# Terrain-based Vehicle Localization to Obtain GPS-Equivalent Vehicle Position Accuracy

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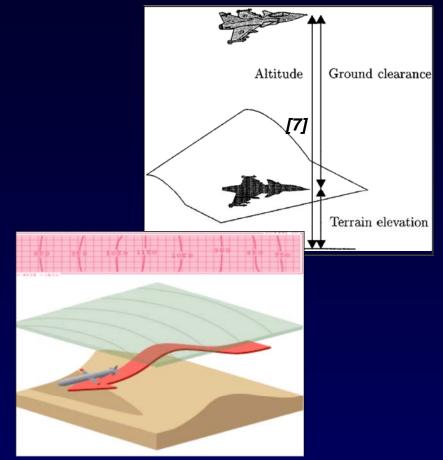
# **Outline of Task 3**

- Past work
  - Motivation for using terrain maps to localize a vehicle
  - Feasibility of location-based road "fingerprints"
  - Framing localization as a nonlinear particle-filter correlation problem
  - Attacking the nonlinear problem with a Kalman approach
  - Hybridizing the method to have the advantages of both the linear/nonlinear approaches
- Task 3 items
  - Vehicle integration, data collection
  - Accuracy reduction including vehicle and maps
  - Integration of terrain-based localization with existing vehicle localization architectures.
  - Large road network testing



## **Terrain-Based Localization**

- Terrain contour matching (TERCOM) was the pre-GPS guidance method for:
  - Missiles
  - Aircraft
  - Underwater systems
    - J. P. Golden, "Terrain contour matching/TERCOM/- A cruise missile guidance aid," *Image processing for missile guidance*, pp. 10–18, 1980.
    - F. Gustafsson, F. Gunnarsson, N. Bergman, U. Forssell, J. Jansson, R. Karlsson, and P. J. Nordlund, "Particle filters for positioning, navigation, and tracking," *Signal Processing, IEEE Transactions on*, vol. 50, no. 2, pp. 425–437, Feb. 2002.
    - A. Bachmann and S.B. Williams. Terrain aided underwater navigation–A deeper insight into generic Monte Carlo localization. In Australasian Conference on Robotics and Automation, pages 1–7, 2003.



http://www.bbc.co.uk/portuguese/especial/2001/ eua\_military\_hardware/cruise\_missile/3.shtml



## **Vehicle terrain-based localization**

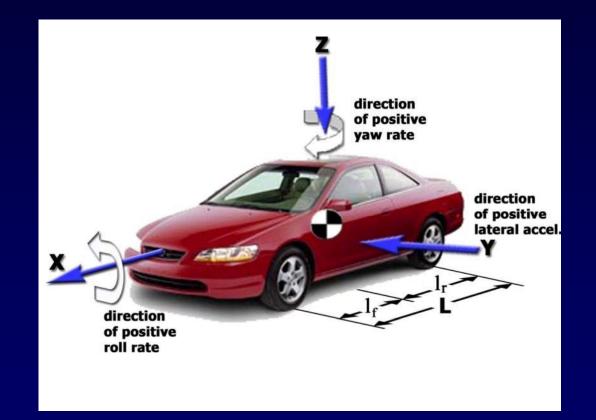
- Matching steering inputs to maps
  - M. E. E. Najjar and P. Bonnifait, "A road-matching method for precise vehicle localization using belief theory and kalman filtering," Auton. Robots, vol. 19, no. 2, pp. 173–191, 2005.
- Matching pressure changes to maps (!)
  - W. Holzapfel, M. Sofsky, and U. Neuschaefer-Rube. Road profile recognition for autonomous car navigation and Navstar GPS support. Aerospace and Electronic Systems, IEEE Transactions on, 39(1):2–12, 2003.
- Both subject to HUGE errors (+/- 1 km!)



# An accidental discovery while examining sideslip during previous work...

# Some terminology to get started...

Standard SAE sign convention





# **Analytical Vehicle Models**

• Model 1 – 2DOF Bicycle Model

$$q = \begin{bmatrix} y \\ \psi \\ \phi \end{bmatrix}$$

$$\begin{bmatrix} -m & 0 & 0 \\ 0 & -I_{zz} & 0 \\ 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} \dot{V} \\ \dot{r} \\ \dot{\phi} \end{bmatrix} + \begin{bmatrix} 0 & -mU & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} V \\ r \\ \dot{\phi} \end{bmatrix} + \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} y \\ \psi \\ \phi \end{bmatrix} = \begin{bmatrix} 2 & 2 \\ 2l_f & -2l_r \\ 0 & 0 \end{bmatrix} \begin{bmatrix} F_f \\ F_r \end{bmatrix}$$
$$\begin{bmatrix} F_f \\ F_r \end{bmatrix} = \begin{bmatrix} -\frac{C_f}{U} & -\frac{l_f C_f}{U} & 0 \\ -\frac{C_r}{U} & \frac{l_r C_r}{U} & 0 \end{bmatrix} \begin{bmatrix} V \\ r \\ \phi \end{bmatrix} + \begin{bmatrix} C_f \\ 0 \end{bmatrix} \delta_f$$



# **Analytical Vehicle Models**

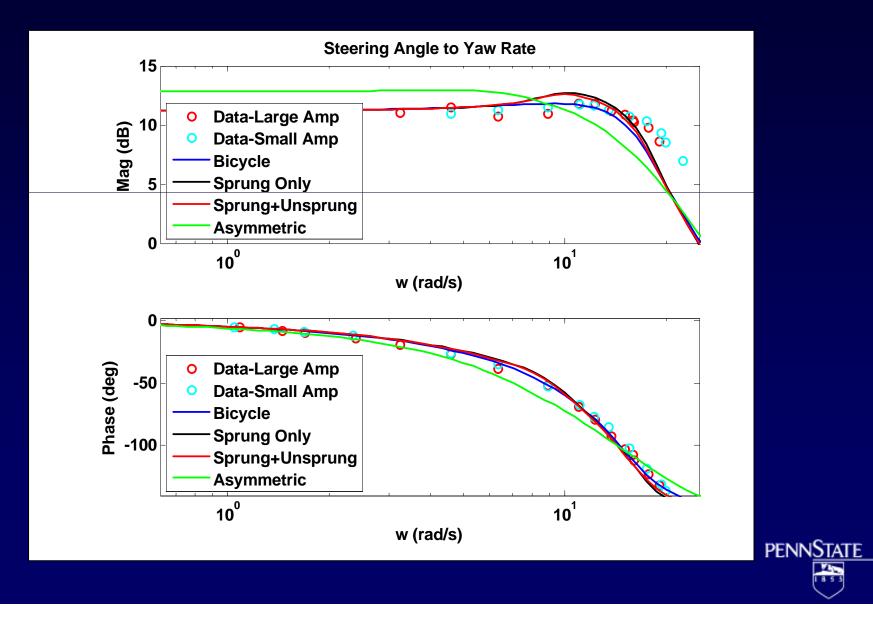
- Model 4 3DOF Roll Model
  - Assumes a sprung mass suspended upon a massless frame
  - x-z planar symmetry
  - No roll steer influence
  - Originally presented by Carlson and Gerdes, Stanford University, 2003

$$\begin{bmatrix} -m & 0 & 0 \\ 0 & -I_{zz} & 0 \\ 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} \dot{V} \\ \dot{r} \\ \dot{\phi} \end{bmatrix} + \begin{bmatrix} 0 & -mU & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} V \\ r \\ \dot{\phi} \end{bmatrix} + \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} y \\ \psi \\ \phi \end{bmatrix} = \begin{bmatrix} 2 & 2 \\ 2l_f & -2l_r \\ 0 & 0 \end{bmatrix} \begin{bmatrix} F_f \\ F_r \end{bmatrix}$$

$$\begin{bmatrix} -m & 0 & -mh \\ 0 & -mh \\ 0 & -I_{zz} & 0 \\ 0 & 0 & -I_{zz} \end{bmatrix} \begin{bmatrix} \dot{V} \\ \dot{r} \\ \dot{\phi} \end{bmatrix} + \begin{bmatrix} 0 & -mU & 0 \\ 0 & 0 & 0 \\ 0 & 0 & D_{\phi} \end{bmatrix} \begin{bmatrix} V \\ r \\ \dot{\phi} \end{bmatrix} + \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & D_{\phi} \end{bmatrix} \begin{bmatrix} V \\ r \\ \dot{\phi} \end{bmatrix} + \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & K_{\phi} - mgh \end{bmatrix} \begin{bmatrix} y \\ \psi \\ \phi \end{bmatrix} = \begin{bmatrix} 2 & 2 \\ 2l_f & -2l_r \\ 2h & 2h \end{bmatrix} \begin{bmatrix} F_f \\ F_r \end{bmatrix}$$

