

Force analysis via dyads

{AB → 0.14, AC → 0.06, CF → 0.25, h → 0.01, d → 0.01, hSlider → 0.02, wSlider → 0.05,
ro → 8000, g → 9.807, Me → 1000., phi[t] → 1.0472, phi'[t] → 52.3599, phi''[t] → 0}

Inertia forces and moments

Link 1

$m_1 = \rho \cdot AB \cdot h \cdot d = 0.112$ [kg]

$IC_1 = m_1 (AB^2 + h^2) / 12 = 0.000183867$ [kg m²]

$F_{in1} = -m_1 \cdot a_{C1} = \{10.7469, 18.6142, 0\}$ [N]

$F_1 = F_{in1} + G_1 = \{10.7469, 17.5158, 0\}$ [N]

$M_{in1} = M_1 = -IC_1 \cdot \alpha_{10} = \{0, 0, 0\}$ [N m]

Link 2

$m_2 = \rho \cdot hSlider \cdot wSlider \cdot d = 0.08$ [kg]

$IC_2 = m_2 (hSlider^2 + wSlider^2) / 12 = 0.0000193333$ [kg m²]

$F_{in2} = -m_2 \cdot a_{C2} = \{15.3527, 26.5917, 0\}$ [N]

$F_2 = F_{in2} + G_2 = \{15.3527, 25.8071, 0\}$ [N]

$M_{in2} = M_2 = -IC_2 \cdot \alpha_{20} = \{0, 0, -0.0475952\}$ [N m]

Link 3

$m_3 = \rho \cdot CF \cdot h \cdot d = 0.2$ [kg]

$IC_3 = m_3 (CF^2 + h^2) / 12 = 0.00104333$ [kg m²]

$F_{in3} = -m_3 \cdot a_{C3} = \{145.238, 45.2941, 0\}$ [N]

$F_3 = F_{in3} + G_3 = \{145.238, 43.3327, 0\}$ [N]

$M_{in3} = M_3 = -IC_3 \cdot \alpha_{30} = \{0, 0, -2.5685\}$ [N m]

$M_{3e} = -\text{Sign}[\omega_2] \{0, 0, M_e\} = \{0, 0, -1000.\}$ [N m]

Joint reactions

Dyad: B_R, B_T, C_R

Sum F for 2 & 3: $F_{03} + F_3 + F_2 + F_{12} = 0$

(x): $160.591 + F_{03x} + F_{12x} = 0$ (1)

(y): $69.1398 + F_{03y} + F_{12y} = 0$ (2)

Sum M for 2 & 3 wrt B: $r_{BC} \times F_{03} + r_{BC3} \times F_3 + M_3 + M_{3e} + M_2 = 0$

(z): $-1004.63 + 0.0612436 F_{03x} - 0.07 F_{03y} = 0$ (3)

Sum F for 3 projected upon BC: $(F_{03} + F_3) \cdot r_{BC} = 0$

$-0.07 (145.238 + F_{03x}) - 0.0612436 (43.3327 + F_{03y}) = 0$ (4)

From Eqs. (1) (2) (3) (4) => F03x, F03y, F12x, F12y

$$F03 = \{F03x, F03y, 0\} = \{7008.6, -8220.01, 0\} \text{ [N]}$$

$$F12 = \{F12x, F12y, 0\} = \{-7169.19, 8150.87, 0\} \text{ [N]}$$

Link 2

$$\text{Sum F for 2: } F32 + F2 + F12 = 0 \Leftrightarrow F32 = -F2 - F12$$

$$F32 = \{7153.84, -8176.68, 0\} \text{ [N]}$$

point Q is on BC: $(y_B - y_C) / (x_B - x_C) = (y_Q - y_C) / (x_Q - x_C) \Rightarrow$

$$0.874908 - \frac{-0.06 + y_Q}{x_Q} = 0 \quad (5)$$

$$\text{Sum M for 2 wrt B: } r_{BQ} \times F32 + M2 = 0$$

$$(z): 1439.68 - 8176.68 x_Q - 7153.84 y_Q = 0 \quad (6)$$

From Eqs. (5) (6) => xQ, yQ

$$rQ = \{x_Q, y_Q, 0\} = \{0.0699967, 0.121241, 0\} \text{ [m]}$$

Link 1

$$\text{Sum F for link 1: } F1 + F21 + F01 = 0 \Leftrightarrow F01 = -F21 - F1$$

$$F01 = \{-7179.94, 8133.35, 0\} \text{ [N]}$$

$$\text{Sum M for 1 wrt C1: } C1B \times F21 + C1A \times F01 + M1 + Mm = 0 \Leftrightarrow$$

$$Mm = - (C1B \times F21 + C1A \times F01 + M1)$$

$$Mm = \{0., 0., 1439.82\} \text{ [Nm]}$$