Electronic equalizations for optical fiber dispersion compensation

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Abstract. This paper presents complete models for various fiber dispersions and their mitigations using electronic equalizers. A novel constant-modulus-adaptive (CMA) blind equalization technique is proposed for fiber dispersion compensation. Simulations demonstrated effective compensation means for chromatic and polarization mode dispersions using least-mean-square (LMS) and CMA blind equation techniques. Also proposed is the adaptive fiber transceiver architecture with eye-open-detect circuits that can be used to provide the feedback controls for adaptive thresholds and high-speed analog equalizers. © 2007 Society of Photo-Optical Instrumentation Engineers. [DOI: 10.1117/1.2715955]

Subject terms: fiber dispersion; chromatic dispersion; polarization mode dispersion; electronic equalization; constant-modulus-adaptive; blind equalization.

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1 Introduction

Since the early 1980s, the transmission speed of the optical networks has doubled almost every two years. When 10-Gigabits-per-second (Gb/s) optical networks were debated in the mid-1990s, many predicted that the 10-Gb/s-format would never become reality due to various obstacles. Similar debates now exist about the higher data rate at 40-Gb/s and the daring new concepts such as the agile optical network. The agile optical network is a reconfigurable optical network and is more resilient and more efficient compared to the traditional fixed point-point networks. However, in order to dynamically route an optical channel, an agile optical network requires dynamical dispersion management and adaptive dispersion compensation. One of the main concerns for high-data-rate agile optical networks is the dispersion effect in the optical fibers.

Modal, chromatic, and polarization mode dispersions are the major sources of transmission impairments in high-data-rate fiber communications. Without proper compensation, the performance of the fiber communication systems will be severely limited. The available dispersion compensation fiber is static in nature and therefore does not support agile optical networks. Other optical solutions are only capable of compensating one form of the dispersions with very high cost, high insertion loss, and slow tuning speed if they are tunable at all. The electronic equalizer can be dynamically tuned and has much smaller form factor and much lower cost. An electronic equalizer can be integrated into a single chip using the high-speed silicon germanium (SiGe), indium phosphorus, or CMOS technologies. Further cost reduction is possible if the electronic equalizer and other receiver circuitry such as clock data recovery are integrated on the same die.

Blind channel identification and equalization approaches have received increasing attention in recent years because of their applications in wire line and wireless communications. Traditionally, a training sequence is transmitted during the acquisition mode to enable the receiver to program an equalizer or estimate the channel. For a time-varying dispersive channel, the training sequences may have to be transmitted periodically. The drawback of conventional equalizer algorithms lies on the fact that they all need the assistance of a training sequence. When the eye pattern of the channel output is initially closed, the conventional equalizer requires reference signals for channel estimation. On the other hand, blind equalization provides a reference-free equalization algorithm, which meets the current fiber communication transmission standard. Blind equalization is thus critical for agile optical networks with a time-varying channel environment.

Fiber dispersion includes both static chromatic dispersion (CD) and time-varying polarization mode dispersion (PMD) effects. In fiber networks with PMD, the channel dispersion characteristics constantly vary due to effects such as temperature variation and fiber stress and vibration. Traditional equalization methods using training patterns are thus not suitable for fiber polarization mode dispersion compensations. The impact of the modal dispersion and the first-order PMD on system performance in fiber networks is very similar to multipath interference in wireless systems, where blind equalization has been a common practice. Therefore, the blind equalization algorithm used in wireless systems can be applied to compensation of the modal dispersion and the first-order PMD. The second-order PMD is a combination of depolarization (DPLZ) and polarization-dependent chromatic dispersion (PCD). The second-order PMD is thus a wavelength-dependent dispersion, which does not have a similar countereffect in wireless communications. We will thus extend the prior art blind equalization techniques to include effects such as wavelength-dependent chromatic dispersion for high-data-rate fiber networks.

An electronic equalizer module is superior considering its cost, size, reliability, flexibility, and speed. A theoretical model of PMD compensation using digital signal processing was presented in Ref. 1 in which analog equalization...
was not discussed. An integrated analog and digital signal processing technique implemented using both SiGe and CMOS technologies was presented in Ref. 2 for compensating dispersion in 10 Gb/s fiber networks. A seven-tap distributed transversal equalizer was implemented in a 0.18-μm SiGe BiCMOS process for 10-Gb/s multimode fiber optic links. Both references were focused on integrated circuit designs without detailed equalization feedback algorithms. A hybrid opto-electronic equalizer optimized jointly using a least-mean-square algorithm was briefly presented in Ref. 4. The algorithm needs a training sequence and thus is not suitable for agile fiber networks. This paper presents adaptive electronic equalization means for the compensation of all forms of fiber dispersions, including modal, chromatic, and polarization mode dispersions. The proposed electronic equalizer employs a novel constant-modulus-adaptive-based blind equalization technique to achieve adaptive dispersion compensation without training sequence. Simulations demonstrate excellent dispersion compensations for various fiber dispersions such as CD and PMD. We will also discuss the adaptive fiber receiver implementations for agile high-speed fiber networks.

