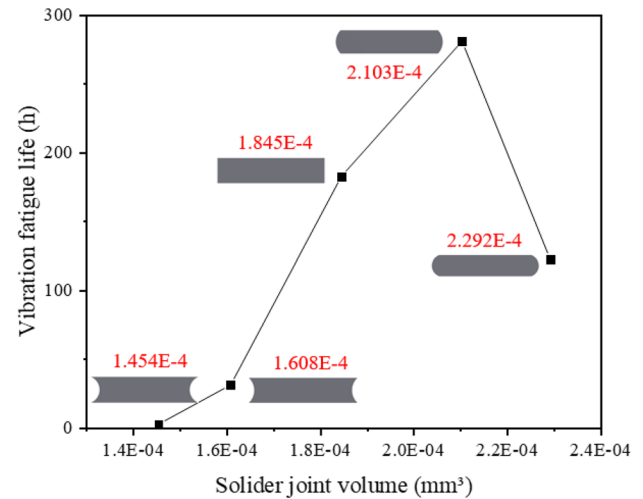
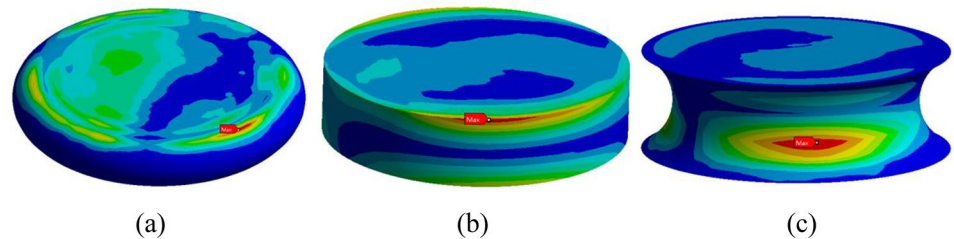
Figure 13 shows the solder joint images of the three shapes of solder joints at random vibration for 4 h, from which neither the column shape nor the hourglass shape produces obvious cracks, whereas the drum shape solder joint can be seen in Fig. 15f that there is already a slight crack produced, the cracks are located at the IMC where the copper pillar on

**Fig. 8** Cloud view of  $1\sigma$  strain distribution in flip-flop solder joints



**Table 4** Relationship between solder joint height variation and vibration fatigue life

| Number                                | 1        | 2        | 3           | 4           | 5        |
|---------------------------------------|----------|----------|-------------|-------------|----------|
| Pad Diameter(mm)                      | 0.1      | 0.1      | 0.1         | 0.1         | 0.1      |
| Solder Joint volume(mm <sup>3</sup> ) | 1.845E-4 | 1.845E-4 | 1.845E-4    | 1.845E-4    | 1.845E-4 |
| Solder Joint height(mm)               | 0.0185   | 0.02     | 0.023       | 0.028       | 0.032    |
| $D_v$                                 | 0.0143   | 1.96E-3  | 3.38<br>E-3 | 9.67<br>E-3 | 0.0139   |
| Vibration fatigue life(h)             | 48.93    | 356.57   | 182.57      | 72.38       | 50.19    |

**Fig. 9** Fatigue life of a solder joint as a function of solder joint height**Fig. 11** Fatigue life of a solder joint as a function of solder joint volume**Fig. 10** Strain distribution at different solder joint heights: **a** 0.0185 mm; **b** 0.023 mm; **c** 0.032 mm**Table 5** Relationship between solder joint volume variation and vibration fatigue life

| Number                                | 1        | 2        | 3        | 4        | 5        |
|---------------------------------------|----------|----------|----------|----------|----------|
| Pad Diameter(mm)                      | 0.1      | 0.1      | 0.1      | 0.1      | 0.1      |
| Solder Joint volume(mm <sup>3</sup> ) | 1.454E-4 | 1.608E-4 | 1.845E-4 | 2.103E-4 | 2.292E-4 |
| Solder Joint height(mm)               | 0.023    | 0.023    | 0.023    | 0.023    | 0.023    |
| $D_v$ (h <sup>-1</sup> )              | 0.0376   | 0.0226   | 3.83E-3  | 2.49E-3  | 5.73E-3  |
| Vibration fatigue life(h)             | 18.64    | 31       | 182.57   | 280.97   | 122.05   |