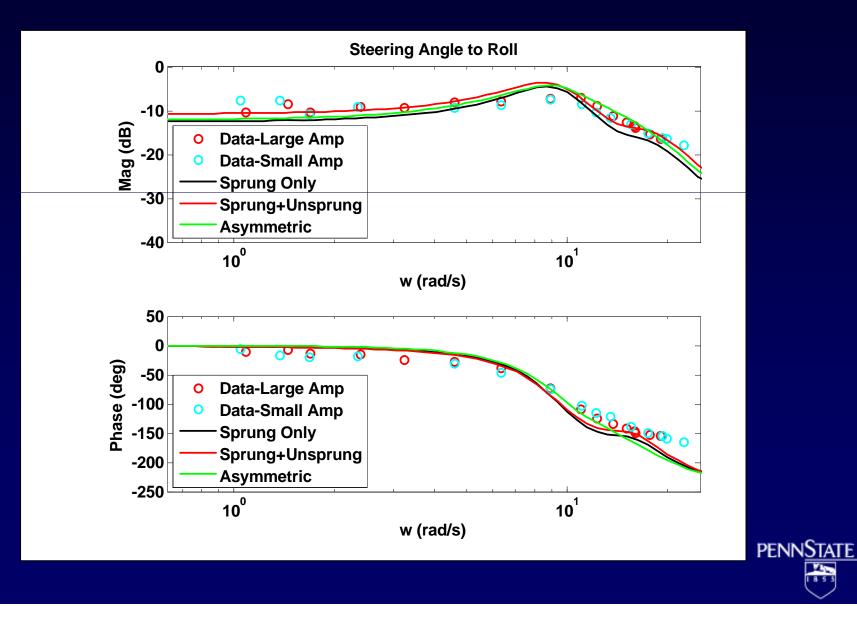
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## **Model Fitting** Frequency Response – Yaw Rate



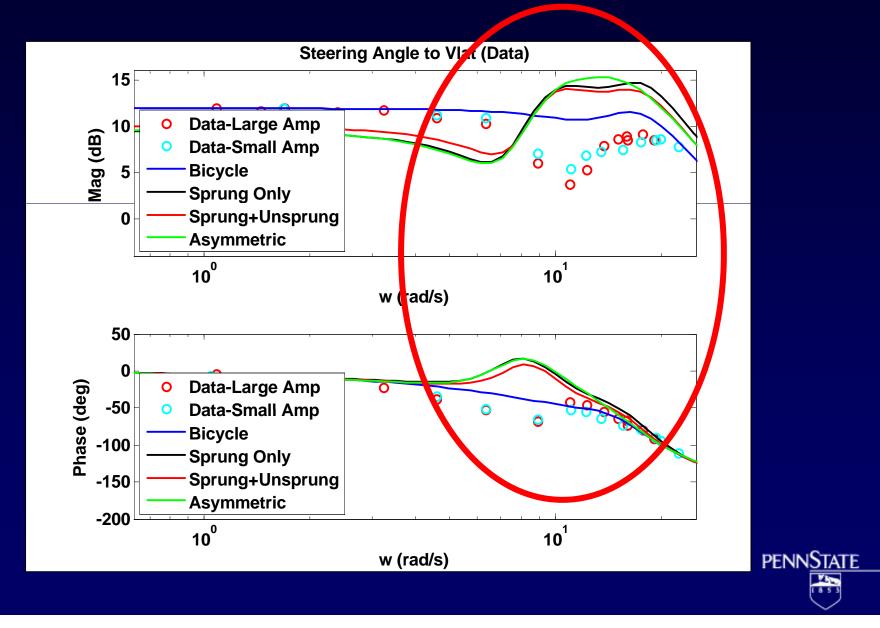
## **Model Fitting** Frequency Response – Roll Angle

### Frequency responses show good fits! How about roll responses? Time domain?



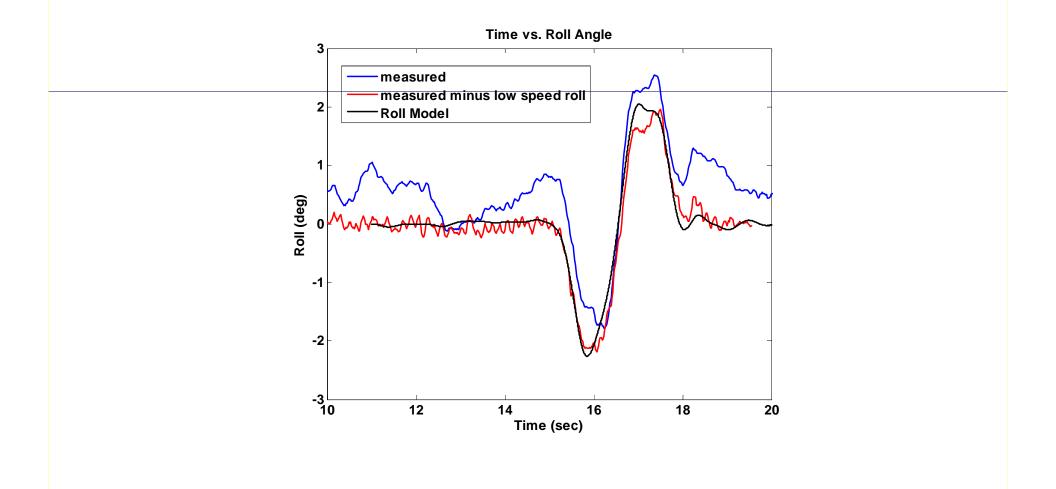
## **Model Fitting** Frequency Response – Lateral Velocity

### AWFUL fit Turns out have a poor SNR EXACTLY in region of interest



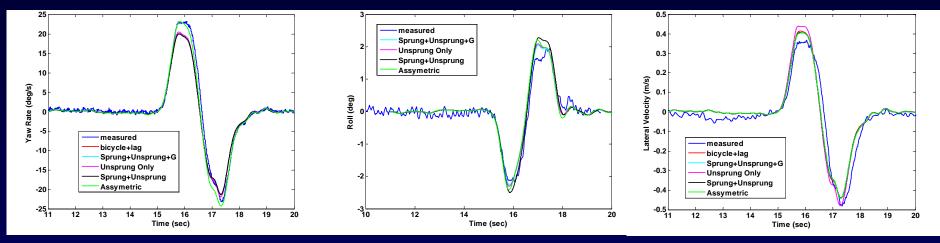
# The influence of terrain

Step 1: Collect data set 1 along a path at high speed. Note tire marksStep 2: Drive over tire marks at low speed, collect data set 2.Step 3: Subtract data set 2 from data set 1. Plot results.