The paper will start with a tutorial discussion on various fiber dispersions in Sec. 2. In Secs. 3, fiber channel emulation models with various dispersions will be developed. The proposed adaptive electronic equalization techniques with blind feedback algorithms are presented in Secs. 4 and 5. Finally, fiber dispersion compensations using the proposed electronic equalization approach will be demonstrated in simulation in Sec. 6.

## 2 Dispersion in Optical Fiber

Dispersion limits the bit-rate and transmission distance of fiber networks. Newly developed nonzero dispersion shifted fibers (LEAF and TrueWave) are mainly used in improving power and reducing fiber nonlinear effects. They fail to reduce dispersion in each separate channel, since dispersion is wavelength-dependent and accumulates at different rates. There are three main dispersion effects in optical fibers: (1) the modal dispersion; (2) the chromatic dispersion; and (3) the polarization mode dispersion.

### 2.1 Modal Dispersion

Modal dispersion occurs when light travels in multimode fibers that have core diameters of about 50 to 80 μm. In multimode fibers, each mode travels at a different speed for a given fiber length. The modal dispersion of a multimode fiber limits the signal transmission rate to about 100 Mbs/s over several kilometers. Due to the low cost and ease of connection, the multimode fiber is still the choice for short-reach optical connection. If cost is not a concern, single-mode fibers can be used to eliminate the modal dispersion.

### 2.2 Chromatic Dispersion (CD)

CD occurs in single-mode fibers due to the wavelength dependence of the light velocity. CD is inherent in fiber due to material refractive index and waveguide dispersion. Both the refractive index and group index vary with wavelength. Modern fiber exhibits both normal and anomalous dispersion regimes. For normal dispersion, blue wavelengths travel slower than red wavelengths. Anomalous dispersion reverses this order. An optical pulse is comprised of a range of wavelengths. CD impacts the pulse by retarding one color with respect to the other, causing pulse envelope spread.

Data modulation of a single-wavelength laser causes the modulated laser spectrum to spread. An optical pulse in 10-Gbs/s format consists of a collection of photons with wavelength distribution spans over about 10 GHz and will travel along the fiber at different speeds. After some distance, the difference in speed will cause noticeable pulse spread in time and result in possible wrong detection at an optical receiver. Assuming electrical field of a linearly polarized light wave in a single mode-fiber is given by $E = E_0 e^{i(k_0 z - \omega t)}$, where $\beta(\omega) = n(\omega) c$ is the propagation constant at angular frequency $\omega$ and the group velocity $v_g$ is defined as $v_g = \beta_3/\beta_1 = d\beta_1/d\omega$. The frequency-dependent group velocity, i.e., the group velocity dispersion (GVD), leads to pulse broadening of

$$\Delta T = \frac{dT}{d\omega} \Delta \omega = \frac{d}{d\omega} \left( \frac{L}{v_g} \right) \Delta \omega = L \frac{d^2\beta_1}{d\omega^2} \Delta \omega = LD \Delta \lambda$$

where $D = d\omega_g^{-1} d\lambda = -2\pi c / (\lambda^2 d^2 \beta_1 / d\omega^2)$ is defined as the dispersion parameter in units of ps/km/nm. In the absence of non-linearity, pulse propagation and dispersion can be described with the first few terms of the Taylor series of $\beta(\omega)$ at the interested frequency $\omega_0$ as

$$\beta(\omega) = \beta_0 + \beta_1 (\omega - \omega_0) + \beta_2 (\omega - \omega_0)^2/2 + \beta_3 (\omega - \omega_0)^3/6$$

where $\omega_0/\beta_0$ is the phase velocity, $1/\beta_1$ is the group velocity, $\beta_2 = d^2 \beta / d\omega^2$ is the GVD parameter, and $\beta_3 = d^3 \beta / d\omega^3$ is related to the dispersion slope. CD is caused by the variation in the group velocity with respect to the frequency. $\beta_2$ and $\beta_3$, in practice, describe the measurable CD in an optical fiber.

CD limits the maximum distance of a signal transmitted without regeneration. The estimated chromatic dispersion limit of a signal with data rate of $B$ and bandwidth of $\Delta \lambda$ is given by $L_T = 1/(B D \Delta \lambda)$. The CD limited maximum transmission distance at $\lambda = 1550$ nm for two most popular optical fibers from Corning are listed in Table 1.

