

Privacy Protected Query Processing on Spatial Networks

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Abstract

With the proliferation of mobile devices (e.g., PDAs, cell phones, etc.), location-based services have become more and more popular in recent years. However, users have to reveal their location information to access location-based services with existing service infrastructures. It is possible that adversaries could collect the location information, which in turn invades user's privacy. There are existing solutions for query processing on spatial networks and mobile user privacy protection in Euclidean space. However there is no solution for solving queries on spatial networks with privacy protection. Therefore, we aim to provide network distance spatial query solutions which can preserve user privacy by utilizing K -anonymity mechanisms. In this paper, we present two novel query algorithms, PSNN and PSRQ, for answering nearest neighbor queries and range queries on spatial networks without revealing private information of the query initiator. The effectiveness of our privacy protected algorithms has been validated using real world road networks. In addition, we demonstrate the appeal of our technique using extensive simulation results.

1 Introduction

Due to the recent advances in low-power technologies, mobile devices with computation, storage, and wireless communication capabilities have become increasingly popular. At the same time, the technique of positioning systems is embedded into these mobile devices. As a result, new mobile applications allow users to issue location-dependent queries in a ubiquitous manner. Examples of such location-dependent queries include 'find the nearest gas station' and 'find the top three closest French restaurants'. To get location-dependent data, users have to reveal their current locations when launching location-dependent queries. From the location-dependent query logs of location-based service providers (LBSP), it is possible that adversaries could collect the location history and monitor the behavior of some users, which in turn invades their privacy. Therefore, with the popularity of location-based services (LBS), user privacy protection is a very important research issue to be studied.

Recent research has explored the K -anonymity con-

cept [16]¹ in which one trusted server is needed to cloak at least K users' locations for protecting location privacy. In order to implement K -anonymity, one trusted server is set up to collect user location information and perform cloaking procedures in which the exact location of the query requester is blurred as a cloaked spatial area whose boundary is defined by the locations of $K - 1$ other users. Then, the trusted server will send the location-dependent query along with the cloaked spatial area to location-based service providers to retrieve location-dependent data. Note that since the query location is an area instead of a single query point, location-dependent service providers should fetch those query results based on the cloaked spatial region. Prior work in [12] proposed a framework for location services without compromising location privacy. However, only a free space environment is considered, which is not fully applicable in real world environments. On the other hand, recent research has produced novel mechanisms to compute location-dependent queries on spatial networks. For example, executing nearest neighbor queries based on the spatial network distance provides a more realistic measure for applications where mobile user movements are constrained by underlying networks. Though devising spatial query schemes in spatial networks, the prior works in [13, 10] did not consider location privacy issues. Thus, we aim to provide spatial query (nearest neighbor query and range query) solutions with privacy protection concerns in this study. With our techniques location-based service users can obtain high quality results without sacrificing their privacy. The contributions of our study are as follows.

- We propose a novel algorithm for solving privacy protected nearest neighbor queries on spatial networks.
- We extend our nearest neighbor query solution to answer range queries with protection of privacy.
- We demonstrate the feasibility and efficiency of our approach through extensive simulations.

¹Note that we use the symbol K for the degree of anonymity and k for k nearest neighbor queries.

2 Related Work

In this section, we introduce the background information and related research regarding spatial queries, location-based services, and location privacy preservation.

2.1 Spatial Queries

We focus on two common types of spatial queries, namely k nearest neighbor queries and range queries. With R-tree [8] based spatial indices, depth-first search (DFS) [14] and best-first search (BFS) [9] have been the prevalent branch-and-bound techniques for processing nearest neighbor (NN) queries. In order to increase the NN query accuracy, recent research proposed solutions based on spatial networks. Kolahdouzan et al. [10] presented a novel approach to efficiently evaluate k NN queries in spatial network databases using a first order Voronoi diagram. Papadias et al. [13] proposed two algorithms, the Incremental Euclidean Restriction (IER) algorithm and the Incremental Network Expansion (INE) algorithm to solve nearest neighbor queries on spatial networks.