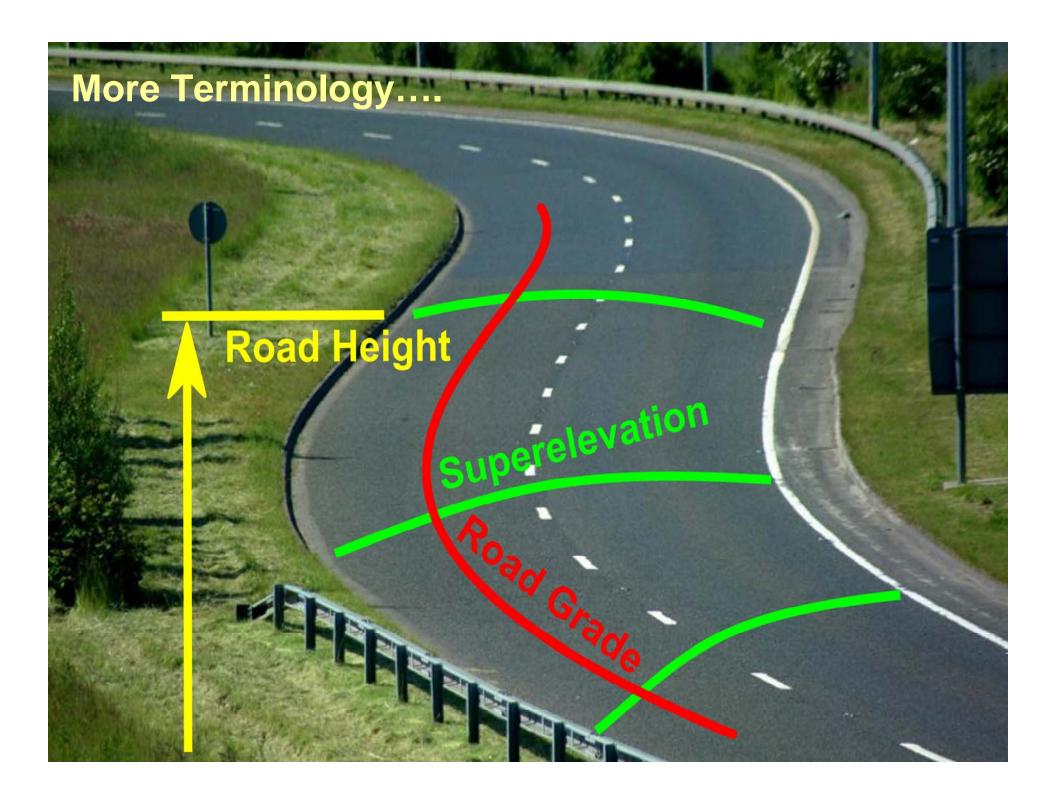


## "Terrain Corrected" Model Fits – Time Domain Iane change

## After terrain influence is removed...

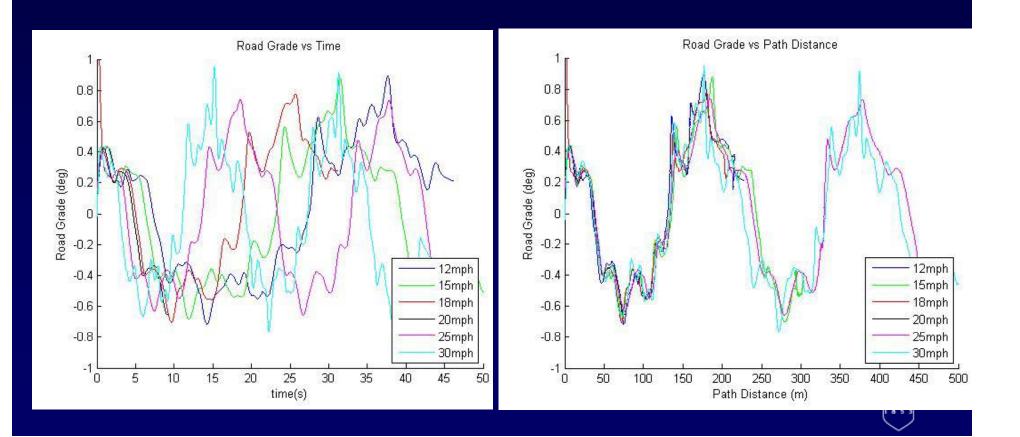






# Further analysis of the influence of terrain

- Road grade (vehicle pitch) investigated for steady state circle at various speeds
- When aligned based on global yaw angle (path distance covered), the road grade measurement is very repeatable regardless of speed



# Feasibility

- Past work
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# Again... go back to the test track!

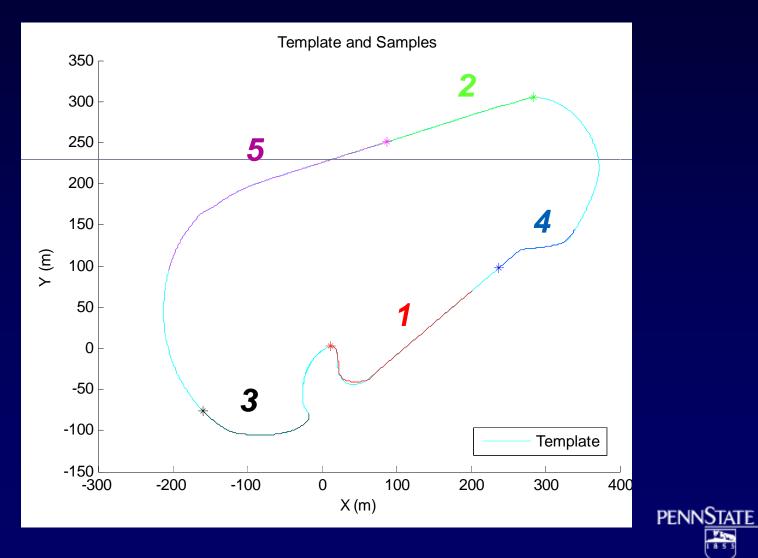
"Theory guides. Experiment decides." - Anonymous



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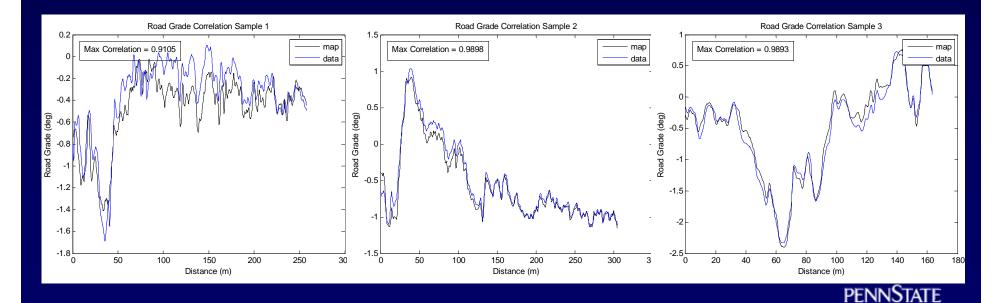
# **Road Grade Positioning**

• 5 Trials



# **Road Grade Positioning**

Sample	Average  Path Error	Standard Deviation	Average  Lane Keeping Error	Correlation
1	134 cm	27 cm	48.6 cm	0.9105
2	15 cm	12 cm	11.5 cm	0.9898
3	9 cm	5 cm	9.7 cm	0.9893
4	66 cm	14 cm	16.7 cm	0.961
5	13 cm	14 cm	9.1 cm	0.9889



# Are we matching BIG bumps in the road? No...





# What is being correlated?

Roadway surface texture ~ 0.01 meters

Step changes in surface elevation ~ 1 meter Potholes ~ 0.1 meters

http://media.torontolife.com/dynimages

Surface leveling undulations ~ 10 – 100 meters Road elevation ~ 1000 meters

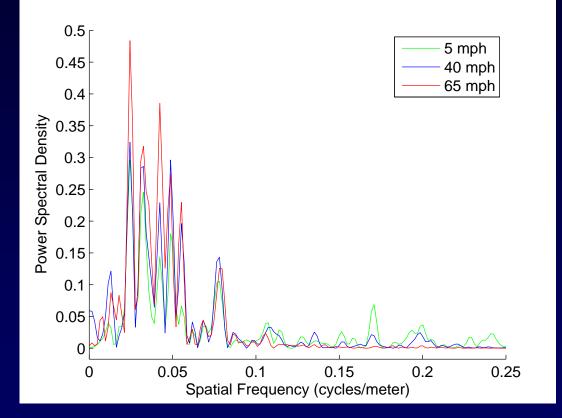
mo Road ~ mo

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### **Speed Invariance Test**

The Power Spectral Density of the vehicle response at various speeds shows:

- The low-speed data has a higher power density at high frequencies
- The correlation between signals matches quite well for frequencies < 0.1</li>
- Use a low-pass filter at 0.1 cycles/meter for speed invariant correlation





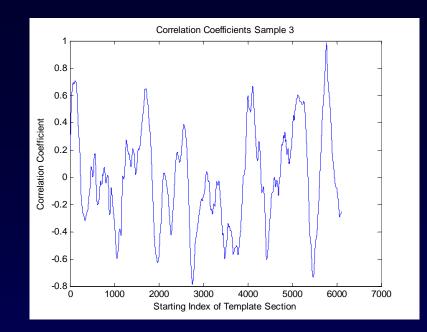
# Feasibility

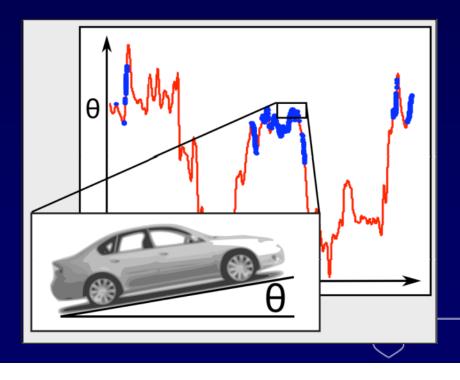
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## **Terrain-Based Approach**

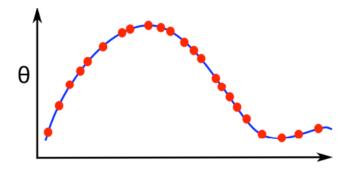
- Goal: use a terrain map for road vehicle localization using attitude measurements, assuming:
  - The lane of travel has been previously mapped
  - The map is available onboard the vehicle
- Problem: multiple local solutions
- First approach: use a Particle Filter



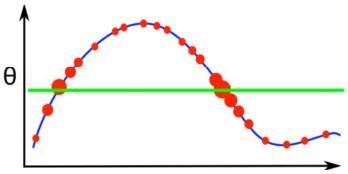


# **Particle Filtering Using Road Data**

 Populate a road grade or pitch response map with N particles



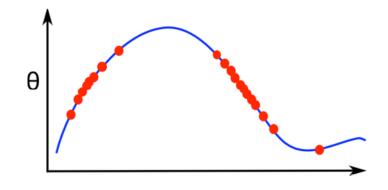
2. Weight the particles according to their pitch using the true pitch measurement and:



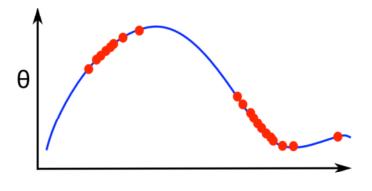
$$q_i^k = \frac{exp\left(-\frac{1}{2 \cdot R} \cdot \left(\theta_a - \theta_{p,i}\right)^2\right)}{\sum_{i=1}^N \left(exp\left(-\frac{1}{2 \cdot R} \cdot \left(\theta_a - \theta_{p,i}\right)^2\right)\right)}$$



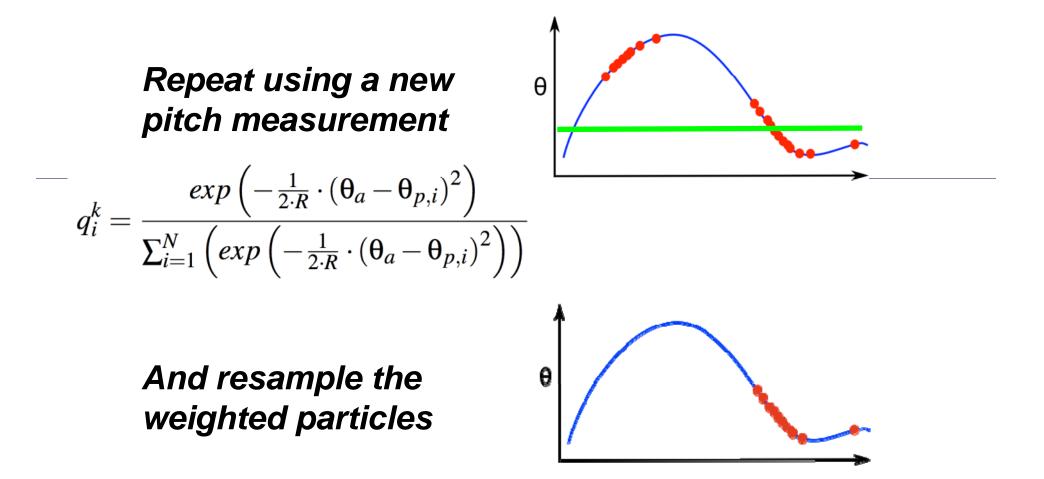
 Resample the particles according to their weight. High weights get more particles nearby.



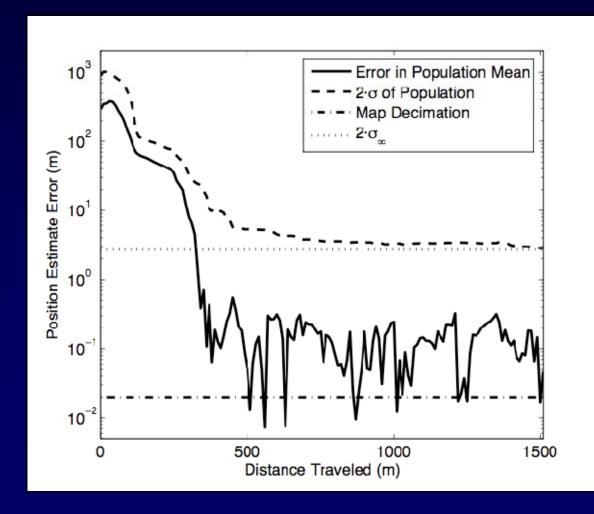
4. Shift the particles using the measured odometry and added variance:



$$P_X^k = P_X^{k-1} + dX + Q_X$$



# Longitudinal Positioning: LTI Results



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# **Kalman Filtering**

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# **System Model**

• Assuming the state model to be:

$$x_k = A \cdot x_{k-1} + B_u \cdot u_{k-1} + B_w \cdot w_{k-1}$$
$$y_k = C \cdot x_k + D_u \cdot u_{k-1} + D_v \cdot v_{k-1}$$

• Can approximate the particle filter using a singlestep Kalman filter

$$x_{k+1} = A \cdot (I - K_k C) \cdot x_k + A K_k y_k + B_u u_k$$
  

$$K_k = P_k C^T \cdot (C P_k C^T + R)^{-1}$$

$$P_{k+1} = Q + AP_k A^T - AP_k C^T (CP_k C^T + R)^{-1} CP_k A^T$$

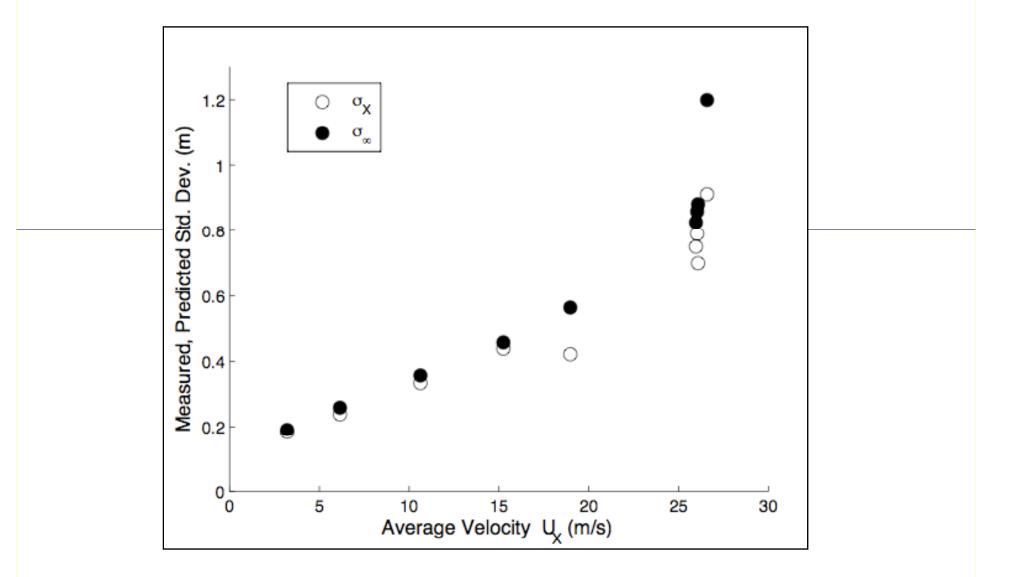
• Under conditions of controllability and observability, the covariance will converge to:

$$P_{\infty} = Q + AP_{\infty}A^{T} - AP_{\infty}C^{T} (CP_{\infty}C^{T} + R)^{-1} CP_{\infty}A^{T}$$

 Because it is independent of any measurements, let A = 1 and simplify to get

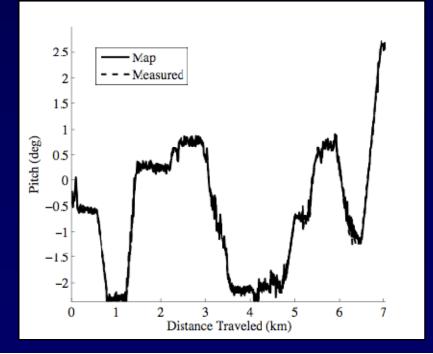
$$\mathbf{P}_{\infty} = \frac{Q}{2} \cdot \left( 1 + \sqrt{1 + \frac{4 \cdot R}{C^2 \cdot Q}} \right)$$

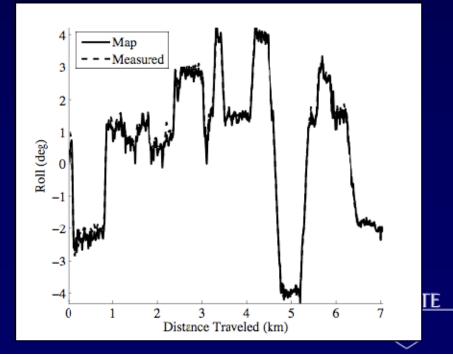
# **Predicted vs. Measured: Great Agreement!**



# Longitudinal Positioning: Highway Results (Time)

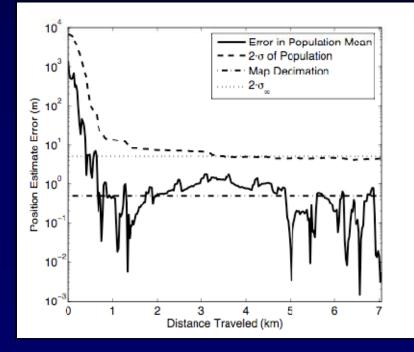
- Highway implementation more realistic and difficult
  - Smoothest roads available, reduced variations in pitch
  - High traveling speeds, increased wheelbase filtering



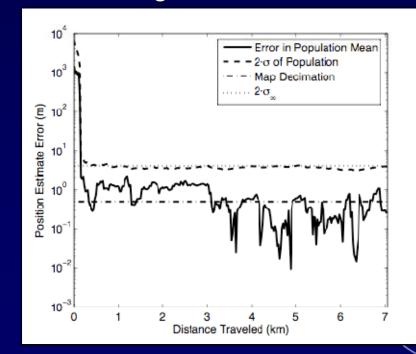


# Longitudinal Positioning: Highway Results (Error)

- Estimated vehicle position with meter-level accuracy
- Using roll resulted in a faster convergence