To overcome CD, dispersion compensation fiber (DCF) is normally used. DCF can introduce signal power loss. For example, to compensate the CD of 50 km of SMF-28 fiber (the standard single mode fiber), the compensation module

<table>
<thead>
<tr>
<th>Fiber type</th>
<th>2.5 Gbs/s $\Delta\lambda = 0.025$ nm</th>
<th>10 Gbs/s $\Delta\lambda = 0.1$ nm</th>
<th>40 Gbs/s $\Delta\lambda = 0.4$ nm</th>
</tr>
</thead>
<tbody>
<tr>
<td>SMF-28</td>
<td>930 km</td>
<td>58 km</td>
<td>3.5 km</td>
</tr>
<tr>
<td>LEAF</td>
<td>4000 km</td>
<td>250 km</td>
<td>15 km</td>
</tr>
</tbody>
</table>

$D = 17$ ps/nm/km

$D = 4$ ps/nm/km
PMD has been greatly reduced in recent deployed fibers. Corning SMF-28 standard single-mode fiber made in 2001 has a maximum PMD of 0.2 ps/√km for individual fibers. However, about 30% of the total fiber networks were deployed before 1993, which has high PMD of 1 ps/√km. In Table 2, the maximum optical transmission distance (km) limited by PMD is listed, where the EDFA and CDC dispersion parameter is assumed to be 0.141 ps/√km and the maximum tolerable PMD without PMD compensation (PMDC) is assumed to be 15% of the data period. According to Table 2, at 10 Gb/s, the transmission distance is severely limited by PMD for old fibers laid out before 1993. At 40 Gb/s, the transmission distance is severely limited by PMD for any fibers manufactured based on today’s technology. PMD compensation devices are still at the early research and development stage, with most teams working on various expensive optical solutions.

As illustrated in Fig. 1, PMD can be represented as a vector \( \hat{\tau} = \tau \hat{\rho} \), where the magnitude of the PMD vector stands for DGD, which is the time delay between orthogonal pulses. The direction of the PMD vector is represented by the unit Stokes vector \( \hat{\rho} \) in the direction of PSP. The PMD vector cannot, in general, be represented on the Poincaré sphere, as its length is other than unity. As the PSPs change the pointing direction with frequency, so does the PMD vector. Also, as the frequency changes, the vector length can change as well. Expanding the PMD vector around the interested frequency \( \omega_0 \), we have

Table 2. Maximum transmission distance limited by polarization mode dispersion.

<table>
<thead>
<tr>
<th>Fiber Type/Data Rate</th>
<th>2.5 Gbs/s</th>
<th>10 Gbs/s</th>
<th>40 Gbs/s</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bad fiber (made before 1993)</td>
<td>2763 km</td>
<td>173 km</td>
<td>11 km</td>
</tr>
<tr>
<td>Good fiber (made after 1993)</td>
<td>8750 km</td>
<td>547 km</td>
<td>34 km</td>
</tr>
<tr>
<td>Best fiber (made after 2000)</td>
<td>23,497 km</td>
<td>1469 km</td>
<td>92 km</td>
</tr>
</tbody>
</table>

Fig. 1 Vector representation of first-order and second-order PMD.
various fiber dispersions can be considered in the blind

wellian

a fixed PMD, DGD is a random variable that has a Max-

PMD vector takes over the length of a long PMD fiber. For

Gaussian distributions comes from the “random walk” the

is projected onto the three coordinates. The origin of

dependent PSP, namely, depolarization

component is the change of PSP direction with frequency

DGD with frequency, namely, the PCD. The perpendicular

nal PMD vector. The parallel component is the change of

High DGD, second-order im-

SOPMD can be expressed as

amplitude, a “sech” function.8 The magnitude SOPMD is

4

are derived in a similar manner to DGD statis-

3.1 Emulation of Chromatic Dispersion

CD is caused by the wavelength dependence of the light

slope at the zero dispersion wavelength \( \lambda_{ZD} \). The

SOPMD for SMF-28 fiber can be determined as

\[
S = \frac{dD}{d\lambda} = \frac{S_0(1 + 3\lambda_{ZD}^4/\lambda^4)}{4}.
\]

The second order and third order propagation constants are
given as follows:

\[
\beta_2 = -\frac{D}{(2\pi/c\lambda^3)}, \quad \beta_3 = \frac{S - 4\pi c \beta_2/\lambda^3}{(2\pi/c\lambda^3)^2}.
\]

qNeglecting wavelength-independent \( \beta_1 \), the light propagation
distorted by chromatic dispersion can be modeled as

\[
A(z,t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} \tilde{A}(0,\omega) \exp \left[ i \beta_2 \omega^2 + \frac{i}{6} \beta_3 \omega^3 - i\omega t \right] d\omega,
\]

where \( \tilde{A}(0,\Delta\omega) \) is the spectrum of the undistorted input
signal \( A(0,t) \).

