LASSO and LSTM Integrated Temporal Model for Short-Term Solar Intensity Forecasting

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Abstract—As a special form of the Internet of Things, smart grid is an Internet of both power and information, in which energy management is critical for making the best use of the power from renewable energy resources, such as solar and wind, while efficient energy management is hinged upon precise forecasting of power generation from renewable energy resources. In this paper, we propose a novel least absolute shrinkage and selection operator (LASSO) and long short term memory (LSTM) integrated forecasting model for precise short-term prediction of solar intensity based on meteorological data. It is a fusion of a basic time series model, data clustering, a statistical model, and machine learning. The proposed scheme first clusters data using k-means++. For each cluster, a distinctive forecasting model is then constructed by applying LSTM, which learns the nonlinear relationships and LASSO, which captures the linear relationships within the data. Simulation results with open-source datasets demonstrate the effectiveness and accuracy of the proposed model in short-term forecasting of solar intensity.

Index Terms—Internet of Things (IoT), k-means++, least absolute shrinkage and selection operator (LASSO), long short term memory (LSTM), short-term solar power forecasting.

I. INTRODUCTION

INTERNET of Things (IoT) is defined as uniquely identifiable objects that are organized in an Internet-like structure [1]. The Internet of information, vehicles, power, and energy are all typical forms of IoT. With innovative structure and techniques, IoT promotes the new developments of many traditional industries, and the smart grid (SG) is one of them. As a special form of the IoT, SG is considered as an Internet of both power and information [2]. In recent years, more and more IoT-based technologies have been developed to make SG a more sustainable, economic, safe, and reliable power grid from many aspects [3]–[5]. Among them, energy management is one of the most innovative and important techniques, which can increase the efficiency, reliability, and economy of the SG [6]–[9].

Energy management in the SG is usually based on different timescales, depending on practical constraints and purposes [10]. At the daily scale, day-ahead strategies for power devices and budget for utilities can be developed, according to the day-ahead predictions of daily average power generation and demand, which focus on state estimation and market guidance. At the hourly or minutely scale, the real-time power distribution can be optimized based on predicted power generation and demand updated every hour or several minutes, and the current power storage, which determines the power flows in SG for more reliable, efficient, and economic operation. For both cases, energy management relies on predictions of power generation and demand in the SG [6]. And precise short-term predictions are more important to guarantee the power balance and system reliability, and thus require higher precision. Among the various renewable energy sources, solar power is highly fluctuating, and changes very fast in some cloudy days, making it difficult for accurate short-term forecasting [11]. Therefore, precise short-term prediction of solar power generation is highly demanded to achieve a highly efficient energy management scheme for the SG.

Solar power generation from solar panels are proportional to solar intensity, so it can be estimated by predicting short-term solar intensity [12]. Many recent works focus on applying the time series model (TSM) to predict short-term solar intensity. The work in [13] conducts the short-term prediction of solar radiation using autoregressive integrated moving-average (ARIMA) and time delay neural network (NN). Hejase and Assi [14] proposed a time-series regression model with ARIMA and artificial NN (ANN) to predict solar intensity in the city of Al-Ain, United Arab Emirates. The temporal model works well when the weather is sunny and stable. However, in cloudy, heavily cloudy, rainy, and similar weather conditions, the time series-based methods are not very accurate due to the high variations of solar intensity. Therefore, applying only temporal model is inadequate for further increasing the forecasting accuracy [11].

Machine learning techniques, which can capture the relationships between solar intensity and the meteorological variables, are also popular in forecasting renewable power generation. For example, support vector machine (SVM) is applied in [15], and a method based on ANN is proposed in [16]. Although many machine learning methods can achieve fairly good results [15]–[18], they do not perform a deep
analysis of the data, and thus there is still room for more accurate predictions. We summarize the pros and cons of both time series and machine learning models in solar intensity predictions in Table I.

Recurrent NN (RNN) acquires the output from not only the current input information but also the past experience and input information, which is a good candidate to be integrated into the solar intensity forecasting model. However, when the distance between two cells in the RNN is too large, the vanishing gradient may cause losses of important information [19]. Fortunately, the long short-term memory (LSTM) method successfully solves this vanishing gradient problem by adding three gates: 1) input gate; 2) forget gate; and 3) output gate into the RNN cell [20]. It is thus a suitable method to further increase the forecasting accuracy by capturing the nonlinear relationships between solar intensity and the meteorological variables. On the other hand, there exist both linear and nonlinear relationships in the meteorological data. The linear representation can be captured by a regression method. To this end, the least absolute shrinkage and selection operator (LASSO) is a linear regression analysis method, which reduces over-fitting and enhances the prediction accuracy through variable selection and regularization [1].