#### **Using Pitch Measurements**

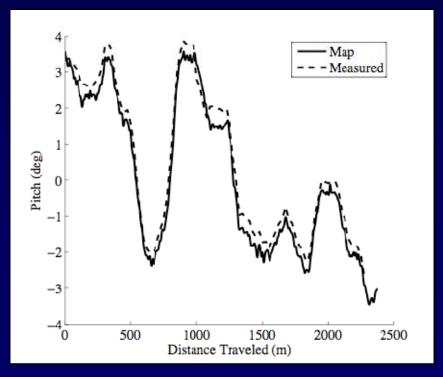


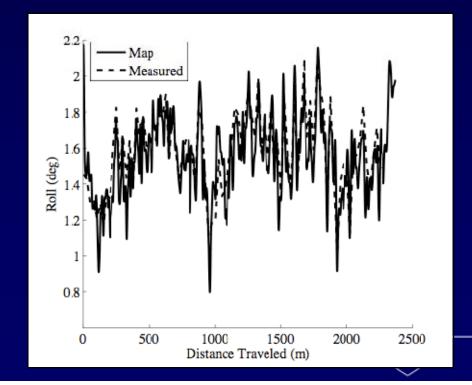
#### **Using Roll Measurements**

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# **Longitudinal Positioning: City Results**

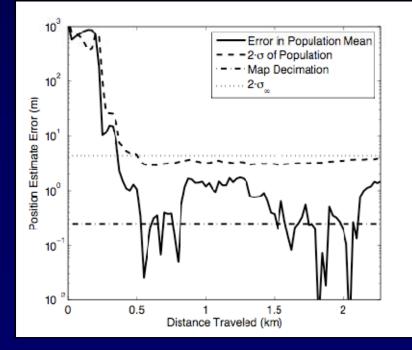
- Localizing along secondary roadways can be:
  - More accurate due to large signal-to-noise ratio in pitch
  - Less accurate due to lane-keeping errors with uneven superelevation profiles



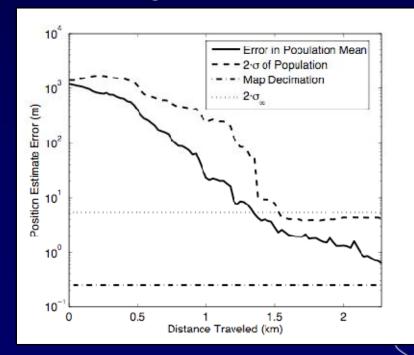


## **Longitudinal Positioning: City Results**

- Using the pitch measurements resulted in meterlevel accuracy
- The low signal-to-noise ratio of the roll measurements resulted in a slow convergence



#### **Using Pitch Measurements**



#### Using Roll Measurements

**TE** 

## **Kalman Filtering**

- Past work
  - Motivation for using terrain maps to localize a vehicle
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#### Task 3 items

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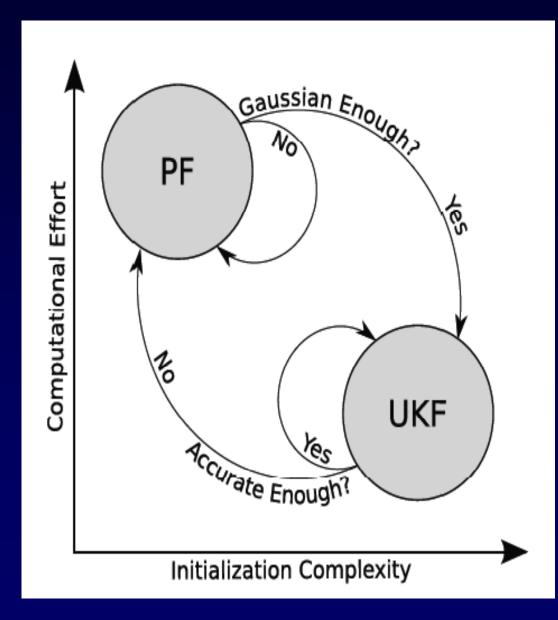
## Why a Hybrid approach?

	Particle Filter	UKF
<b>Computational Complexity</b>	High	Low
Initialization Complexity	Low	High

- Unscented Kalman Filters
  - Are computationally cheaper than Particle Filters, actually a special case of a Particle Filter where you have 2n+1 particles instead of thousands
  - Need to be initialized with a Gaussian
     Probability Distribution



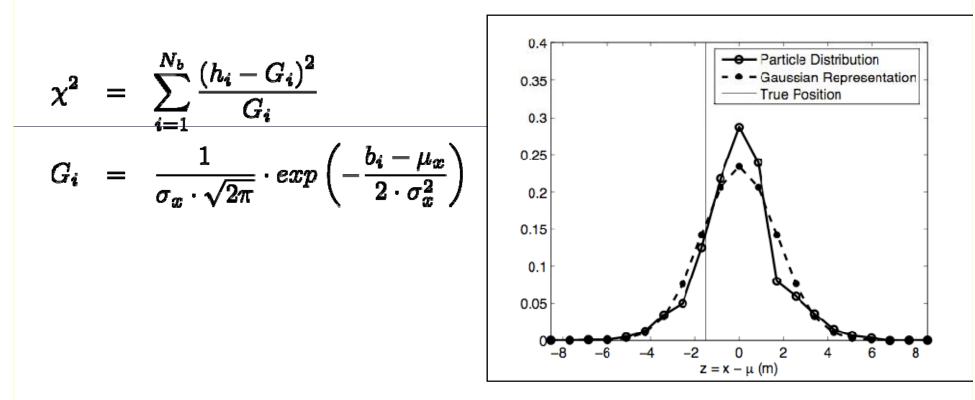
## **Using an Unscented Kalman Filter**



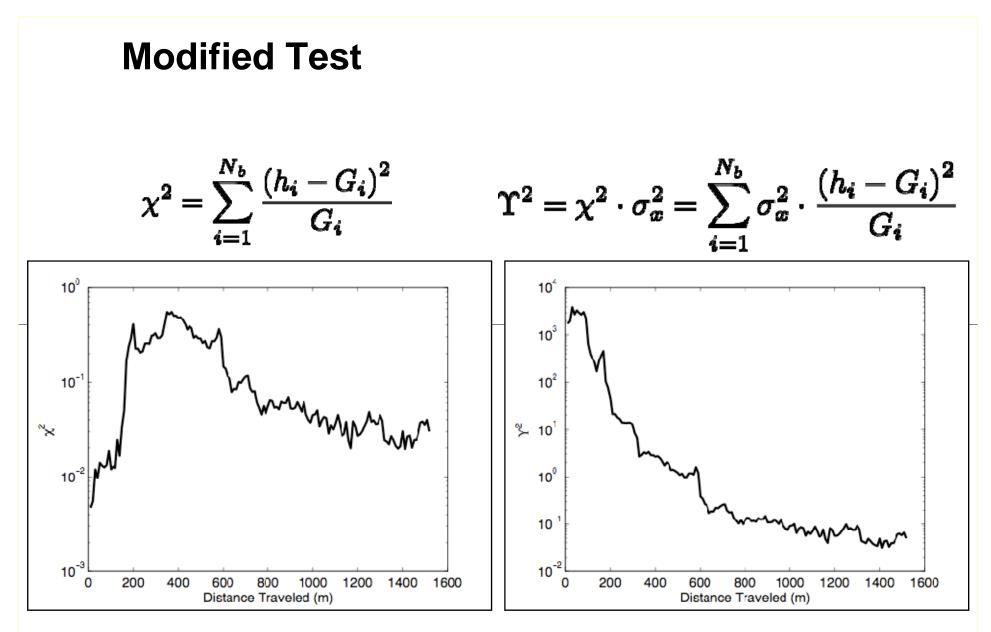


## Initialization

• Use a Chi-squared test to detect a Gaussian distribution:

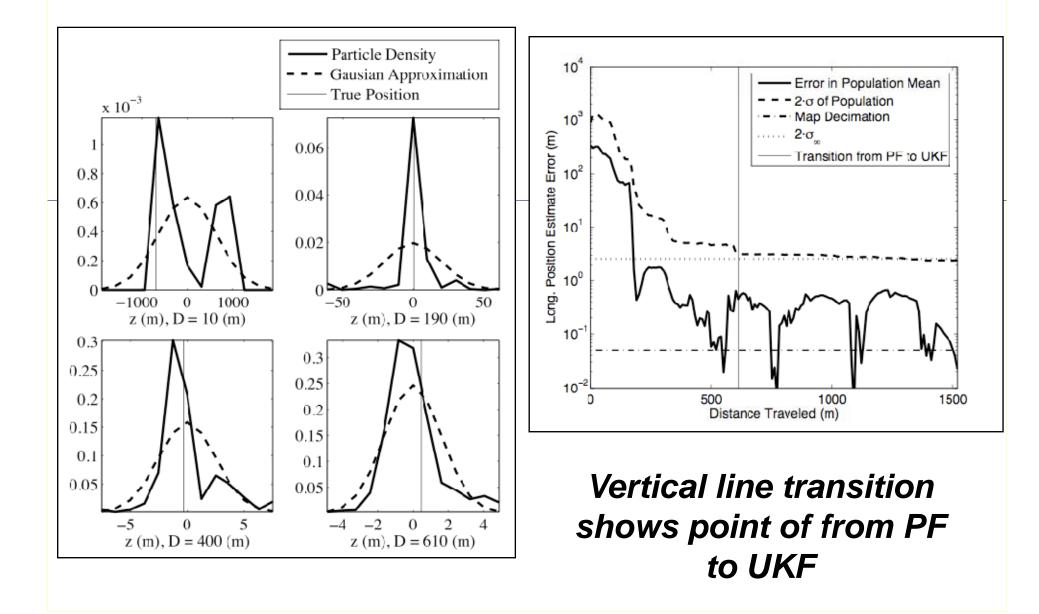


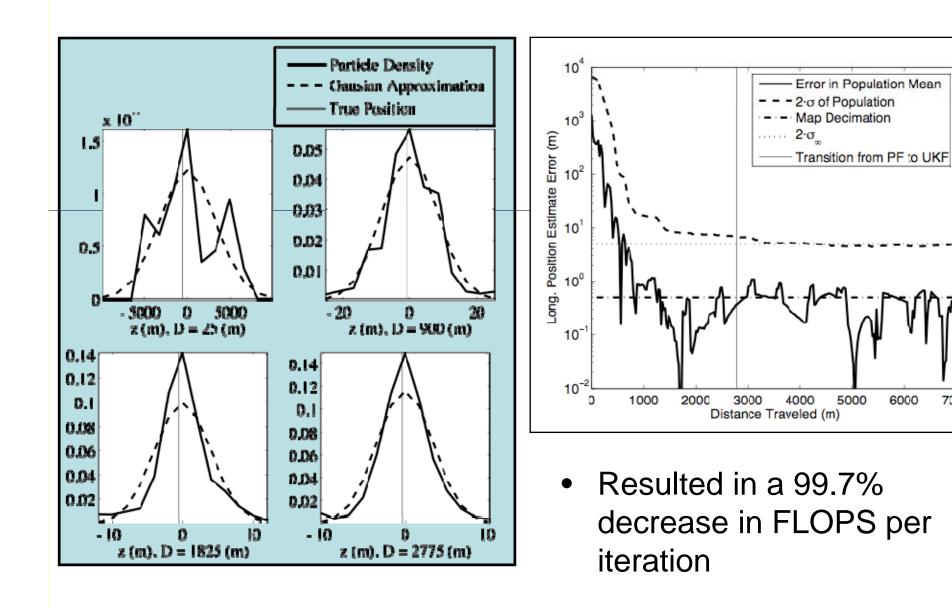
- where h<sub>i</sub> is the histogram of the population at bins b<sub>i</sub> and using the standard deviation of the population
- Switch to a UKF when reduced to a desired threshold  $\sigma_x$



Threshold is more obvious using the modified test

## Localization Results: LTI





## **Ongoing Work**

- Past work
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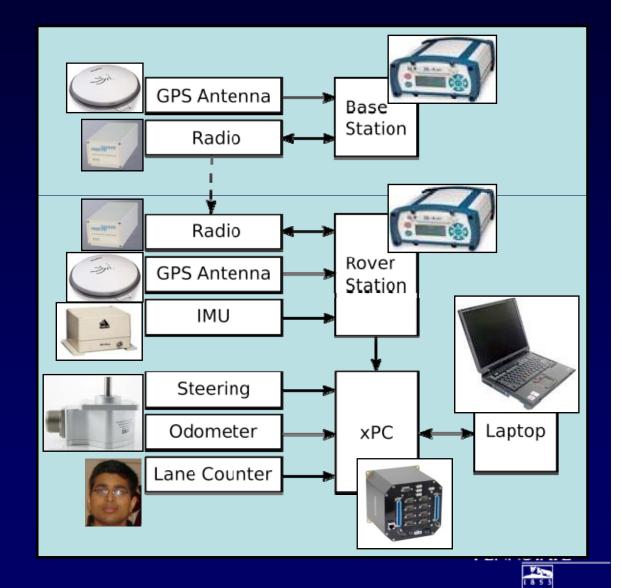
## **Data Acquisition**





### **Data Acquisition**

- Using:
  - NovAtel SPAN
     GPS/IMU system
  - US Digital Optical Encoders
  - Diamond PC104
  - IBM laptop
- Logging:
  - Vehicle Position
  - Vehicle Attitude
  - Steering Input
  - Wheel Odometry
  - Lane Index



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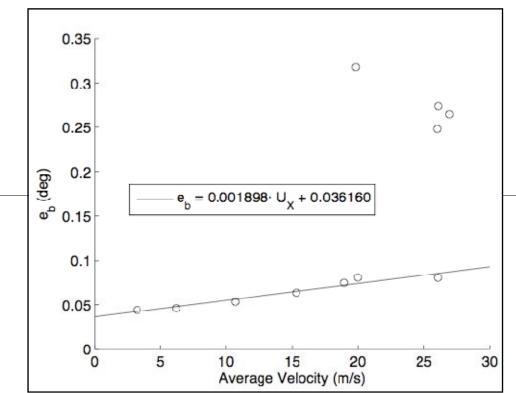
#### Accuracy reduction of vehicle data

- Accuracy of vehicle data needs to be determined, particularly on test vehicle.
- We have started this on our own vehicle, and found that sensor fidelity depends on
  - Speed
  - Roadway type (highway versus secondary)
  - Sensor specs
- We have functions that describe this behavior for our vehicle, but need to know if this holds on other vehicles



#### Sensor bias error versus speed

- We calculated the average bias of several data sets at various speeds
- Plotted as a function of traveling velocity and linearized
- Use to estimate the minimum variance:



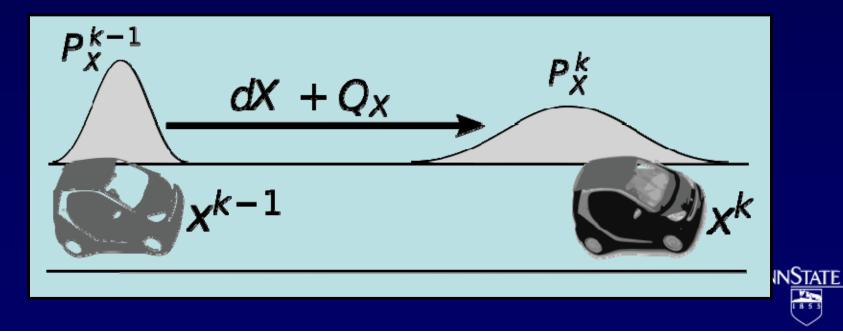
$$\begin{aligned} R_p &= \sigma_p^2 = \left(\frac{e_b}{3}\right)^2 = \left(0.00063 \cdot u_x + 0.012\right)^2 \\ \bullet \quad \text{Use } R_p \text{ to get:} \qquad P_\infty &= \frac{Q}{2} \cdot \left(1 + \sqrt{1 + \frac{4 \cdot R}{C^2 \cdot Q}}\right) \end{aligned}$$

#### **Encoder-Induced Motion Variance**

- The particle's longitudinal position are updated using the motion model:  $p_k = p_{k-1} + dY + Q_{k-1}$ 

$$P_X^k = P_X^{k-1} + dX + Q_X$$

 The variance Q is used to model the variance in the odometry measurement dX



# Encoder Motion Variance: the Q parameter in a Kalman filter

- Estimate variance Q using:
  - We used aUS Digital optical encoder with  $N_c = 8192$ counts/revolution, sampled at 100 Hz
  - Distance between DGPS points as true travel distance
  - We need to collect similar data for test vehicle, using in-vehicle sensors!