In the CD emulator for SMF28 single-mode fibers, the zero
dispersion wavelength \( \lambda_0 = 1312 \) nm; typical dispersion
slope at \( \lambda_{ZD}S_0 \) is 0.092 [ps/(nm·km)]. Figure 2 shows the eye diagrams distorted by chromatic dispersions
for SMF-28 fiber with fiber lengths of 75 km and 100 km, respectively. Light wavelength \( \lambda = 1550 \) nm. We can see
that the longer the fiber is, the more severe the dispersion is. For a fiber length of 100 km, the eye opening magnitude
is only about 0.25, assuming the undistorted eye opening is 1.

3.2 Emulation of the First-Order PMD

The first-order PMD is wavelength-independent and is
caused by different propagation speed along principal polari-
dation directions. Emulation of the first-order PMD can be
modeled in Matlab Simulink as shown in Fig. 3. The
input signal is split into two principal polarization states
with a relative power splitting ratio of gamma (\( \gamma \)). The
signal with amplitude \( \sqrt{\gamma} \) is delayed by DGD seconds,
while another signal with amplitude \( \sqrt{1-\gamma} \) has zero delay.
Both signals are then recombined based on vector addition.
Output \( \{\text{Out1}\} \) is the intensity of the recombined signal. By
randomizing \( \gamma \), the effect of polarization scrambling can
also be emulated. To emulate the first-order PMD, we choose the relative power ratio $\gamma = 50\%$, which represents the worst-case PMD.

Figure 4 shows the simulated eye diagrams of the 40-Gb/s random signal after the first-order PMD emulator with (1) DGD = 15 ps, and (2) DGD = 25 ps, which equals the period of 40-Gb/s data. A fourth-order Bessel low-pass filter with cutoff frequency at data rate (40 GHz) is used after the emulator. For different DGD values, the simulated distorted eye diagrams are compared with the measured eye patterns generated under the same PMD conditions (40 Gb/s NRZ 231-1 PRBS). The simulated PMD distorted eye patterns agree with the measured eyes quite well. Note that no Gaussian noise has been added in the simulation. Thus, the simulated eye patterns appear as smooth curves. Gaussian ASE noise can also be added based on the different noise variances for ON and OFF signals.

### 3.3 Emulation of the Second-Order PMD

As discussed, the second-order PMD is wavelength-dependent. It has first-order PMD components and is affected by CD as well. To model the distributed random effect of the PMD, Monte Carlo simulations using a fiber waveplate model are used to generate the PMD impaired fiber. A waveplate is a birefringent medium that propagates various incoming polarizations with various time delays. The maximum and minimum time delays are expressed by the eigenstates of the waveplate. The emulator consists of $N$ number of waveplates that have a fixed DGD $\Delta \tau_p$. The model can also be extended to include a birefringent section with varying DGD. The optical axes of the waveplates are rotated randomly relative to each other, as shown in Fig. 5. The resultant PMD emulator has an average DGD of $\Delta \tau = \sqrt{8N/3} \pi \Delta \tau_p$, with the appropriate first- and second-order PMD statistics.

The concatenated birefringent waveplates can be mathematically expressed by a complex two-dimensional unitary matrix, known as the Jones matrix. The input and output optical signals can also be expressed using Jones complex vectors. The unitary propagation matrix and the complex vectors are dependent on wavelength and can thus model the second-order PMD. In addition, other fiber impairments such as loss, linear dispersion, and nonlinearities can also be added into the model. The second-order PMD is modeled in the frequency domain. The resulting field components are then transformed back to the time domain. Signal propagation is accomplished by multiplying the resulting Jones matrix for the concatenated birefringent sections and operating on an incoming input optical field at each frequency, as expressed by

![Fig. 2](image1.png)

*Fig. 2* Eye diagrams distorted by chromatic dispersions for SMF-28 fiber.

![Fig. 3](image2.png)

*Fig. 3* The first-order PMD emulator with power splitting ratio (gamma) and differential group delay (DGD) as input parameters.
\[
\begin{bmatrix}
E_i^2(\omega_k) \\
E_i^1(\omega_k)
\end{bmatrix} =
\begin{bmatrix}
u_i(\omega_k) & u_2(\omega_k) \\
-u_2(\omega_k) & u_i(\omega_k)
\end{bmatrix}
\begin{bmatrix}
E_i^2(\omega_k) \\
E_i^1(\omega_k)
\end{bmatrix},
\]  
(12)

where \( u^* \) represents the complex conjugate of the matrix element \( u \). The total propagation matrix at frequency \( \omega_k \) is obtained by multiplying the Jones matrixes of individual waveplates as

