

Ex. 82 page 91

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$$P(\text{a vehicle passes}) = 0.70$$

a) $P(\text{all the next 3 vehicles pass})$

V_1 passes, V_2 passes, V_3 passes.

$$P(\text{all 3 pass}) = 0.7 \times 0.7 \times 0.7 \\ = \underline{0.343}$$

b) $P(\text{at least 1 of the next 3 fails})$ Event B

V_1 can fail, V_2 can fail, V_3 can fail

V_1, V_2 can fail, V_1, V_3 can fail...

$$P(B) = 1 - P(B')$$

B' = all 3 vehicles pass.

$$P(B') = 0.343$$

$$P(B) = 1 - 0.343 = 0.657$$

c) $P(\text{exactly 1 passes}) = ?$

either 1st or 2nd or 3rd passes &

the remaining 2 fails.


$(V_1)_p (V_2)_f (V_3)_f$ or $(V_1)_f (V_2)_p (V_3)_f$ or
 or $(V_1)_f (V_2)_f (V_3)_p$

$$\begin{aligned}
 P(\text{exactly 1 passes}) &= (0.7)(0.3)(0.3) \\
 &\quad + (0.3)(0.7)(0.3) \\
 &\quad + (0.3)(0.3)(0.7) \\
 &= 0.189
 \end{aligned}$$

d) $P(\text{none passes}) + P(\text{exactly 1 passes})$

$$(0.3)(0.3)(0.3) + 0.189 = 0.216$$

e) $P(A|B) = \frac{P(A \cap B)}{P(B)} = \frac{P(A)}{P(B)}$



$$P(\text{all 3 pass} | \text{at least 1 passes}) = \frac{0.343}{0.973} = 0.353$$

$P(B)$

$$\begin{aligned}
 P(B) &= P(\text{at least 1 passes}) \\
 &= 1 - P(\text{all fail}) \\
 &= 1 - (0.3)^3 = 0.973
 \end{aligned}$$

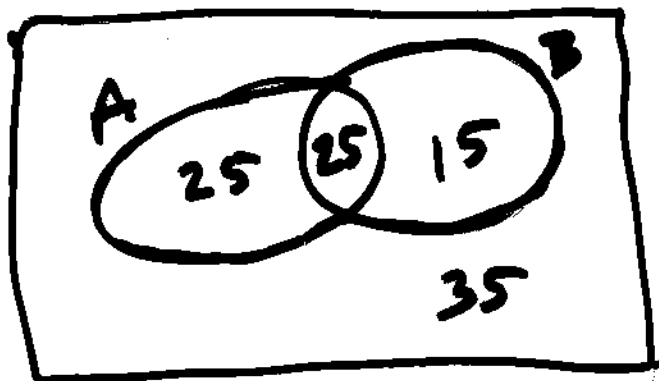


Graphical way.

$$e) \frac{.25 + .25}{.65} = .7692 \text{ OR } P(A|A \cup B)$$

$$P(A|A \cup B) = \frac{P(A \cap (A \cup B))}{P(A \cup B)}$$

$$= \frac{P(A)}{0.65} = \frac{0.5}{0.65} = .7692$$



of students = 100

Number of students with at least one card = 65 $\frac{50}{65} = .7692$

Poisson Distributions Example.

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Avg. # of accidents = 5/day

b) $P(\text{having at most 4 accidents the next day})$

$X =$ the # of accidents during the next day

$$P(X \leq 4) = P(X=0) + P(X=1) + \dots + P(X=4) \\ = p(0; 5) + p(1; 5) + p(2; 5) + \dots + p(4; 5)$$

$$p(x; \lambda) = \frac{\lambda^x}{x!} \cdot e^{-\lambda}$$

$$= \frac{5^0}{0!} \cdot e^{-5} + \frac{5^1}{1!} \cdot e^{-5} + \frac{5^2}{2!} e^{-5} + \dots + \frac{5^4}{4!} e^{-5}$$

$$= 0.44049 \dots$$

c) $P(X \text{ is an odd number})$

$$x = 1, 3, 5, 7, \dots$$

$$P(X \text{ is odd}) = p(1; 5) + p(3; 5) + \dots$$

Poisson dist. with time interval > 1 67

a) $P(Y=11)$ Y is the # of accidents during the next 3 days.