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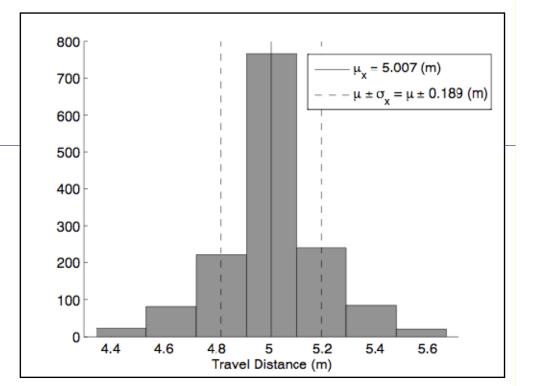
### **Motion Variance: Q**

- Calculate the number of counts to travel 5 meters
- Convert counts to measured distance error:

$$\mathbf{z}_{m,i} = \frac{2\pi R_w}{N_c} \cdot (n_{c,i} - \mu_c)$$

• Calculate the standard deviation of the errors:

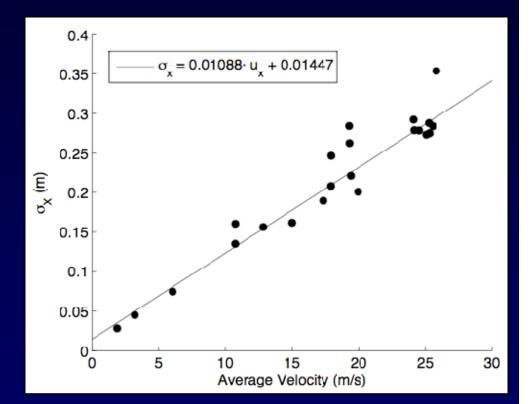
$$\sigma_x = \sqrt{\frac{1}{n} \Sigma \left( z_{m,i} \right)^2}$$



#### **Variance: Motion Model**

- Using several data sets from the LTI test track, city driving, and interstate highway:
  - Plot the standard deviation as a function of traveling speed
  - Use a linear fit to estimate variance in the motion model:

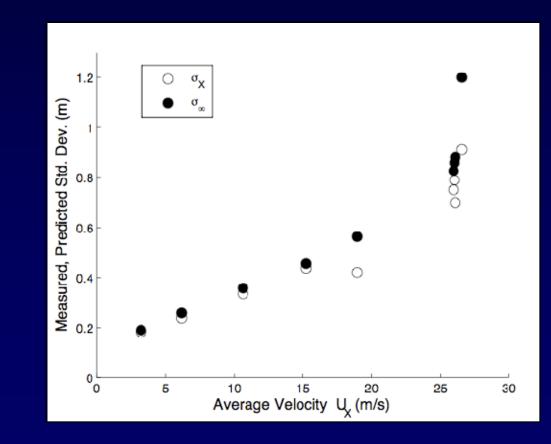
$${
m Q}=\sigma_x^2=(0.01\cdot u_x+0.015)^2$$



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# What are sensor models good for? They predict the accuracy of position information!

 Predicted versus measured variance in PF versus KF (KF is used to predict PF)



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#### **Accuracy reduction of maps**

- Currently are saving location histories every 10 cm on highway, 2 cm on arterial and secondary roads. Results show this is clearly "overkill"
- Currently working on several ideas to reduce data storage for maps.
- 1. Downsampling
  - Using polynomials or interpolation to save fewer points
- 2. Feature methods
  - Use wavelet representations of road features to reduce point-by-point representation
  - The same techniques allow a feature-space representation, and thus enable a "search tree" approach.



#### **Example of feature-points method**

 $W_2f(u,s)$ 0.5 Maxima / 0 Minima -0.5 -1 1.335 1.345 1.35 1.36 1.34 1.355 1.365 1.37 u x 10<sup>4</sup> -0.075 Linearization f \*  $\bar{\theta}_s(u)$ -0.08 -0.085 -0.09 1.35 1.36 1.34 1.345 1.355 1.365 1.37 u x 10<sup>4</sup> -0.075 Feature f \*  $\bar{\theta}_s(u)$ -0.08 vectors -0.085 -0.09 \_\_\_\_\_ 1.335 1.34 1.345 1.35 1.355 1.36 1.365 1.37 u x 10<sup>4</sup> 1 8 5 5

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- Large road network testing



#### **Example of fused sensor inputs**

In the past, we've looked at combining camera data with terrain maps to create augmented reality match

•Real and virtual scenes are compared.

•Preliminary results show orientation accuracies of 0.1 deg





Wonderful potential in this project for similar work!

### **Multi-dimensional System Model**

• Assuming the state model to be:

$$x_k = A \cdot x_{k-1} + B_u \cdot u_{k-1} + B_w \cdot w_{k-1}$$
$$y_k = C \cdot x_k + D_u \cdot u_{k-1} + D_v \cdot v_{k-1}$$

• The previous equations still apply, but instead have higher dimension!

$$\begin{array}{rcl} x_{k+1} &=& A \cdot (I - K_k C) \cdot x_k + A K_k y_k + B_u u_k \\ K_k &=& P_k C^T \cdot (C P_k C^T + R)^{-1} \end{array}$$

$$P_{k+1} = Q + AP_k A^T - AP_k C^T (CP_k C^T + R)^{-1} CP_k A^T$$

# To integrate terrain-localization sensor with other measurements, what is needed?

- 1. Dynamics of the terrain "sensor"
  - a) How fast does it converge
  - b) Does convergence rate change as a function of road position?
- 2. Internal calculation of the estimate "health"
  - a) Obtained by RMS error between predicted/measured values at each location
  - b) If disagreement is large, need to indicate this somehow with a voting algorithm or median filter
- 3. Estimates of variance of the terrain-based sensor
  - a) For PF's, can use particle population variance useful to discern multi-modal estimates
  - b) For KF, can use covariance



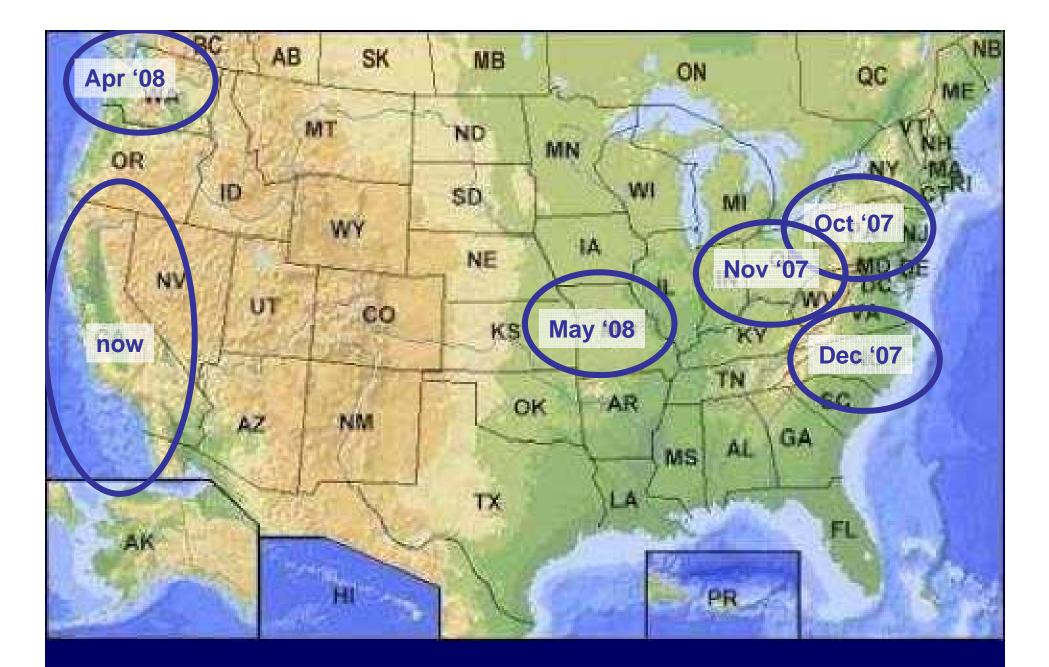
## **Ongoing Work**

- Past work
  - Motivation for using terrain maps to localize a vehicle
  - Feasibility of location-based road "fingerprints"
  - Framing localization as a nonlinear particle-filter correlation problem
  - Attacking the nonlinear problem with a Kalman approach
  - Hybridizing the method to have the advantages of both the linear/nonlinear approaches

#### • Task 3 items

- Vehicle integration, data collection
- Accuracy reduction including vehicle and maps
- Integration of terrain-based localization with existing vehicle localization architectures.
- Large road network testing