\[
\begin{bmatrix}
u_i(\omega_k) & u_2(\omega_k) \\
-u_2(\omega_k) & u_i(\omega_k)
\end{bmatrix} = \prod_{i=1}^{N} R_i^T D_i R_i = \prod_{i=1}^{N} \begin{bmatrix}
\cos(\theta_i) & -\sin(\theta_i) \\
\sin(\theta_i) & \cos(\theta_i)
\end{bmatrix}
\times \begin{bmatrix}
e^{i\phi(\omega_k)/2} & 0 \\
0 & e^{-i\phi(\omega_k)/2}
\end{bmatrix}
\times \begin{bmatrix}
\cos(\theta_i) & \sin(\theta_i) \\
-\sin(\theta_i) & \cos(\theta_i)
\end{bmatrix},
\]  
(13)

where index \( i=1,2,\ldots,N \) represents different waveplate; \( \phi(\omega_k) = \tau \omega_k \) for \( k=1,2,\ldots,M \) frequencies; \( \tau \) is the DGD; and \( \theta \) is the rotation angle of the \( i \)th waveplate.

PMD parameters such as differential group delay (DGD), polarization-dependent chromatic dispersion (PCD) are related to the Jones matrix components as follows:10,11

\[
\text{DGD} = 2\sqrt{|u_i^1(\omega)|^2 + |u_i^2(\omega)|^2}, \quad \text{or}
\]

\[
\text{DGD} = |\text{Arg}(\rho_1/\rho_2)/\omega_{i+1} - \omega_i|,
\]

where \( \rho_1 \) and \( \rho_2 \) are the eigenvalues of the matrix product \( T(\omega_{i+1}) \cdot T^{-1}(\omega_i) \). The last equation represents the derivative of DGD with respect to frequency. The total second-order PMD vector magnitude (SOPMD) is determined by first finding the output PMD vector \( \vec{\tau} \) as a function of frequency for the resultant system expressed by the Jones matrix and

\[
\text{PCD} = \frac{\text{DGD}(\omega_{i+1}) - \text{DGD}(\omega_i)}{\omega_{i+1} - \omega_i},
\]

(14)

\[
\text{Fig. 4} \text{ Simulated eye diagrams of 40-Gb/s random signal after first-order PMD emulator with (a) } \gamma = 0.5 \text{ and DGD=15 ps, (b) } \gamma=0.5 \text{ and DGD=25 ps.}
\]

\[
\text{Fig. 5} \text{ Waveplate model for emulation of fiber PMD.}
\]

\[
\text{Fig. 6} \text{ Eye diagrams distorted by second-order PMD with DGD=70.568 ps, \text{ PCD}=304.16 ps}^2, \text{ DPLZ=2004.15 ps}^2, \text{ SOPMD=2027.1 ps}^2.
\]
then its variation rate, i.e., the derivative with respect to frequency can be found by

\[
\text{SOPMD} = \frac{\dot{\tau}_{i+1} - \dot{\tau}_i}{\omega_{i+1} - \omega_i}. \tag{15}
\]

Note that the two orthogonal components of the total SOPMD vector are the PCD and the depolarization (DPLZ). The depolarization can thus be obtained by

\[
\text{DPLZ} = \sqrt{\text{SOPMD}^2 - \text{PCD}^2}. \tag{16}
\]

Figure 6 gives a simulated eye diagram distorted by second-order PMD with DGD=70.568 ps, PCD=−304.16 ps², DPLZ=2004.15 ps², and SOPMD =2027.1 ps². In the simulation, 10,000 fibers are used to emulate the random statistics of fiber PMD. Each fiber section consists of 12 waveplates with 10-ps delay to model the distributed dispersion effect of the fiber.

4 Adaptive Electronic Equalizations

As shown, fiber communication is limited by transmission impairments due to fiber dispersions. Optical devices are only capable of compensating one form of the dispersions with very high cost, high insertion loss, and slow tuning speed if they are tunable at all. In contrast, electronic equalizers are low cost, tunable, and capable of compensating all forms of fiber dispersions. Figure 7 shows an integrated adaptive fiber transceiver with analog equalizers for fiber dispersion compensation. During operation, data transmitted at lower rates can be fed in a parallel fashion into an N:1 multiplexer, which generates a relatively high-transmission-rate data stream. The data stream can then be amplified by a modulator driver for driving external optical modulator. Polarization scrambler can be inserted after optical modulator to randomize the polarization direction of the transmitted light. When light intensities along the principal polarization directions are the same, the system suffers a maximum power penalty due to PMD. Thus, by scrambling the polarization of the transmitted optical signal, the average PMD related power penalty is reduced because of a lower probability that the system will be locked in states with large power penalties.

Erbium doped fiber amplifier (EDFA) can be inserted after the scrambler to provide sufficient power for transmission of the optical signal along a standard single-mode fiber (SSMF).