$t = 3$ days $\lambda = 5$ accidents/day

$$P(y; \lambda t) = P(11; (5)(3)) = P(11; 15)$$

$$P(11; 15) = \frac{(\lambda t)^y}{y!} \cdot e^{-(\lambda t)} = \frac{(15)^{11}}{11!} \cdot e^{-15}$$

$$= 0.0662874$$

b) $P(\text{at least 11 accidents in the next 3 days})$

$$= 1 - P(\text{at most 10 accidents in the next 3 days})$$

$$= 1 - \underbrace{[P(0; 15) + P(1; 15) + P(2; 15) + \dots + P(10; 15)]}_{0.118464412}$$

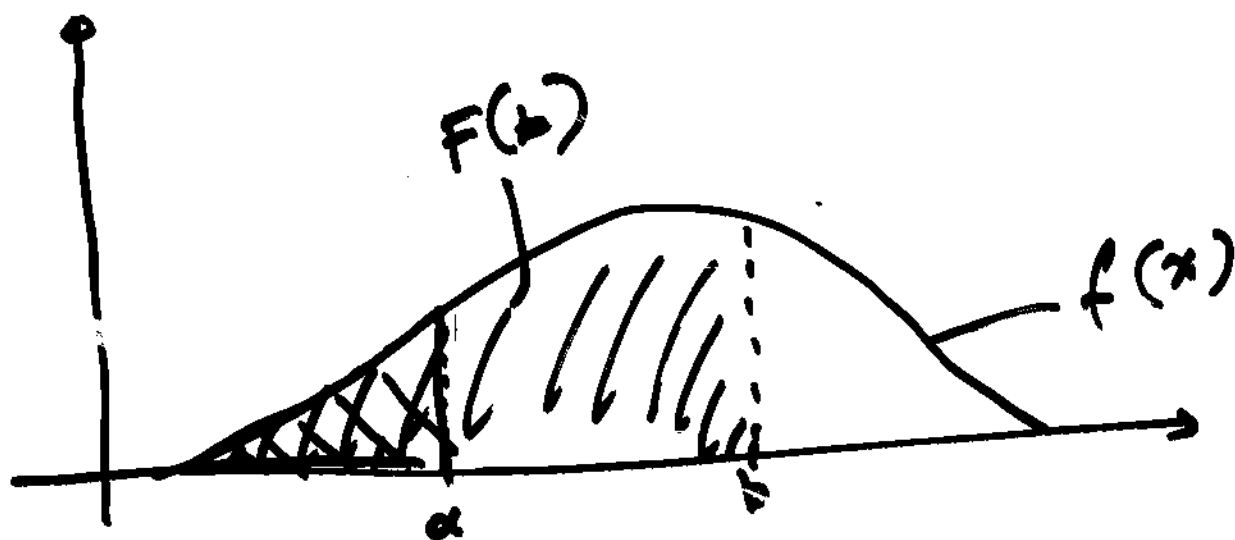
$$P(\text{at least 11 accidents in the next 3 days}) = 1 - 0.118464412 = 0.88153\dots$$

$$c) P(\text{at most 18 accidents in the next 4 days}) = \sum_{i=0}^{18} P(i; 20)$$

$$\lambda t = (5)(4) = 20 \quad = 0.381421949 \quad 5$$

Calculating probabilities using $F(x)$

L7



$F(b) = \text{shaded area} + \text{crossed area}$

$F(a) = \text{crossed area}$

$P(a \leq X \leq b) = F(b) - F(a)$
 $= \text{shaded area.}$