For range queries that find objects within a specified area, the R-tree families provide efficient access to disk-based databases. Basically, an R-tree structure groups objects close to each other into a minimum bounding rectangle (MBR), and a range query only visits the MBRs that overlap with the query area. All the aforementioned spatial query techniques do not take user privacy protection into account.

2.2 Location Privacy Preservation

With the popularity of location-based services, privacy protection for mobile users has become an important issue [7, 15]. Gruteser et al. [6] proposed a middleware architecture and algorithms for maintaining location K -anonymity. Their algorithms adjust the resolution of location information along spatial or temporal dimensions to fulfill the required anonymity constraints. Based on the work in [6], a unified privacy personalization framework is proposed in [5] to support different levels of anonymity according to the requests of users. However, these previous research approaches mainly focused on the system architecture and the location anonymizer design rather than query processing. Mokbel proposed to employ a trusted third party, the *location anonymizer*, which expands the user location into a spatial region for protecting user privacy [11]. Mokbel et al. also proposed related privacy-aware query processing algorithms [12]. However their query processing solutions are based on Euclidean metrics. In real life, mobile users cannot move freely in space but are usually constrained by underlying networks (e.g., cars on roads, trains on tracks, etc.). Therefore, we need solutions for processing privacy protected queries on spatial networks.

3 System Architecture

In this section, we describe the system architecture for supporting privacy protected spatial queries with underlying

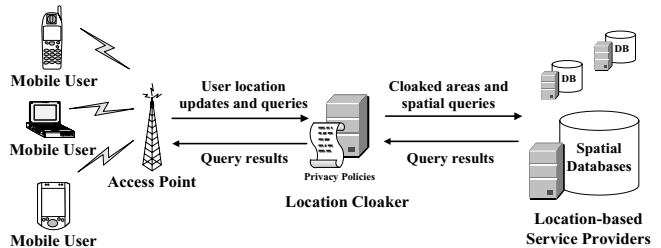


Figure 1. The system architecture.

spatial networks. Figure 1 depicts our operating environment with three main entities: *mobile users*, the *location cloaker*, and *location-based service providers*. We consider mobile clients such as cell phones, personal digital assistants (PDA), and laptops, that are instrumented with a global positioning system (GPS) for continuous position information. Furthermore, we assume that there are access points/base stations distributed in the system environment for mobile devices to communicate with the location cloaker. All users are mobile and travel on the underlying network and they also hold *privacy policies* which specify their privacy requirements. In this research we focus on two parameters, K -anonymous and the minimum cloaked region size, R_{min} , that are included in the user privacy policies. A user can demand the cloaked area to cover the locations of $K - 1$ closest peers for anonymizing its exact location. In order to keep a reasonable size of the cloaked area in high user density regions, the user decides the minimum acceptable size of R_{min} . Based on privacy requirements at different locations or time slots, a user can update his/her privacy policies at any time.

3.1 The Location Cloaker

Compared with location-based service providers, the location cloaker is an intermediate agent which can be trusted by mobile users. The location cloaker receives continuous location updates from mobile users and blurs their exact locations into cloaked areas A_c according to individual user privacy policies before forwarding the information to location-based service providers (e.g., for buddy searching services). In addition, the location cloaker also anonymizes the location of any query requesting user q to a cloaked region before forwarding the query to related location-based service providers. Note that any user identity related information in the query is also removed by the location cloaker during the cloaking process.

According to previous research [12, 6, 5] there are several different mechanisms to support location anonymization. However compared with existing solutions, the location anonymizing technique proposed by Mokbel et al. [12] has prominent efficiency (low cloaking time) and flexibility (user defined privacy profile). Therefore, we adopt the grid-based complete pyramid data structure proposed in [12] for our system to provide cloaking functionalities.