Because of the complex and complicated relationships between the solar intensity and meteorological variables, a method integrating time series characteristics, statistical model and machine learning is highly desirable for precise short-term forecasting of solar intensity. By integrating these three methods, we classify the data into several clusters according to the idea of building different specific forecasting models for different weather types. K-means is the most popular clustering method for its computational efficiency [21]. Once the number of clusters is specified, the clustering result could be obtained. However, the randomness of initial sampling (e.g., bad data) affects the clustering results badly. The improved k-means++ solves this sampling problem so that satisfactory clustering results can be obtained [22]. Therefore, we apply k-means++ to cluster the weather data. For each cluster, we start from a basic temporal model because of its strong temporality in short-term prediction of solar intensity. We then apply an integrated forecasting model in each cluster, capturing both temporal and spatial characteristics. The spatial part is further divided into linear and nonlinear parts linked by optimal ratios. This way, the forecasting accuracy can be increased to a very high level.

The main contribution of this paper is to propose an integrated forecasting model for precise short-term predictions of solar intensity. The model architecture is shown in Fig. 1.

It is a fusion of a basic time serial model, data clustering, a statistical model, and machine learning, which is a comprehensive model considering every aspect inside the short-term solar intensity forecasting problem, including strong time correlation, weather complexity, linear, and nonlinear relationships. It generates different forecasting models for every different clusters from the k-means++ output, in which the TSM captures the strong time correlation, LSTM learns the nonlinear relationship, and LASSO represents the linear relationship. Such a comprehensive model guarantees a very high forecasting accuracy of solar intensity, as will be shown in our performance evaluation and comparison study. Furthermore, our model is also applicable to other data-based short-term forecasting problems, such as predicting short-term wind power, loads of the power grid, and so on.

The remainder of this paper is organized as follows. We present the forecasting model construction in Section II. We propose our integrated short-term forecasting model in Section III. Simulation studies are presented in Section IV. Section V concludes this paper and discusses future work.

### II. Forecasting Models

In this section, we first introduce a general temporal model followed by model refinement from error correction. We then propose the integrated temporal model, which is based on the structure shown in Fig. 1.

#### A. Temporal Model

The data of solar intensity is usually recorded for every time interval, which can be represented using a TSM as follows [23]:

\[
Y(t) = f(Y(t - \delta_t), Y(t - 2\delta_t), \ldots) + \epsilon(t)
\]

where \(Y(t)\) is the solar intensity at time \(t\), \(\epsilon(t)\) is the error at time \(t\), and \(f(\cdot)\) is a function which connects the recorded solar intensity data before \(t\) to the present \(Y(t)\), \(\delta_t\) denotes the time interval between two recordings, which is chosen from different timescales according to the practical application. For
short-term predictions, $\delta_i$ is usually less than one hour. To simplify the expression without loss of generality, we use $t - k$ to represent $t - k\delta_i$ in our models, which do not specify $\delta_i$, and thus, (1) is rewritten as

$$Y(t) = f(Y(t - 1), Y(t - 2), \ldots) + \epsilon(t). \quad (2)$$

In the temporal model, time correlation becomes stronger as $\delta_i$ gets smaller, i.e., data collected minutely correlate each other more tightly than data collected hourly, and $Y(t)$ and $Y(t - 1)$ are more closely correlated than $Y(t)$ and $Y(t - 2)$. Based on this, we can further simplify the model for short-term predictions as

$$Y(t) = Y(t - 1) + \epsilon(t). \quad (3)$$

The shorter the $\delta_i$, the smaller the $\epsilon(t)$. Also, this model works well for stable weather conditions, such as sunny days. However, when it is partly cloudy, $\epsilon(t)$ could be large, causing more uncertainties in the model even when $\delta_i$ is chosen to be less than 5 min. Obviously, the model in (3) is not applicable in this case and a more comprehensive model is required.

### B. Model Refinement

In (3), the error term $\epsilon(t)$ is actually the difference between $Y(t)$ and $Y(t-1)$. The major cause of this difference is from the weather condition and weather change, and thus, by relating them to the change of solar intensity, we can refine $\epsilon(t)$ as

$$\epsilon(t) = g(\tilde{X}(t), \tilde{X}(t) - \tilde{X}(t - 1)) + \epsilon_r(t) \quad (4)$$

where $\tilde{X}(t)$ is the vector of meteorological variables at time $t$, such as temperature, humidity, precipitation, etc.; $\tilde{X}(t) - \tilde{X}(t - 1)$ is the change of meteorological variables in $\delta_i$, and $\epsilon_r(t)$ is the remaining error, which is expected to be less than $\epsilon(t)$. Substituting (4) into (3), we have

$$Y(t) = Y(t - 1) + g(\tilde{X}(t), \tilde{X}(t) - \tilde{X}(t - 1)) + \epsilon_r(t) \quad (5)$$

where $g(\cdot)$ is a function connecting $(\tilde{X}(t), \tilde{X}(t) - \tilde{X}(t - 1))$ to $Y(t) - Y(t - 1)$. Here, we choose both $\tilde{X}(t)$ and $\tilde{X}(t) - \tilde{X}(t - 1)$, because the change of solar intensity in any $\delta_i$ may rely on the meteorological condition and change simultaneously. For example, for a sunny day in summer and winter, similar changes of meteorological data may cause very different amount of solar intensity changes. Also, the relationship between $\tilde{X}(t) - \tilde{X}(t-1)$ and $Y(t) - Y(t-1)$ is actually very complicated overall. However, there exist some useful relations, especially for some specific weather types and conditions, which help to further refine the model.

