

HW 7 solutions

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$$\omega_n^2 = (2\pi(2500))^2 = 2.47 \times 10^8 \text{ s}^{-2}$$

$$T(s) = \frac{\frac{\omega_n}{Q}s + \omega_n^2}{s^2 + \frac{\omega_n}{Q}s + \omega_n^2} = \frac{448.8s + 2.47 \times 10^8}{s^2 + 448.8s + 2.47 \times 10^8}$$

1. $F = \frac{\epsilon_0 \epsilon_r A V^2}{2d^2} = \frac{(8.854 \times 10^{-12})(1)(500 \times 10^{-6})^2 (100)^2}{2(10 \times 10^{-6})^2} = 110.675 \mu\text{N}$

2. $\omega \gg \omega_n$, use $V = V_{\text{rms}}$

$$\therefore F = \frac{\epsilon_0 \epsilon_r A V_{\text{rms}}^2}{2d^2} = \frac{(8.854 \times 10^{-12})(1)(500 \times 10^{-6})^2 (100)^2}{(2)(2)(10 \times 10^{-6})^2} = 55.34 \mu\text{N}$$

3. $V_p = \sqrt{\frac{8Kd^3}{27A\epsilon_0\epsilon_r}}$

$$= \sqrt{\frac{8(50)(10 \times 10^{-6})^3}{27(500 \times 10^{-6})^2 (8.854 \times 10^{-12})(1)}}$$

$$= 81.81 \text{ V}$$

$$F = \frac{\epsilon_0 \epsilon_r A V^2}{2(d-x)^2}$$

$$= \frac{(8.854 \times 10^{-12})(1)(500 \times 10^{-6})^2 (81.81)^2}{2 \left[\frac{2}{3}(10 \times 10^{-6}) \right]^2}$$

$$= 166.67 \mu\text{N}$$

$$4A. \alpha = (\Delta L/L)/T$$

$$\Delta L = \alpha L \Delta T = (2.6 \times 10^{-6})(500 \times 10^{-6})(100) = 1.3 \times 10^{-7} \text{ m} = 0.13 \mu\text{m}$$

$$L_{\text{new}} = L + \Delta L = 500 + 0.13 = 500.13 \mu\text{m}$$

$$5A. L_{\text{new}} = L + \Delta L$$

$$= L + \alpha L \Delta T$$

$$= L(1 + \alpha \Delta T)$$

$$= 500 \times 10^{-6} [1 + (25 \times 10^{-6})(100)] = 5.0125 \times 10^{-4} \text{ m} = 501.25 \mu\text{m}$$

6A. a. Electrostatic

b. Thermal Bimorph

c. Piezoelectric

d. SMA

e. FlowFET

f. Thermal Pump

g. Magnetic

$$7A. d = aS$$

$$= \frac{a}{\omega_n^2}$$

$$= \frac{10(9.8)}{(2\pi(800))^2}$$

$$= 3.88 \times 10^{-6} \text{ m}$$

$$= 3.88 \mu\text{m}$$