3.2 Location-based Service Providers

Location-based service providers play the role of spatial data maintainers and spatial query processors in our system. In order to handle privacy protected spatial queries, location-based service providers implement *privacy protected query processors* in their databases. The privacy protected query processor has the ability to process cloaked spatial queries efficiently and retrieves the *inclusive result set* (i.e., the minimal set which covers all the possible answers) for query requesters. After receiving the result set, mobile users can distill the exact answers from their locations in linear time. The privacy policies of a user determine the computational complexity of his/her spatial queries. Strict privacy requirements (i.e., large K and R_{min} values) increase the complexity of processing the query.

In addition to a privacy protected data processor, a LBSP also needs to maintain spatial databases for storing (cloaked) user locations, spatial data and road networks. The stored spatial data can be categorized as public data and private data. Public data covers static objects such as restaurants, hotels, and gas stations and the dynamic information (e.g., real-time bus locations) which are directly open to public queries. In contrast, private data mainly comprise cloaked mobile user locations from the location cloaker. Based on the two data categories, the spatial queries submitted to a LBSP can be classified as four types: (1) *public queries over public data*, (2) *public queries over private data*, (3) *private queries over public data*, and (4) *private queries over private data*. For the first query type, there were already existing solutions proposed in [13, 10]. Because the movement of mobile users is limited by the underlying road networks, we can easily extend the mechanisms proposed in [13, 10] for solving queries of the second query type (e.g., Figure 2a) with probability density functions [3]. To the best of our knowledge, there is no existing solution for the third query type. Similarly the fourth query type (e.g., Figure 2b) can be answered by extending the algorithms of the third query type. Therefore, we propose our novel techniques for solving private queries over public data on spatial networks in Section 4.

In order to support queries on spatial networks, we as-

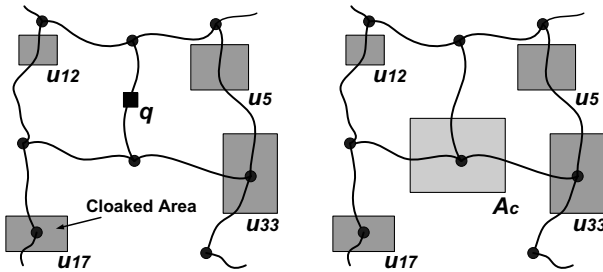


Fig. 2a. Public query over private data.

Fig. 2b. Private query over private data.

Figure 2. Two novel query types.

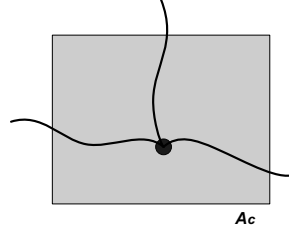


Fig. 3a. The network segments in A_c are totally connected.

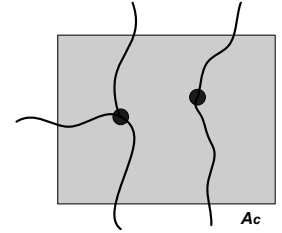


Fig. 3b. The network segments in A_c comprise two separate subgroups.

Figure 3. The two possible connection statuses of the network segments inside a cloaked area A_c .

sume a digitization process that generates a modeling graph from an input spatial network. The modeling graph contains three categories of graph nodes: the network junctions, the start/end points of a road segment, and other auxiliary points (e.g., speed limit change points). In addition, as discussed in [13], we assume that the spatial network database supports the following primitive operations:

- $inside_segments(A_c)$: returns a set of subsegments of a network N which intersects with the cloaked area A_c .
- $find_objects(segment_x)$: returns the data objects which fall on the input network segment $segment_x$.
- $Dist(p_1, p_2)$: calculates the network distance of two input points, p_1 and p_2 , in the underlying network by applying an algorithm (e.g., Dijkstra's algorithm [4]) to compute the shortest path between p_1 and p_2 .

4 Privacy Protected Query Processing

We illustrate our mechanisms for solving private queries over public data on road networks in this section. We focus on two popular query types, nearest neighbor queries and range queries.