### C. Integrated Temporal Model

Considering both linearity and nonlinearity, the function $g(\cdot)$ is composed as

$$g(\tilde{X}(t), \tilde{X}(t) - \tilde{X}(t - 1)) = (\tilde{X}(t), \tilde{X}(t) - \tilde{X}(t - 1))^T \hat{\beta} + E(\tilde{X}(t), \tilde{X}(t) - \tilde{X}(t - 1)) \quad (6)$$

where the first term is a linear regression model representing the linear part in the data, and $\hat{\beta}$ is the vector of the regression coefficients; the second term is a function $E(\cdot)$ representing the nonlinear part, which is usually revealed by machine learning methods. We then substitute (6) into (5) to obtain a comprehensive integrated temporal model

$$Y(t) = Y(t - 1) + (\tilde{X}(t), \tilde{X}(t) - \tilde{X}(t - 1))^T \hat{\beta} + E(\tilde{X}(t), \tilde{X}(t) - \tilde{X}(t - 1)) + \epsilon_r(t). \quad (7)$$

The corresponding forecasting model is thus written as

$$\hat{Y}(t) = Y(t - 1) + (\tilde{X}(t), \tilde{X}(t) - \tilde{X}(t - 1))^T \hat{\beta} + \hat{E}(\tilde{X}(t), \tilde{X}(t) - \tilde{X}(t - 1)). \quad (8)$$

In order to apply this forecasting model, we need to identify $\hat{\beta}$ and $\hat{E}(\cdot)$. To improve forecasting precision, solution methods are very decisive. As introduced in Section I, LASSO is a good option to get a better estimator $\hat{\beta}$. It is also capable of selecting meteorological variables, which is very useful to reduce the computational complexity. As for $\hat{E}(\cdot)$, LSTM is a good choice for learning the nonlinear relationship. Moreover, linearity and nonlinearity have different weights in different weather types. For example, in sunny days, linear relationship is the leading factor, while in cloudy days, nonlinearity takes bigger role. So the weights allocated to them need to be carefully selected for different weather types. To solve the above problem, we propose the LASSO and LSTM integrated forecasting algorithm (LLIFA) in Section III.

### D. Model Characteristics

Before proceeding to the algorithm, it is necessary to examine the statistical characteristics of the forecasting model with respect to unbiasedness, consisting, efficiency, and sufficiency. However, since the proposed model (8) is an integration of statistical and machine learning methods, we cannot evaluate the model directly through statistical tests. Actually, the integrated model takes into account all the four characteristics. Here, we further analyze the model to show how these characteristics can be achieved.

In the meteorological data-based short-term solar intensity forecasting problem, it is very difficult to find an unbiased estimator or predictor, if such estimator exists. This is because the relationships between solar intensity and the meteorological data are very complex and complicated, including linearity, nonlinearity, time correlation, and others. Because of this, the proposed model originates from a simple TSM (3), which is actually a first order auto-regressive model AR(1) of the parameter as 1. It is a nonstationary process and thus the error $\epsilon(t)$ is not white noise. In order to further reduce the bias of the model, we thus refine the error by (4).

In our forecasting model (7), data is partitioned into several clusters. Then for each cluster, we identify $\hat{\beta}$ and $\hat{E}(\cdot)$ to apply the forecasting model. When the data size is approaching infinite, the error $\epsilon_r(t)$ is approaching zero; because of clustering, $\hat{\beta}$ and $\hat{E}(\cdot)$ become more accurate. Theoretically, machine learning methods are able to capture any relationship, and the more data it learns, the better the model is. From this aspect, the proposed predictor is consisting.

Normal solar intensity prediction performance in fast changing weather conditions are worse than that in sunny weather.
other words, the efficiency of a forecasting model depends mainly on the prediction performance in fast changing weathers. Because of this, we cluster the data into several groups so that a specific model is generated for each group to improve accuracy. This way, the overall performance is improved, and thus, the model efficiency is increased correspondingly.

To guarantee the sufficiency of the model, we make full use of the dataset and partition the dataset into training data, evaluation data, and testing data.

In summary, the integrated temporal model actually takes into account of all the four aspects, i.e., unbiasedness, consistency, efficiency, and sufficiency. Since theoretic analysis of the characteristics of an estimator is important but very difficult, it has to be replaced with quantitative simulations. We will evaluate the model characteristics through simulations in Section IV.

III. LASSO AND LSTM INTEGRATED ALGORITHM

In this section, we first present LASSO and LSTM and discuss their parameter selection. We then present the method to combine them together. Then, we propose the integrated algorithm for short-time solar intensity forecasting.