On the receiver side of the circuit, another EDFA is used to compensate for gain lost during transmission and also provides an overall gain control so that photodetector (PD) and front-end amplifier can operate in their proper dynamic ranges. The received optical signal is converted to electrical signal using a PD. A trans-impedance amplifier (TIA) is
used to convert the electrical current mode signal to voltage mode signal. After the decision stage, the data stream can be used to recover the clock, which is synchronized with the data. Clock and data recovery circuitry can be embedded in an adaptive receiver. The receiver IC preferably detects errors occurring during data detection and adjusts the decision thresholds adaptively. Error detection can include top and bottom error detectors, and respective top and bottom error counters. Error detection can also include left and right error detectors, and respective left and right error counters. The detected error signals indicate the degree of eye opening and are processed by a digital signal processing chip embedded with the equalization algorithms. A DAC provides the analog feedback control signals needed for adaptive thresholds and equalizer tap coefficients. The high-speed analog electronic equalizers can be implemented in SiGe and CMOS technologies. Figure 8 further illustrates analog electronic equalizers including a feed forward equalizer (FFE) and decision feedback equalizer (DFE). The voltage signal output from the TIA is fed to the data input of the FFE, which performs the dispersion compensation for the distorted voltage signal. The output of the FFE is experienced additional compensation at the DFE. The compensated signal is then fed into a clock data recovery block to recover the data clock. FFE, a linear equalizer, is used to compensate for moderate amplitude distortion. On the other hand, a decision feedback equalizer is used to improve receiver performance in the presence of moderate to severe amplitude distortion. A DFE is intrinsically nonlinear as it feeds back to the input a sequence of hard decisions made at the equalizer output. The feedback section removes the lagging intersymbol interference that is beyond the reach of the forward section. However, the DFE suffers from the problem of error propagation since hard decisions may destroy information: once a wrong decision is made, errors are fed back to the equalizer input, which in turn leads to a higher probability of error on subsequent decisions. The end result is a burst of errors. Moreover, like any feedback system, a DFE design involves stability analysis, while an FFE is always stable. The performance of an analog electronic equalizer is limited by the circuit linearity and bandwidth. The equalizer circuit should have minimum group delay in order to minimize the additional dispersion due to the equalizer. The implementation of the high-speed equalizer is not easy even at 10 Gb/s, and it is very challenging at 40 Gb/s. Even if the equalizer itself can be implemented for high-data-rate applications, the feedback circuits cannot operate at the data rate, since complicated calculations need to be done within one clock cycle. Fortunately, fiber dispersion is either a time-invariant (e.g., CD) or slow time-variant (e.g., PMD) process. The feedback circuit thus needs only operate at a much slower frequency than the data rate. The input to the feedback block can be an accumulated averaged data, as illustrated in Fig. 7. The tap coefficients of the equalizer are thus updated at a much slower frequency as well. An alternate approach is to sample the input distorted signal using a high-speed analog-to-digital converter (ADC), if such as a converter is available. Thus, all the equalizations, and error corrections plus equalization feedback algorithms can be implemented digitally, providing a more accurate and higher performance alternative to analog equalizers. The digital equalization approach is illustrated in Fig. 9.

5 Feedback Algorithm for Electronic Equalizers Various adaptive equalizer algorithms have been developed for digital signal processing. LMS maximum likelihood algorithms are widely used in equalizer designs. Recursive least-squares (RLS) algorithm achieves faster convergence, but is computationally more complex than LMS since matrix inversion is required. The reference signal required by the LMS algorithm can be either provided by a transmitted training sequence or estimated by the detected bits. Decision-directed tap adaptation uses the output of the slicer/decision circuit as an estimation of the transmitted sequence. LMS is simple and can be implemented for FFE and DFE equalizations. For higher data rates, the steepest descent algorithm can be used, which consecutively dithers the equalizer taps to achieve the optimized signal quality. As a simplified variant of LMS, sign-sign LMS
algorithm evaluates only the signal signs, which has greatly reduced computation time, yet with very “noisy” gradient estimate. The biggest advantages of sign-sign LMS algorithm is that it does not require any high-speed ADC and thus can be implemented at high speed.

The drawback of conventional equalization algorithms lies on the fact that they need the assistance of a training sequence, which is not suitable for applications with a varying channel environment. On the other hand, blind equalization provides a reference-free equalization algorithm, which meets the current fiber communication transmission standard. Blind equalization is thus critical for agile optical networks, where the channel environment varies constantly. Since binary ON-OFF key modulation with constant envelope is used in fiber communication system, constant-modulus adaptive algorithm (CMA) is proposed for fiber dispersion compensation using blind equalization. The key to the success of a blind equalization is the efficient error estimation through built-in eye-open detection circuits such as the one proposed in the previous section.