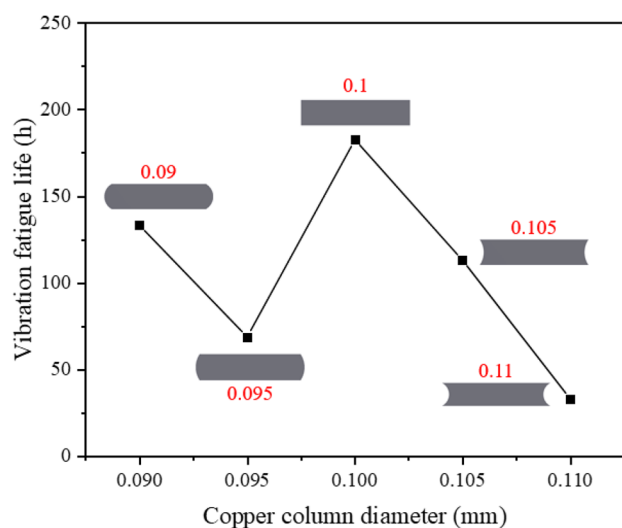
**Table 6** Relationship between copper pillar diameter variation and vibration fatigue life

| Number                                | 1        | 2        | 3        | 4        | 5        |
|---------------------------------------|----------|----------|----------|----------|----------|
| Pad Diameter(mm)                      | 0.09     | 0.095    | 0.1      | 0.105    | 0.11     |
| Solder Joint volume(mm <sup>3</sup> ) | 1.845E-4 | 1.845E-4 | 1.845E-4 | 1.845E-4 | 1.845E-4 |
| Solder Joint height(mm)               | 0.023    | 0.023    | 0.023    | 0.023    | 0.023    |
| $D_v$                                 | 5.26E-3  | 0.0102   | 3.83E-3  | 6.91E-3  | 0.0212   |
| Vibration fatigue life(h)             | 133.15   | 68.67    | 182.57   | 113      | 32.98    |

the substrate side contacts the solder. The chip side solder joints did not produce obvious cracks.

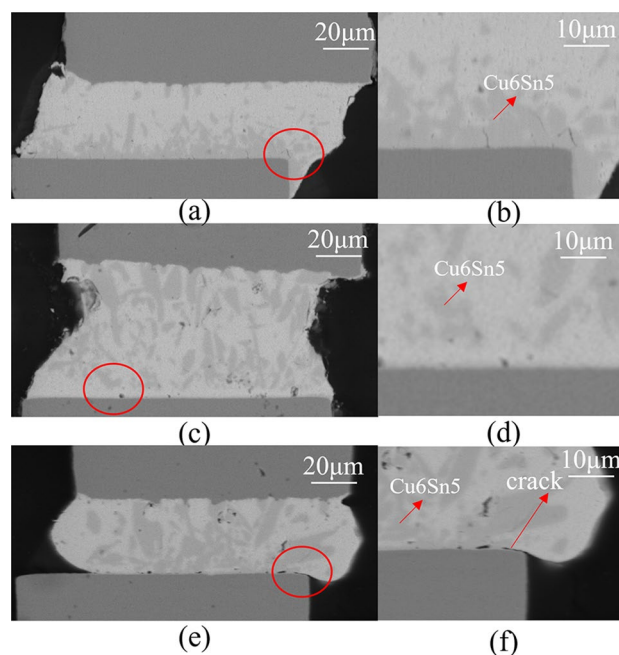
Figure 14 shows the solder joints after 8 h of random vibration, from the figure it can be found that the three kinds of shape of the solder joints have different degrees of cracks, and cracks are generated from the substrate side of the copper pillar in the contact surface of the solder, the chip side is still no cracks, and at the same time from the finite element analysis, the maximum stress and strain of the solder joints appeared in the substrate side of the copper pillar in the contact surface of the solder. The location of crack growth in random vibration verifies the reliability of the simulation. Comparing Fig. 13d with Fig. 14d, it is found that the cracks in the solder joint suddenly increase a lot with 4 h more random vibration because the solder joint in Fig. 14d are filled with IMC and the copper pillar on the side of the substrate have micro holes, so longer cracks are produced during random vibration.

Figure 15a shows the diagram of some solder joints with bad bonding quality, from which it can be found that when there is a hole on the side of the solder joint and the copper pillar of the substrate, cracks are very easy to be generated during the vibration process, especially in the place where IMC is abundant, Fig. 15b shows the graph of IMC less hourglass shaped solder joint, which is found to