A. Least Absolute Shrinkage and Selection Operator

Let \( Y_1(t) \) denote \((\bar{X}(t), \bar{X}(t) - \bar{X}(t-1))^T \hat{\beta} \), i.e., the linear part in (7), and the predicted \( Y_1(t) \) is written as
\[
\tilde{Y}_1(t) = (\bar{X}(t), \bar{X}(t) - \bar{X}(t-1))^T \hat{\beta}
\]
where \( \tilde{Y}_1(t) \) is considered as the linear portion of the predicted changes of the solar intensity from \( t-1 \) to \( t \). Because of its shrinkage function and parameters’ selection, LASSO is used here to identify the estimated coefficients \( \hat{\beta} \) as
\[
\hat{\beta} = \text{argmin}_{\beta} \left\{ \sum_{i=1}^{N} \left( y_i - \beta_0 - \sum_{j=1}^{p} x_{ij} \beta_j \right)^2 + \lambda \sum_{j=1}^{p} |\beta_j| \right\}
\]
where \( \lambda \) is a system parameter. LASSO is able to shrink large regression coefficients in order to reduce over-fitting by the constraint of the sum of the absolute value of the regression coefficients smaller than a fixed value, which filters out some coefficients, and thus effectively simplifies the model.

To acquire a fitted system parameter \( \lambda \), two methods are commonly used: cross validation [24] and regularization path [25]. Cross validation is a very general and common technique finding an optimal parameter. Its weakness is the slow computation. Regularization path is able to achieve a good estimation accuracy with fairly quick computation. It also has the potential to achieve a high estimation accuracy even when information is lacking. Thus, we use the regularization path to obtain \( \lambda \) based on the following steps.

1) Choose a set of possible \( \lambda \)s and sort them in ascending order.
2) Execute the proposed algorithm for each \( \lambda \) and record their performance.
3) Plot the achieved precision performance versus \( \lambda \).

4) Choose an acceptable point on the curve to guarantee the performance while achieving the maximized estimation speed due to sparsity.

B. Long Short Term Memory

For the nonlinearity representing function \( E(\cdot) \) in the model of (7), a specific machine learning method is required to learn it from the meteorological data and change of solar intensity. For simplification, we use \( Y_2(t) \) to denote the nonlinear part in (7), and thus we can write the predicted \( Y_2(t) \) as
\[
\tilde{Y}_2(t) = \hat{E}(\bar{X}(t), \bar{X}(t) - \bar{X}(t-1))
\]
where \( \tilde{Y}_2(t) \) is the output of the function acquired by the learning method.

NN is a common method to capture the nonlinear relationship in a complex dataset. RNN is an improved NN, which is able to combine both the current and previous information to find solutions. However, it is very difficult to obtain useful information if two RNN cells are far away from each other, due to the gradient vanishing problem. To address this issue, LSTM incorporates three gates into the RNN cell, as shown in Fig. 2. Each cell of LSTM sends two state variables to the next cell, which ensures the reliability of information transmission and thus avoids gradient vanishing. Moreover, the results from LSTM are highly repeatable [26]. Because of the above advantages, we apply LSTM to acquire a precise \( Y_2(t) \).

Here, LSTM is used to generate the classification network and regression network, for classifying evaluation and prediction data, and learning nonlinear characteristics, respectively. Both the two networks have three major steps. The first two steps are feature extraction and the LSTM network, respectively. The third step is softmax classifier for the classification network, and a NN for the regression network [27], [28].

1) Feature Extraction: For better feature extraction, we implement one fully connected layer with ReLU(·) as the activation function, which is given as
\[
z_t = \text{ReLU}(Wz_{t-1} + b)
\]
where \( x_t \) and \( z_t \) are the input and output of the fully connected layers, respectively, \( W \) and \( b \) are the weights and biases of the layers. The activation function is formulated as \( \text{ReLU}(\cdot) = \max(x, 0) \). The ReLU(\( x \)) function has several advantages, such

Fig. 2. Structure of LSTM.
as sparse representation, efficient gradient propagation, and computation.

2) LSTM Network: After feature extraction, we use the LSTM for training optimal weights. For the classification LSTM network, we stack two layers of the LSTM network to obtain a stronger learning ability, which improves the performance of classification and regression.

3) Softmax Classifier: The output of the final cell’s hidden state in the classification LSTM network is the input to a fully connected layer, which trains the output data using the softmax classifier. The softmax function maps the $N$ dimensional vector to normalized data $p = [p_1, p_2, \ldots, p_N]$, and

$$p_i = \frac{e^{h_i}}{\sum_{j=1}^{N} e^{h_j}}, \quad \text{for } i = 1, 2, \ldots, N$$

(13)

where $N$ is the number of training data, $h_i$ is the output vector of the final cell’s hidden state in the LSTM network, and $\omega_i$ is the weight vector of the fully connected layer. Let $L(t)$ be the loss function, which is formulated as

$$L(t) = \frac{1}{2} \sum_{i=1}^{N} (p_i - y_i)^2$$

(14)

where $y_i$ is the true classification result for the $i$th training data. We then use back propagation through time and real-time recurrent learning to train the classification LSTM networks [29]. We also use the Adam optimizer to improve the efficiency of optimization.

C. Data Clustering by K-Means++

By LASSO and LSTM, we can use (8) to make predictions given any dataset. Based on the complete historical data, however, only one forecasting model will be constructed, which is too general to adapt to various weather conditions. Therefore, we need to cluster the data, and build a specific model for each cluster.