4.1 Privacy Protected Nearest Neighbor Query on Spatial Networks

Given a query point q and an object data set \mathbb{S} , a network k nearest neighbor query retrieves the k objects of \mathbb{S} closest to q based on the network distance. Papadias et al. [13] proposed two algorithms (*incremental euclidean restriction* and *incremental network expansion*) to efficiently solve nearest neighbor queries with spatial network databases. However in order to protect user privacy, a location-based service provider can only receive cloaked spatial areas from users. Therefore, LBSPs need to have a competent mechanism for retrieving an inclusive query result set based on the input cloaked area and the underlying spatial network. We design a *privacy protected spatial network nearest neighbor query* (PSNN) algorithm by extending the incremental network expansion solution [13].

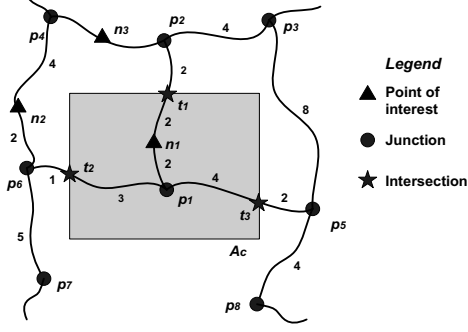


Figure 4. Searching k network nearest neighbors with PSNN where the cloaked area contains k objects ($k = 1$ in this example).

PSNN first locates all the intersection points between the edges of the input cloaked area A_c and the spatial network as a point set \mathbb{T} by executing primitive database operations. If \mathbb{T} is not empty, A_c covers at least one network segment. We denote these network segment(s) within A_c as Seg_i and the segments outside A_c as Seg_o . According to the network topology, the network edges inside A_c can be fully connected or comprise several separate subgroups. Figure 3 illustrates the two cases. Since we designed efficient solutions for the case in which the network edges inside A_c are fully connected, we can utilize the divide and conquer strategy to handle the case demonstrated in Figure 3b. Consequently, we perform a pre-process for splitting the input cloaked area until each subregion contains only one connected network segment set. Then we execute our algorithms on each subregion separately and merge their results after the whole computation. For ease of presentation, we assume the pre-process has been done in the following sections.

We observe that the number of data objects inside a cloaked area A_c can meet one of two conditions: (i) there are at least k objects inside A_c or (ii) there are fewer than k objects within A_c .

4.1.1 The Cloaked Area Contains at Least k Objects

Since Seg_i contains a limited number of network segments, PSNN starts the search on Seg_i for retrieving data objects inside A_c . If Seg_i covers more than or equal to k data objects, the search can be finished by expanding the intersection points in \mathbb{T} . First PSNN includes the data objects within A_c into the result set \mathbb{R} . Next, for each point t_i in \mathbb{T} , PSNN calculates the distance from t_i to its k^{th} nearest object inside A_c as $Dist(t_i, n_k)$, and then expands outward from point t_i to search for data objects on Seg_o within distance $Dist(t_i, n_k)$. Consequently, we can cover the special case when q is located exactly at t_i . All the newly discovered data objects are inserted into the result set \mathbb{R} .

Figure 4 demonstrates an example where the circles represent the nodes in the modeling graph, triangles indicate the data objects, and the gray rectangle stands for the cloaked

area. Assuming that only one nearest neighbor is queried ($k = 1$), PSNN first retrieves n_1 by searching the network segments inside A_c . Since the number of data objects found in A_c is equal to 1, PSNN computes the network distance from t_1 , t_2 , and t_3 to n_1 as 2, 5, and 6 respectively. Afterwards, PSNN expands the search space outbound from the three intersection points according to their distance to n_1 . No data object is found from the expansion of t_1 and t_3 . The expansion of t_2 reaches n_2 and it is inserted into the result set. Consequently, the final search result set covers objects n_1 and n_2 .