5.1 LMS Equalization

If a reference training sequence is transmitted during a pre-assigned time slot, the equalizer coefficients can be adapted by using the LMS adaptive algorithm so that the output of the equalizer closely matches the training sequence. The LMS reference can also be estimated by the detected bits. In this case, a blind equalization is implemented with the goal of widening the eye-open for improved BER. If $r_k$ is the reference signal and $y_k$ is the equalizer output at time instance $k$, respectively, the error signal of LMS is defined as

$$e_k = r_k - y_k = r_k - W_k^T X_k,$$

where $X_k$ is the equalizer input signal and $W_k$ is the equalizer tap coefficients at time instance $k$, respectively. The cost function to be minimized is defined as

$$J_k = e_k^2 = (r_k - W_k^T X_k)^2.$$  \hspace{1cm} (17)

In each iteration, the gradient is estimated by

$$\nabla J_k = \frac{\partial J_k}{\partial W_k} = 2e_k \frac{\partial e_k}{\partial W_k} = -2e_k X_k.$$  \hspace{1cm} (18)

With the steepest descent adaptive algorithm and a bounded step size $\mu$, the equalizer tap coefficients can thus be adapted as follows:

$$W_{k+1} = W_k - \mu \nabla J_k.$$  \hspace{1cm} (19)

The key to the success of a blind equalization is the efficient error estimation through built-in eye-open detection circuits such as the one proposed in the previous section.

Table 3 TAP coefficients of 3-, 5-, and 7-tap LMS FFE for first-order PMD compensation with DGD=0.25%, 0.5%, and 0.75% symbol period.

<table>
<thead>
<tr>
<th>DGD</th>
<th>25%</th>
<th>50%</th>
<th>75%</th>
</tr>
</thead>
<tbody>
<tr>
<td>C1 of 3-tap FFE</td>
<td>0.001295</td>
<td>-0.03202</td>
<td>-0.3023</td>
</tr>
<tr>
<td>C2 of 3-tap FFE</td>
<td>1.185</td>
<td>1.2</td>
<td>1.515</td>
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<tr>
<td>C3 of 3-tap FFE</td>
<td>-0.2147</td>
<td>-0.1914</td>
<td>-0.2791</td>
</tr>
<tr>
<td>C1 of 5-tap FFE</td>
<td>0.00003686</td>
<td>0.001223</td>
<td>0.06619</td>
</tr>
<tr>
<td>C2 of 5-tap FFE</td>
<td>0.0009815</td>
<td>-0.03445</td>
<td>-0.3336</td>
</tr>
<tr>
<td>C3 of 5-tap FFE</td>
<td>1.187</td>
<td>1.204</td>
<td>1.532</td>
</tr>
<tr>
<td>C4 of 5-tap FFE</td>
<td>-0.2232</td>
<td>-0.197</td>
<td>-0.3061</td>
</tr>
<tr>
<td>C5 of 5-tap FFE</td>
<td>0.04044</td>
<td>0.03116</td>
<td>0.05649</td>
</tr>
<tr>
<td>C6 of 5-tap FFE</td>
<td>0.0001306</td>
<td>-0.0002302</td>
<td>-0.0153</td>
</tr>
<tr>
<td>C7 of 5-tap FFE</td>
<td>0.0001521</td>
<td>0.001364</td>
<td>0.07292</td>
</tr>
<tr>
<td>C8 of 5-tap FFE</td>
<td>0.0009156</td>
<td>-0.03417</td>
<td>-0.3367</td>
</tr>
<tr>
<td>C9 of 5-tap FFE</td>
<td>1.187</td>
<td>1.204</td>
<td>1.543</td>
</tr>
<tr>
<td>C10 of 5-tap FFE</td>
<td>-0.2236</td>
<td>-0.1972</td>
<td>-0.3088</td>
</tr>
<tr>
<td>C11 of 5-tap FFE</td>
<td>0.042</td>
<td>0.03221</td>
<td>0.06169</td>
</tr>
<tr>
<td>C12 of 5-tap FFE</td>
<td>-0.007656</td>
<td>-0.005136</td>
<td>-0.01132</td>
</tr>
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</table>

Fig. 10 PMD compensation using a 7-tap analog FFE. (a) Eye diagram distorted by first-order PMD with power splitting ratio=0.5 and DGD=0.8 period. (b) Compensated eye diagram with LMS adaptive feedback. (c) Compensated eye diagram with fixed tap coefficients.
5.2 CMA Blind Equalization

Inclusion of the training sequence with the transmitted information adds an overhead and thus reduces the throughput of the system. Therefore, to reduce the system overhead, adaptation schemes are preferred that do not require training, i.e., blind adaptation schemes. In blind equalization, instead of using the training sequence, one or more properties of the transmitted signal are used to estimate the inverse of the dispersive channel. Unlike the LMS algorithm, which assumes a reference \( r_k \), the error \( e_k \) in Eq. (17) cannot be used to define the cost function in blind equalization. Since the transmitted signal in fiber communication is of the constant amplitude, we can assume constant amplitude \( A \) in the absence of signal degradations. Then, the error signal in blind equalization can be defined as

\[
e_k = |y_k|^2 - A^2.\tag{21}
\]