K-means++ clustering is a commonly used method, which selects $k$ initial center points arbitrarily and clusters the data according to the distances from each data point to the centers. Its simple principle makes it suitable for fast computation for many applications, although it is sometimes difficult to get suitable number of $k$ [30]. Here, we go through all possible $k$s in the specified range. To overcome the shortcoming of random selection of initial center points, which may lead to bad clustering performance, k-means++ applies the $d^2$-sampling method [22] with the following procedure.

1) Select the first center point randomly.
2) Calculate the probability of selecting the next center by

$$p(x|C) = \frac{d(x, C)^2}{\sum_{x' \in X} d(x', C)^2}$$

(15)

where $X$ represents a set of $n$ points in $\mathbb{R}^D$, $D$ is the dimension of $X$, $x$ denotes a point in $X$, $C$ is the set of center points and $c$ is a selected center point, $x'$ denotes the other points in set $X$ except for $x$, and the function $d(x, C)^2$ is defined as $d(x, C)^2 = \Sigma_{c \in C} \| x - c \|^2$.

This way, the selected center points are far from each other with a high probability, and thus k-means++ is suitable for clustering the meteorological data. Therefore, we first cluster the data, and then find the forecasting model for each cluster.

D. LASSO and LSTM Integrated Forecasting Algorithm

We now propose the LLIFA for short-term solar intensity forecasting. Let $S = \{\tilde{X}(t), \tilde{Y}(t)\}$ represent the dataset of meteorological and solar intensity. We first divide it into two subsets: 1) the training set $T = \{\tilde{X}(t), \tilde{Y}(t)\}_T$ and 2) the evaluation set $E = \{\tilde{X}(t), \tilde{Y}(t)\}_E$, where $T \cup E = S$ and $T \cap E = \emptyset$. Then, we cluster the training set $T$ into $N$ groups of data, and each group is denoted as $T_k = \{\tilde{X}(t), \tilde{Y}(t)\}_{T_k}$, where $k = 1, 2, \ldots, N$. According to (6), the input variable for the k-means++ clustering is the vector $[\tilde{X}(t), \tilde{X}(t) - \tilde{X}(t-1)]$ in $T$. $T_k$ is then divided into two parts: 1) the input vector $\tilde{X}_{T_k} = [\tilde{X}(t), \tilde{X}(t) - \tilde{X}(t-1)]_{T_k}$ and 2) the output vector $\tilde{Y}_{T_k} = \tilde{Y}(t) - \tilde{Y}(t-1)$ for training. We next divide each training output $\tilde{Y}_{T_k}$ into the linear part $\tilde{Y}_{1,T_k}$ and the nonlinear part $\tilde{Y}_{2,T_k}$

$$\tilde{Y}_{1,T_k} = \tilde{Y}_{T_k} \cdot 1/(1 + \alpha_k)$$

(16)

$$\tilde{Y}_{2,T_k} = \tilde{Y}_{T_k} \cdot \alpha_k/(1 + \alpha_k)$$

(17)

where $\alpha_k$ is a positive ratio coefficient in the $k$th cluster. $\alpha_k$ is set to different values in different clusters, to adjust the weights of $\tilde{Y}_{1,T_k}$ and $\tilde{Y}_{2,T_k}$ in the forecasting model. Given $\alpha_k$s, we can solve for the regression coefficients $\tilde{\beta}$ and the function $\tilde{E}(\cdot)$ using LASSO and LSTM, respectively, to determine the forecasting model for each cluster. It is thus important to search for the optimal $\alpha_k$s, as evaluated by the set $E$.

First, we need to classify $E$ into $N$ clusters according to the classification standard in $T$. However, k-means++ does not produce the same classification results, because $T$ and $E$ are different. So we use LSTM to learn the classification net classnet in $T$. Through classnet, $E$ can be clustered under the same rule into $N$ clusters, denoted as $E_k = \{\tilde{X}(t), \tilde{Y}(t)\}_{E_k}$, where $k = 1, 2, \ldots, N$. Based on this, we can perform the traversing method to obtain the optimal $\alpha_k$s. Considering both (16) and (17), $\alpha_k$s are limited in $\alpha_k \in [\alpha_{\min}, \alpha_{\max}]$, which is determined according to the dataset. $\alpha_{k,j}$ gradually increases from $\alpha_{k,0} = \alpha_{\min}$ to $\alpha_{k,j} = \alpha_{\max}$ by an increment $d_a$, where $j = 0, 1, \ldots, J$, and $J = \lfloor(\alpha_{\max} - \alpha_{\min})/d_a \rfloor$. For every $\alpha_{k,j}$, the corresponding $\tilde{\beta}_{k,j}$ and the function $\tilde{E}_{k,j}(\cdot)$ are generated. According to (8), (9), and (11), the predicted $\tilde{Y}_{E_k}(t)$ can be found for every solar intensity in every evaluation cluster $E_k$. So under $\alpha_{k,j}$, we can calculate the sum of errors for each cluster by

$$e_{\alpha_{k,j}} = \frac{1}{J} \sum_{j=1}^{J} |\tilde{Y}_{E_k}(t) - \tilde{Y}_{E_k}(t)|$$

(18)

and then acquire the optimal $\tilde{\alpha}_k$ by

$$\tilde{\alpha}_k = \arg\min_{\alpha_{k,j}} \{e_{\alpha_{k,j}}\}.$$  

(19)

This way, we are able to obtain the optimal ratio coefficients, the corresponding regression coefficients, the nonlinear function, and thus the forecasting model of each cluster. We summarize the steps to acquire $\tilde{\alpha}_k$s in Algorithm 1.