4.1.2 The Cloaked Area Contains Fewer than k Objects

If there are fewer than k data objects found on Seg_i , PSNN has to search the network segments which are outside of A_c . Since the points in \mathbb{T} are all on the boundary of A_c , they determine the network search expansion upper bound. Consequently, PSNN executes the network expansion from all the intersection points for retrieving an inclusive result set. For every point t_i in \mathbb{T} , the PSNN algorithm first retrieves the network segment $p_m p_n$ which passes through t_i and searches all data objects on this segment. In the meantime, the two end points p_m and p_n are inserted into a queue Q with their distance to t_i . Afterward, if the search found fewer than k objects on $p_m p_n$ or the search retrieved no fewer than k objects but one end point of $p_m p_n$ whose distance to t_i is shorter than $Dist(t_i, n_k)$ (n_k is the k^{th} nearest neighbor of t_i), the end point p_x which is closer to t_i will be popped from Q and expanded. For each non-visited adjacent point p_y of p_x , PSNN searches $p_x p_y$, updates the result set, and inserts p_y with its distance to t_i into Q . Then the point in Q with the shortest distance to t_i is de-queued. The procedure repeats until k nearest neighbors of t_i are found and the k objects are inserted into the result set \mathbb{R} . PSNN repeats the whole process until it has expanded all the points in \mathbb{T} .

4.2 Privacy Protected Range Query on Spatial Networks

We define a spatial network range query as follows: given a query point q , a range value r , and an object data set \mathbb{S} , the query retrieves all elements of \mathbb{S} that are within network distance r from q . For executing a *privacy protected spatial network range query* (PSRQ), first we have to locate the intersection points of the cloaked spatial area A_c and the underlying road network as a point set $\mathbb{T} = \{t_1, \dots, t_m\}$. Then, PSRQ searches the network segments inside A_c and inserts the retrieved objects into \mathbb{R} . For each point t_i in \mathbb{T} we can compute a set of *candidate segments* within network range r from t_i and then retrieve the data objects falling on these segments. Because the search range r could be a large number and it may cover many candidate segments, it is inefficient to check each candidate segment with the primitive operation $find_objects(segment)$. Therefore, we utilize

Algorithm 1 PSNN (q, k, A_c)

```
1: locate the intersection points between  $A_c$  and the underlying network
   as  $\mathbb{T} = \{t_1, \dots, t_m\}$ 
2:  $Seg_i = inside\_segments(A_c)$ 
3: search objects on  $Seg_i$  and insert the retrieved objects into  $\mathbb{R}$ 
4: if  $Seg_i$  covers  $\geq k$  objects then
5:   for  $\forall t_i \in \mathbb{T}$  do
6:     expand  $t_i$  outward  $A_c$  for searching objects within distance
        $Dist(t_i, n_k)$ 
7:     insert any discovered objects into  $\mathbb{R}$ 
8:   end for
9: else
10:  for  $\forall t_i \in \mathbb{T}$  do
11:     $p_m p_n = find\_segment(t_i)$ 
12:     $R_i \cup find\_objects(p_m, p_n)$ 
    /*  $\{n_1, \dots, n_k\}$  = the  $k$  nearest objects in  $R_i$  sorted in ascend-
    ing order,  $n_j, n_{j+1} \dots, n_k$  may be  $\emptyset$ , if  $|R_i| < k$  */
13:     $Dist_{max} = Dist(t_i, n_k)$ 
    /*  $Dist_{max} = \infty$ , if  $n_k = \emptyset$  */
14:     $Q = \langle (p_m, Dist(p_m, t_i)), (p_n, Dist(p_n, t_i)) \rangle$ 
15:    de-queue the node  $p$  in  $Q$  with smaller  $Dist(p, t_i)$ 
16:    while  $Dist(p, t_i) < Dist_{max}$  do
17:      for each non-visited adjacent vertex  $p_x$  of  $p$  do
18:         $R_i \cup find\_objects(p_x, p)$ 
19:        update  $Dist_{max}$  with sorted  $R_i$ 
20:        en-queue( $p_x, Dist(p_x, t_i)$ )
21:      end for
22:      de-queue the next vertex  $p$  in  $Q$ 
23:    end while
24:     $\mathbb{R} = \mathbb{R} \cup R_i$ 
25:  end for
26: end if
27: Sort  $\mathbb{R}$  for removing duplicates
28: return  $\mathbb{R}$ 
```

the intersection join function [2] for retrieving all intersection object pairs from the spatial network R-tree and the object R-tree. When reaching the leaf node level, PSRQ executes the plane-sweep method with the object R-tree nodes which intersect with the MBR of at least one candidate segment and stores the qualified objects into \mathbb{R} .