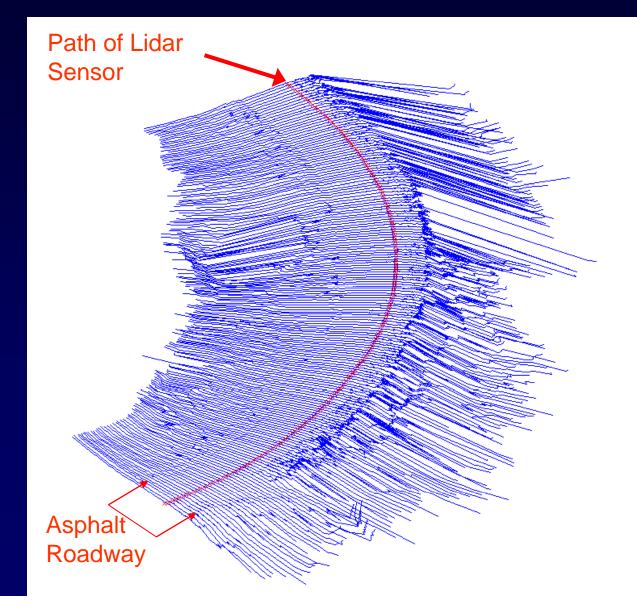


See http://controlfreaks.mne.psu.edu for more info

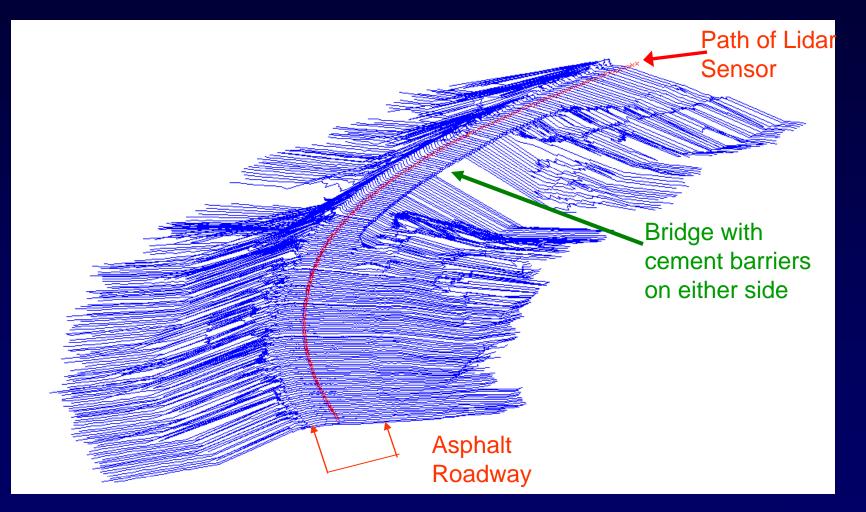


## Mapping terrain

- Shown at right is a banked curve from the test track
- Getting 10 to 30 scans per second out to 80 meters of range.
- Accuracy on the order of 6 cm at best case (perfect GPS).
- Actual error is on the order of a meter or less.



## Example bridge section



See http://controlfreaks.mne.psu.edu for more info







### **Remaining field mapping**

We propose to include terrain-based localization methods over a large area network. Steps:

1) Collect data over a large network locally (so it can be re-mapped)

Starting in Jan 2010, we will be mapping (LIDAR) entire region around Penn State area (Pennsylvania and sections of NY)

- Sponsored by SHRP2, so can leverage same effort for this project
- Database will be public in 3-6 years
- 2) Collect data over a large network remotely

Use portable data-collection system to map

- Auburn area
- New York City (ITS)
- Other sites?



## **Task 3 estimated timeline**

1.2 Conduct Expert Panel Mtgs						
2.0 Literature Survey						
3.0 Investigate Terrain-Based Localization						
3.1 Install on Test Vehicle						
3.2 Define Test Protocol						
3.3 Collect Characterization Data and Analyze Results						
4.0 Investigate Visual Odometry Based Positioning						
4.1 Install on Test Vehicle						

#### • Milestones?

- 3.1: Test data
  - Vehicle characterization data transferred to PSU
  - Characterization of sensor bias / error for Kalman filter
- 3.2: Protocol
  - Regions for testing and test routes identified
- 3.3: Data collection
  - Field data collected for at least one "prime" region
  - Error analysis for test routes

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#### Past and other ongoing supporters

**The National Science Foundation** – funded research into fundamentals of dynamic behavior through several student fellowships. (~\$200k)

**The National Academy of Science**, The Transportation Research Board – funded roadway scanning and terrain modeling (-\$300k)

**Army TACOM** – currently funding HIL work (~\$1M) and vehicle platooning work

The Federal Transit Agency – funded test track and vehicle systems used on the track such as the DGPS/IMU system (track ~\$14M, current project ~\$300k)

**Naval Explosive Ordinance Disposal** – currently funding robotics work that uses terrain models (~\$600k)



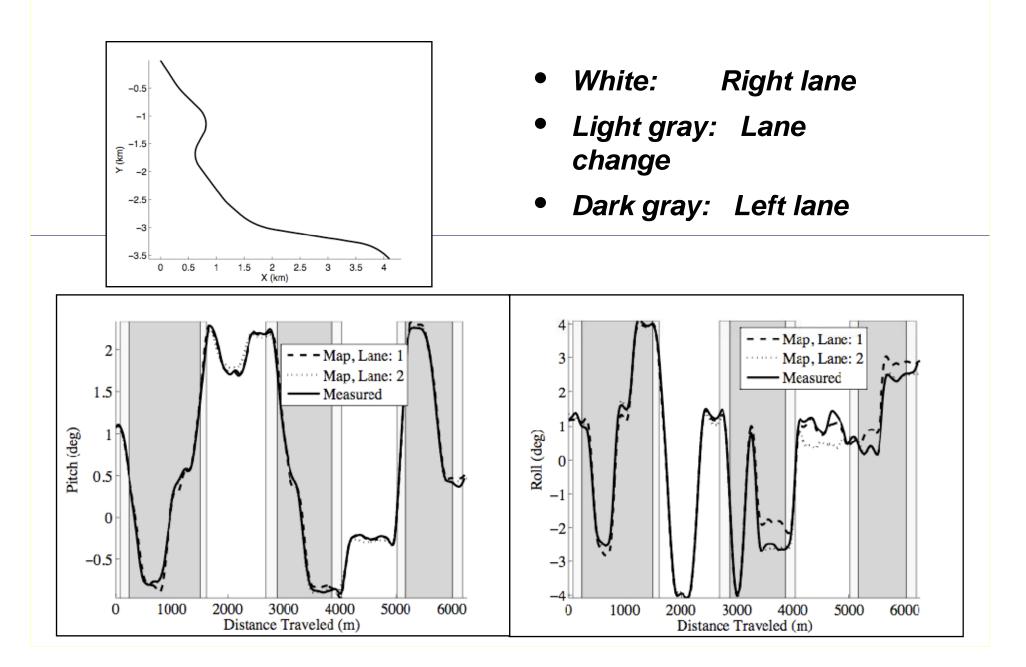
## **Questions?**

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## **Extra slides follow**

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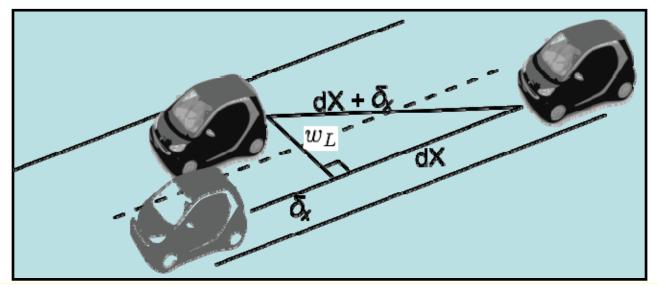
### **Multi-Lane Terrain Maps**



#### **Lateral Positioning: PF**

- Decouple the longitudinal and lateral positioning estimates
- Modify the motion model to account for odometry errors due to lateral motion

$$\delta_x = \sqrt{dX^2 + w_L^2} - dX$$
 $P_X^k = P_X^{k-1} + dX - rac{\delta_x}{w_L} \cdot \left| P_Y^k - P_Y^{k-1} \right| + Q_x$ 

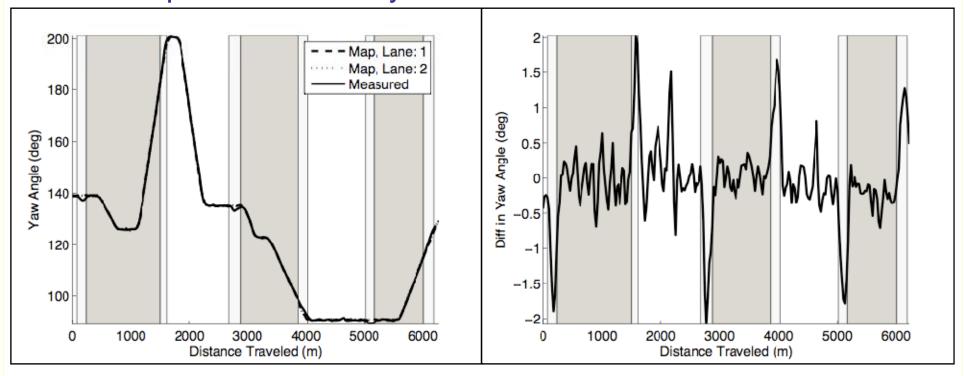


## **Measuring Lane Maneuvers**

• Add the lateral position estimate to the motion model using:

$$P_Y^k = P_Y^{k-1} + K \cdot (\psi_a - \psi_p) + Q_y$$

 Use difference in yaw measurements to shift particles laterally



#### Lane Indexing

 Round the particles lateral position to the nearest lane

#### **Using Pitch Measurements**

#### **Using Roll Measurements**