To predict the solar intensity for a future time $t$, new input data is first classified into an appropriate cluster through the
classnet, then the solar intensity can be predicted based on the corresponding model of that cluster. We summarize the procedure to perform LLIFA in Algorithm 2, which is a fusion of LASSO and LSTM through $k$-means++ clustering. Note that to make sure the forecasting model for every cluster is precise, it needs to guarantee both the training dataset $T$ and the evaluation dataset $E$ are sufficiently large, so that the ratio coefficients in each forecasting model is significant. Also, we divide the training and evaluation data before clustering them separately, because the training data, and thus the choices of the ratio coefficients are more appropriate.

### IV. Simulation Studies

In this section, we verify our proposed forecasting model and algorithms on two trace-driven datasets, and compare the performance with other benchmarks. The simulation results show that the proposed forecasting model achieves outstanding performance for different datasets under different timescales, and outperforms other benchmarks.

#### A. Data Description

The first trace-driven dataset is acquired from the Davis weather station located in Amherst, MA, USA [31]. The meteorological data was collected every 5 min. The main recorded weather variables, including temperature, wind chill, humidity, dew-point, wind speed, wind direction, and rainfall. The dataset is recorded from February 2006 to January 2013, which also contains some missing data and errors, recorded as $-100\,000$. In the simulation study, we excluded such errors and missing data. Moreover, we only consider the solar intensity on the day time when the solar intensity is nonzero, so the data of which the solar intensity is zero is also excluded. For short-term solar intensity forecasting, we mainly use the data from January 1, 2011 to February 28, 2013. We divide the data into three subsets: 1) training; 2) evaluation; and 3) testing data. The data from January 1, 2011 to December 31, 2012 is departed every other day into training data and evaluation data separately. This generates almost the same size of training and evaluation data, ensuring both datasets are large enough to get precise forecasting models for all clusters. The remaining data from January 1, 2013 to February 28, 2013 are taken as testing data.

The second dataset is recorded in Harhill and Diddington in the U.K. [32]. At each location, two weather stations are installed (four in total), which recorded every 30 min the data of rainfall, temperature, humidity, wind speed, and so on. We use this the data recorded from August 2011 to December 2012. Missing data in datasets are represented by NaN. By excluding such invalid data, the remaining useful data are separated into the training, evaluation, and testing data as same as the first dataset. The data from August 1, 2011 to September 30, 2012 is departed every other day into training data and evaluation data, respectively. The remaining data are taken as testing data. Note that this data has a longer recording time interval than the first one, which helps us to evaluate the proposed forecasting model under different timescales.

#### B. Model Improvement With Data Analysis

We first use three fundamental models and their combinations to analyze the data and model characteristics in short-term solar intensity forecasting. According to Section II, we apply the following models to predict solar intensity every 5 min:

\[
\tilde{Y}(t) = Y(t - 1)
\]

\[
\tilde{Y}(t) = (\tilde{X}(t), \tilde{X}(t) - \tilde{X}(t - 1))^T \vec{\tilde{\beta}}_o
\]

\[
\tilde{Y}(t) = \tilde{E}_m(\tilde{X}(t), \tilde{X}(t) - \tilde{X}(t - 1))
\]

\[
\tilde{Y}(t) = Y(t - 1) + (\tilde{X}(t), \tilde{X}(t) - \tilde{X}(t - 1))^T \vec{\tilde{\beta}}_m
\]

\[
\tilde{Y}(t) = Y(t - 1) + \tilde{E}_m(\tilde{X}(t), \tilde{X}(t) - \tilde{X}(t - 1))
\]

where (20) is a short-term TSM, (21) and (22) are based on LASSO and LSTM, respectively, (23) is an integrated model combining TSM and LASSO, and (24) is another integrated model combining TSM and LSTM. Based on the UMASS dataset of 2011 and 2012, we find $\vec{\beta}_o$, $\vec{\beta}_m$, $\tilde{E}_m(\cdot)$, and $\tilde{E}_m(\cdot)$, and use the above five models to predict the solar intensity every 5 min for the first two months in 2013.
both mean absolute percentage error (MAPE) and root mean square error (RMSE) to measure the accuracy of the forecasting models, which are summarized in Table II. We also plot the predicted solar intensity for February 8, February 19, and January 25 based on three single models of TSM, LASSO, and LSTM from Figs. 3–11. These three days represent three different weathers: 1) stable; 2) fluctuating; and 3) fast changing.