An example is demonstrated in Figure 5. Assuming r is equal to a 7 unit distance, PSRQ joins the candidates segments (solid lines) with the object R-tree and retrieves leaf node E_5 intersecting with segment $p_4 p_6$. After executing the intersection test (plane-sweep method), PSRQ retrieves

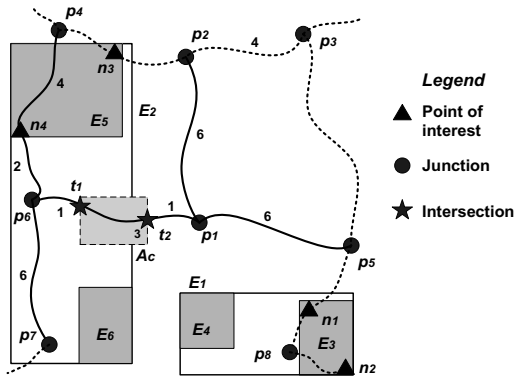


Figure 5. Network range query with PSRQ.

n_4 as the query result. The complete algorithm of PSRQ is shown in Algorithm 2.

5 Experimental Validation

We implemented our privacy protected query algorithms in a simulator to evaluate the performance of our approach. Our main objectives are to observe the influence of performance related factors (e.g., cloaked region size) on the system. Performance is measured in terms of the result set size and CPU time. All simulation results were recorded after the system model reached steady state.

5.1 Simulator Implementation

Our simulator consists of three main components, the *mobile environment*, the *location cloaker*, and the *location-based service provider*. For the mobile environment, we utilized the *network-based moving objects generation framework* [1] to produce a set of mobile users and the underlying road network inside a geographical area, measuring 10 miles by 10 miles. Each mobile user is an independent object which encapsulates all of its related parameters (e.g., its current speed and destination). We implemented the location cloaker as a new module for interacting with mobile users to anonymize spatial queries in the framework. Our privacy protected query approaches (Section 4.1 and Section 4.2) were also implemented inside the framework as new functions and play the role of the LBSP. We obtained our road network data from the TIGER/Line street vector data available from the U.S. Census Bureau.

5.2 Exploring Performance Influencing Factors

We are interested in the effect of three major performance influencing factors: the cloaked region size, the number of k , and the Point of Interest (POI) number, of spatial queries. We experimented with both nearest neighbor queries and range queries with these factors as follows.

5.2.1 Effect of the Cloaked Region Size

We first varied the cloaked region size from 2% to 10% of the whole experimental region. Figure 6 demonstrates