The cost function can be further defined as

\[
J_k = E(e_k^2) = E\{(y_k^2 - A^2)^2\} \tag{22}
\]

The true gradient of \( J \) at time step \( k \) can be approximated by its instantaneous value as

\[
\nabla J_k = \frac{\partial J_k}{\partial W_k} = 2e_k \frac{\partial e_k}{\partial W_k} = 4e_k y_k X_k = 4(y_k^2 - A^2)y_k X_k. \tag{23}
\]

The CMA recursion expression becomes

\[
W_{k+1} = W_k - \mu \nabla J_k = W_k - \mu (y_k^2 - A^2)y_k X_k, \tag{24}
\]

where the equalizer output is \( y_k = W_k^T X_k \).

6 Simulation Results

6.1 LMS Equalizer

To demonstrate the effect of an electronic equalizer on fiber dispersion compensation, we simulated a 7-tap analog feed forward equalizer (FFE) with LMS feedback algorithm for PMD compensation (Fig. 10) and chromatic dispersion compensation (Fig. 11). Note that the severely distorted signal can be compensated using just 7 taps in an analog transversal equalizer. With the adaptive feedback, the tap coefficients are constantly adjusted based on the error signal. Even without feedback, the fixed coefficient equalizer can still open the distorted eye. For a fixed network, we can thus predetermine the equalizer tap coefficients and load them into the equalizer at the field, which is very attractive from a cost reduction point of view. For chromatic dispersion, tap coefficients can be programmed based on the length and type of the fiber, providing a much more economic way than the current solution using dispersion compensation fiber (DCF), which is static and also wavelength-dependent. As a reference for practical designs, we summarize in Table 3 the tap coefficients of 3-, 5-, and 7-tap LMS transversal equalizers for first-order PMD compensation with DGD=0.25%, 0.5%, and 0.75% of the symbol period, respectively.

6.2 CMA Blind Equalizer

In simulation for blind equalization, we set signal amplitude \( A \) to 1 and normalized the input signal to the range of \([-1, 1]\). Baud-Spaced CMA (sampling period equal to the symbol period) is used, and tap coefficient \( W_0 \) is initialized to be “Single-Spike” (one nonzero tap coefficient, and all other to 0). Three scenarios with different settings of DGD are investigated. Symbol period is set to be 0.025 nsec (25e−12 seconds). Simulation results for DGD of 80% of
In all scenarios, feedback gain $\mu$ is set to 0.005. In Fig. 12(a) and 12(b), show the eye diagrams before and after the compensation; (c) gives the initial and adapted tap coefficients; and (d) plots the eye opening and the cost function $J$, which is defined in (22) and ideally converges to 0. Assuming the eye is constant along the horizontal direction, the eye-open is then measured as the vertical height between the mean of peak amplitudes and the mean of valley amplitudes, which converges to value 2 ideally. Note that when DGD is 80\% of the symbol period, it takes more than 100 nsec for the coefficients to converge, and the cost function $J$ cannot fully converge to 0 and it stays around 0.1, but the eye is opened much wider than the distorted one.

We then applied our CMA equalizer to CD compensation, and the compensated eyes are shown in Fig. 13 for a 7-tap FFE. We investigated two fiber lengths of 75 km and 100 km with their distorted eyes given in Fig. 2. As a quantitative comparison, the CD distorted eye opening for 75-km fiber is from $-0.75$ to $0.4$, while the CMA compensated eye opening is from $-0.9$ to $0.75$, with 143\% improvement. For 100-km fiber, the CD distorted eye opening is from $-0.5$ to $0.25$, while the CMA compensated eye opening is from $-0.9$ to $0.6$, with 200\% improvement.

7 Conclusions

This paper presented rigorous channel models for various fiber dispersions and investigated their mitigations using digital and analog electronic equalizers. A novel CMA-based blind electronic equalization technique is proposed. While LMS feedback algorithm requires a training sequence to obtain the equalizer coefficients, the blind equalization automatically finds the optimal tap coefficients uti-
lizing the constant amplitude features in binary fiber transmissions. As a reference for LMS-based transversal equalizer design, the optimal tap coefficients for first-order PMD compensation have been summarized in Table 3. For CMA blind equalization, PMD compensation with DGD =80% symbol period and CD compensation with 200% eye-opening improvement were demonstrated. Also discussed is the adaptive fiber transceiver architecture with eye-open detectors that can be used to provide the feedback control for high-speed analog equalizers.

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References


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