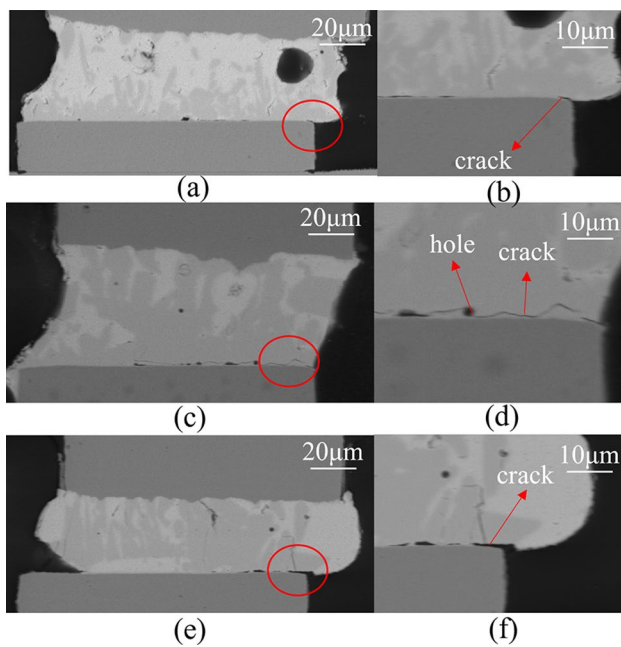
**Fig. 12** Fatigue life of solder joints as a function of copper pillar diameter

have almost no crack generation in the presence of a hole as compared to Fig. 14d, probably due to the absence of IMC at the place where this hole is generated, thus IMC has a great impact on the random vibration reliability of the solder joint and its generation should be avoided as much as possible.

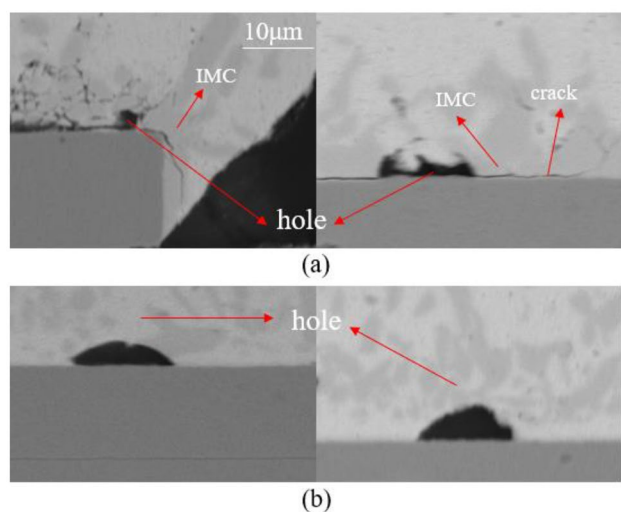
From the above analysis, the cracks of the three different solder joints started to grow at the contact surface between the copper pillar and the solder on the side of the substrate, and the first to crack is the drum joint followed by the hourglass and pillar joints. In the process of random vibration, the PCB board will fluctuate up and down with the vibration will produce tensile and compressive stress and strain on the solder joints, in this kind of alternating stress, the solder joints will produce internal damage, when the damage accumulates to a certain degree, cracks will be produced. On the other hand, during the flip bonding process, IMC is generated inside the solder joint, and the nature of IMC with low temperature brittleness does not match the nature of the solder, resulting in stress concentration at the interface.

**Fig. 13** SEM image of solder joints with 4 h random vibration **a** column overall; **b** column partial; **c** hourglass overall; **d** hourglass partial; **e** drum overall; **f** drum partial





**Fig.14** SEM image of solder joints with 8 h random vibration **a** column overall; **b** column partial; **c** hourglass overall; **d** hourglass partial; **e** drum overall; **f** drum partial



**Fig.15** SEM image of solder joints with poor bonding quality **a** with voids and cracks; **b** with voids and no cracks

Under these two factors, the solder joint cracks at the IMC layer and expands until it fails.

## 4 Conclusion

- (1) In the random vibration process is in the outermost layer of the flip chip solder joints subject to the greatest stress strain, is the weakest solder joints in the entire chip (prone to failure).

- (2) Control the volume of the solder joint and copper pillar diameter is constant, when the height of the solder joint has 0.0185 mm-0.032 mm change, the fatigue life of the solder joint is maximum when the height of the joint is 0.02 mm, and as the height of the joint increases, the failure position of the joint gradually moves to the middle of the joint; control the height of the solder joint and copper pillar diameter is constant, when the volume of the solder joint from 1.454E-4mm<sup>3</sup>-2.292E-4mm<sup>3</sup> change, fatigue life of solder joints increases and then decreases; controlling the volume of the solder joint and the height of the solder joint constant, when the diameter of the copper column changes from 0.09 mm-0.11 mm, there is no clear pattern in the fatigue life of solder joints.
- (3) Under the effect of random vibration, the cracks of solder joints are located at the IMC of the contact surface between the copper pillar and the solder joints on the side of the substrate, and the solder joints with the first cracks are located at the periphery of the chip and are very prone to cracks when there are holes in the IMC layer. For all three shapes, the drum shape is the most prone to cracking, followed by the hourglass and column shapes.

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**Data Availability** The datasets generated during and/or analyzed during the current study are available from the corresponding author on reasonable request.

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