From Table II, we have several observations. Among the first three models, TSM achieves much better results than LASSO and LSTM, while LASSO has the worst performance whatever the weather is. This is because the temporal correlation is very strong between the meteorological data and solar intensity. LASSO has poor performance shown also in Figs. 6–8, because the linear relationship in the data under short time period is weaker than that under longer timescale, such as daily or weekly. LSTM has better performance than LASSO because of its capability at learning and capturing strong time correlations in the data.

On the other hand, comparing the forecasting results between the integrated models and the first three ones, we find that both LSTM and LASSO can increase the predicting accuracy of TSM. For three days shown in Table II, comparing with TSM, the RMSEs decrease by 5.31%, 2.85%, and 2.58% respectively, under TSM-LASSO, and decrease by 24.48%, 41.89%, and 68.47%, respectively, under TSM-LSTM. Note that the improvement of LSTM and LASSO on TSM differs
for different weathers. LASSO can be a good assistant in stable days, while LSTM is good for cloudy days. They complement each other in assisting TSM. Based on these observations and analyzes, we propose the LLIFA by deep fusion of LSTM and LASSO into TSM. And we notice that in different weathers, LSTM and LASSO have different performance, based on which, we cluster the data, find the regression coefficients for LASSO, train the function for LSTM and allocate their weights in the corresponding forecasting models.

C. Performance Evaluation of LLIFA

By applying LLIFA proposed in Section III-D, we need to cluster the data into an optimal number of subsets. We cluster the data into different numbers and calculate the forecasting errors for every cluster. We plot in Fig. 12 the forecasting errors for the three typical days February 8, February 19, and January 25 under different number of clusters. Predictions on other days have the same trend. It shows the forecasting errors for all three days are minimized in 11 clusters. Fig. 12 indicates that when the clustering number is either too small or too large, the forecasting performance is poor. This is because given the same dataset, increasing the number of clusters reduces the amount of data in each cluster, which correspondingly reduces the accuracy of the models. On the other hand, a small number of clusters are not sufficient to capture the essential information in the complex weather data and thus cause large forecasting errors. We therefore set $N = 11$.

According to Algorithm 2, we use $k$-means++ to cluster the data into 11 clusters. For each cluster, we obtain a corresponding forecasting model which is used to predict the solar intensity. By comparisons, we build another model in the form of (8) without clustering. We compare the average forecasting errors in each cluster with that without clustering in Figs. 13 and 14. It can be seen that in every cluster, the forecasting error reduces much from no clustering, which verifies the effectiveness and importance of the clustering.

We plot the forecasting results of LLIFA for February 8, February 19, and January 25 in Figs. 15–17, respectively. The RMSEs and MAPEs for these three days are $7.83 \text{ watt/m}^2$, $5.16 \text{ watt/m}^2$, and $3.86 \text{ watt/m}^2$. The forecasting errors of three days under different clusters are shown in Table II. For every cluster, the forecasting error decreases much from no clustering, which verifies the effectiveness and importance of clustering.

<table>
<thead>
<tr>
<th>Date</th>
<th>Feb. 8</th>
<th>Feb. 19</th>
<th>Jan. 25</th>
</tr>
</thead>
<tbody>
<tr>
<td>TSM MAPE</td>
<td>11.48</td>
<td>34.16</td>
<td>51.92</td>
</tr>
<tr>
<td>TSM RMSE</td>
<td>7.58</td>
<td>13.63</td>
<td>29.06</td>
</tr>
<tr>
<td>LASSO MAPE</td>
<td>221.37</td>
<td>159.62</td>
<td>208.12</td>
</tr>
<tr>
<td>LASSO RMSE</td>
<td>448.14</td>
<td>448.42</td>
<td>467.63</td>
</tr>
<tr>
<td>LSTM MAPE</td>
<td>75.02</td>
<td>81.81</td>
<td>66.28</td>
</tr>
<tr>
<td>LSTM RMSE</td>
<td>37.66</td>
<td>59.55</td>
<td>96.58</td>
</tr>
<tr>
<td>TSM-LASSO MAPE</td>
<td>10.87</td>
<td>33.19</td>
<td>50.58</td>
</tr>
<tr>
<td>TSM-LASSO RMSE</td>
<td>5.63</td>
<td>12.23</td>
<td>28.49</td>
</tr>
<tr>
<td>TSM-LSTM MAPE</td>
<td>8.67</td>
<td>19.85</td>
<td>16.37</td>
</tr>
<tr>
<td>TSM-LSTM RMSE</td>
<td>3.86</td>
<td>7.04</td>
<td>11.76</td>
</tr>
</tbody>
</table>
2.81%, 15.53 watt/m², 5.81%, 13.31 watt/m², 9.83%, respectively, summarized in Table III. Note that in Fig. 17, the proposed LLIFA achieves the average MAPE of only 9.83% in forecasting the solar intensity every 5 min even in fluctuating or fast changing weathers. For stable sunny day, the predictions are very precise with MAPE as small as 3% in Fig. 15.