Algorithm 2 PSRQ (q, r, A_c)

```
1: locate the intersection points between  $A_c$  and the underlying network
   as  $\mathbb{T} = \{t_1, \dots, t_m\}$ 
2:  $Seg_i = inside\_segments(A_c)$ 
3: search objects on  $Seg_i$  and insert the retrieved objects into  $\mathbb{R}$ 
4: for each point  $t_i$  in  $\mathbb{T}$  do
5:   Compute all the candidate segments within distance  $r$  from  $t_i$  as  $C$ 
6:   Intersection join  $C$  with the object R-tree for finding intersection
   leaf nodes
7:   for each retrieved leaf node  $E_i$  do
8:      $R_{ti} =$  intersection test of the intersected segments with data ob-
       jects in  $E_i$ 
9:   end for
10:   $\mathbb{R} = \mathbb{R} \cup R_{ti}$ 
11: end for
12: Sort  $\mathbb{R}$  for removing duplicates
13: return  $\mathbb{R}$ 
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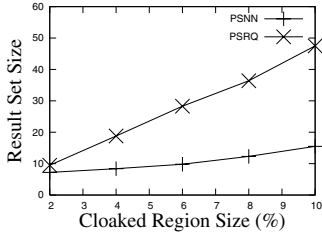


Fig. 6a. Result Set Size.

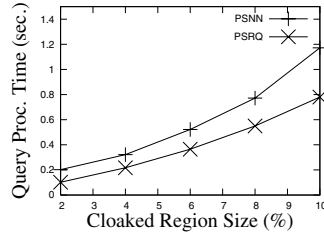


Fig. 6b. Query Proc. Time.

Figure 6. The effect of the cloaked region size.

the result set size and query processing time with different cloaked region sizes. Since a bigger cloaked region usually intersects with more underlying network segments, it generates a larger candidate result set and takes longer to process. As shown in Figure 6a., the curve of PSRQ remarkably increases because the result set covers all the POIs within the cloaked region and the search range r . In contrast, PSNN removes duplicated objects from \mathbb{R} . In addition, the query processing time of PSNN increases notably with an enlarged cloaked region size as illustrated in Figure 6b.

5.2.2 Effect of k

Next we tested the impact of varying the number of requested nearest neighbors, i.e., k . We altered k in the range from 4 to 20. As shown in Figure 7, the result set size grows when we raised k from 4 to 20 and we also observe that the result set increases super-linearly when k is a relatively large number. For example, the result set covers around 25% more objects than the queried k number when k is equal to 20. This factor has a similar super-linear influence on the query processing time as demonstrated in Figure 7b.

5.2.3 Effect of the Number of POI

To see the effect of varying the total POI number, we increased the total POI number from 200 to 1000 in the simulation environment. Figure 8 illustrates the result set size and query processing time of PSNN and PSRQ with increasing POI numbers. We notice that with a higher POI density the result set of PSRQ increases conspicuously compared with PSNN. This is expected, since PSRQ has to report all the objects inside the cloaked region. In addition, the query processing time of PSNN is always longer than that of PSRQ.

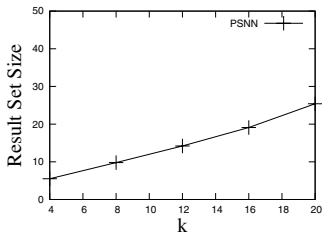


Fig. 7a. Result Set Size.

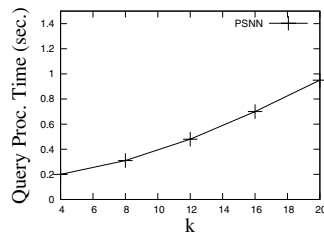


Fig. 7b. Query Proc. Time.

Figure 7. The effect of k .

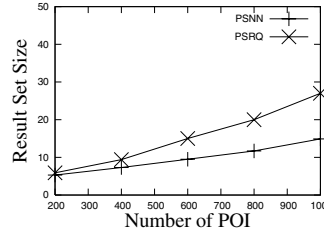


Fig. 8a. Result Set Size.

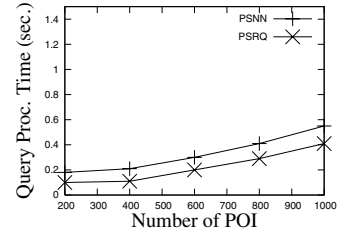


Fig. 8b. Query Proc. Time.

Figure 8. The effect of the POI number.

6 Conclusions

In this paper we propose two novel algorithms for processing k nearest neighbor queries and range queries on spatial networks with privacy protection. The main idea is to hide the exact mobile user location with a cloaked region. The cloaked region covers the query requester and at least $K - 1$ other users based on the K -anonymity concept. The spatial queries are executed based on both the cloaked region and the underlying networks. A candidate result set will be returned to the requesting user who filters out the exact answer. Our comprehensive simulations with real and synthetic parameter sets demonstrate the efficiency of our methods.

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