D. Comparisons of LLIFA to the Benchmarks

We now compare our proposed LLIFA scheme with a commonly used time series method ARIMA and a representative supervised learning method SVM. As a typical TSM, ARIMA can transform any nonstationary process into a stationary process through the differential time series. Solar intensity is actually a nonstationary time series, and thus ARIMA is applicable in solar intensity forecasting, especially in sunny and stable weather. On the other hand, SVM is a representative and widely adaptable machine learning method, which generates very good results in many application scenarios, when the optimal parameters are used. For example, SVM is applied in [15] for solar intensity forecasting. Therefore, we compare our model with ARIMA and SVM in our comparison studies.

Predictions are made every 5 min for the first two months in 2013 using UMASS weather data. The 5-min mean and median RMSEs and MAPEs for LLIFA, ARIMA, and SVM are summarized in Table IV. The predicting results show that LLIFA outperforms ARIMA and SVM with averaged MAPE 4.73% and median MAPE 3.16%. ARIMA has fairly good performance which is much better than SVM, because ARIMA
TABLE III
5-min Forecasting Errors on MAPE (%) and RMSE (watts/m²) by LLIFA for Three Typical Days with UMASS Data

<table>
<thead>
<tr>
<th>Date</th>
<th>Feb. 8</th>
<th>Feb. 19</th>
<th>Jan. 25</th>
</tr>
</thead>
<tbody>
<tr>
<td>RMSE</td>
<td>7.83</td>
<td>15.53</td>
<td>13.31</td>
</tr>
<tr>
<td>MAPE</td>
<td>2.81</td>
<td>5.81</td>
<td>9.83</td>
</tr>
</tbody>
</table>

TABLE IV
Mean & Median Value of MAPEs (%) and RMSEs (watts/m²) for 5-min Predictions with Three Models from January 1 to February 28

<table>
<thead>
<tr>
<th>Model</th>
<th>RMSE Mean</th>
<th>MAPE Mean</th>
<th>RMSE Median</th>
<th>MAPE Median</th>
</tr>
</thead>
<tbody>
<tr>
<td>LLIFA</td>
<td>10.67</td>
<td>4.73</td>
<td>8.34</td>
<td>3.16</td>
</tr>
<tr>
<td>ARIMA</td>
<td>19.42</td>
<td>9.94</td>
<td>15.27</td>
<td>7.29</td>
</tr>
<tr>
<td>SVM</td>
<td>79.04</td>
<td>67.52</td>
<td>76.89</td>
<td>58.65</td>
</tr>
</tbody>
</table>

is good at modeling the short-term temporal relationship [13] while SVM lacks a deep analysis of the complex and complicated weather data, by simply trying different kernels [15]. LSTM works better than SVM with its stronger temporal learning capability. The results verify again the strong time correlation in the short-term forecasting problem. LLIFA fully considers the strong temporality and integrates both statistical regression and machine learning methods, so it has better forecasting performance.

E. Predicting Performance of LLIFA on Longer Recording Time Scale

Next we test LLIFA on another trace-driven data in Diddington by forecasting the solar intensity every 30 min. This time, we cluster the data into $N = 10$ groups by checking the data with the same process as previous. We also select three typical days: 1) stable; 2) fluctuating; and 3) fast changing, and plot the corresponding forecasting results in Figs. 18–20, respectively. The predictions using only LSTM are also plotted as a comparison. And the forecasting errors are summarized in Table V. Note that these three days are clustered into Cluster 6, 2, and 8, respectively.

In a typical sunny day, LLIFA has very precise predictions, tracking the actual observations closely. The RMSE and MAPE in Fig. 18 are 22.32 watts/m² and 9.85%, respectively. It can be found from Figs. 19 and 20 that in fluctuating and fast changing weathers, the predicting performance of LLIFA is not ideal. The MAPEs are 14.94% and 21.18%, respectively. This shows that when the weather changes fast, i.e., data index 19 to 23 in Fig. 19, and data index 15 to 23 in Fig. 20, LLIFA has bad performance, although it still works better than LSTM. This is same as the result from the previous UMASS data. In summary, it is most difficult to predict the solar intensity in fast changing weathers.

By comparing Table V with Table III, we could also find that LLIFA predicts better with the UMASS data than the Diddington data. This is because when the time interval of data recordings increases, the time correlation decreases and thus the forecasting precision of LLIFA decreases. In summary, LLIFA works great in short-term solar intensity forecasting...
especially in stable weathers. However, when the time interval between data recordings increases, the forecasting accuracy is getting down. However, LLIFA could still beat other methods because it integrates temporal model, clustering, statistical model and machine learning.

F. Evaluations on Model Characteristics

Finally, we sum up the errors between the actual solar intensity and the predictions using the proposed model for three different datasets of the two traces. The results are summarized in Table VI. For both UMASS and Diddington traces, the sum of predicting errors for three datasets are all very close to zero, indicating the proposed model is close to be unbiased. Unbiasedness appears more obviously in the UMASS trace, indicating the proposed model is close to be unbiased. Also, as timescale increases. So it may not be suitable for predicting solar intensity on longer timescales. Our future work is to propose an accurate general forecasting model which can predict the solar intensity precisely on different timescales.

REFERENCES


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