d. Oscillators Using Crystal and Ceramic Resonators

Some limiting factors in LC oscillators include:

(1) The size and weight of inductors (particularly at low frequencies)
(2) Resistive losses in inductors (low inductor Q)
(3) Inductive accuracy of inductors
(4) Long term stability

Piezoelectric crystal and ceramic resonators are therefore used to improve these issues.

Quartz is a piezoelectric material. Piezoelectric materials experience a small dimensional change is response to an applied voltage. Also, they generate an electric charge in response to an applied mechanical stress. Some ceramics also exhibit piezoelectric properties.

Schematic symbol for piezoelectric crystal and ceramic resonators:
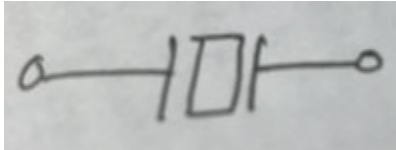
Overall equivalent circuit:
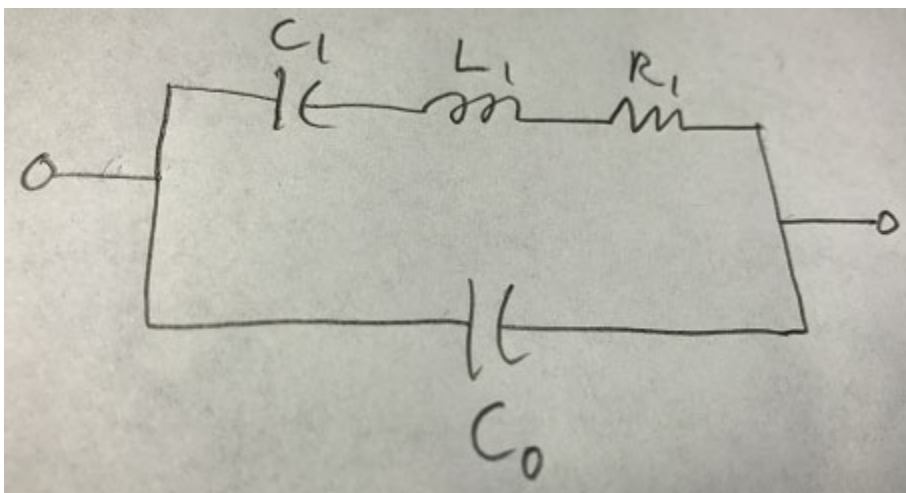
C_1: equivalent capacitance, motional capacitance

L_1: equivalent inductance, motional inductance

R_1: equivalent resistance, series resistance

C_o: inner electrode capacitance, holder or shunt capacitance
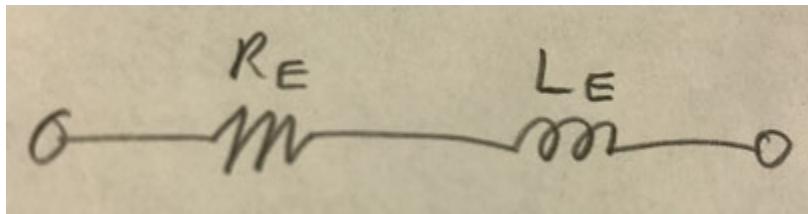

The resonator has an impedance Z=R+jX

f_r is the resonant frequency: $f_r = \dfrac{1}{2\pi\sqrt{L_1 C_1}}$

f_a is the anti-resonant frequency: $f_a = f_r\sqrt{(1 + C_1 + C_0)}$

Q_m is the mechanical quality factor: $Q_m = \dfrac{1}{2\pi F_r C_1 R_1}$

In between f_r and f_a, Z is normally inductive. See example on next page.

In between f_r and f_a, the resonator can be modelled as:

R_E is the effective resistance over this frequency range.

L_E is the effective inductance over this frequency range.

Z=R$_E$+jωL$_E$

Example L_1, C_1, R_1, C_o and Q_m values for some ceramic and crystal resonators <below>.

Note: higher oscillation modes (overtones) do exist due to the mechanical resonance. They only occur at odd multiples of the fundamental frequency (3rd, 5th, etc.). Crystals specified for frequencies over 30 MHz often use overtones. Your oscillator circuit must therefore be designed appropriately if using an overtone mode.
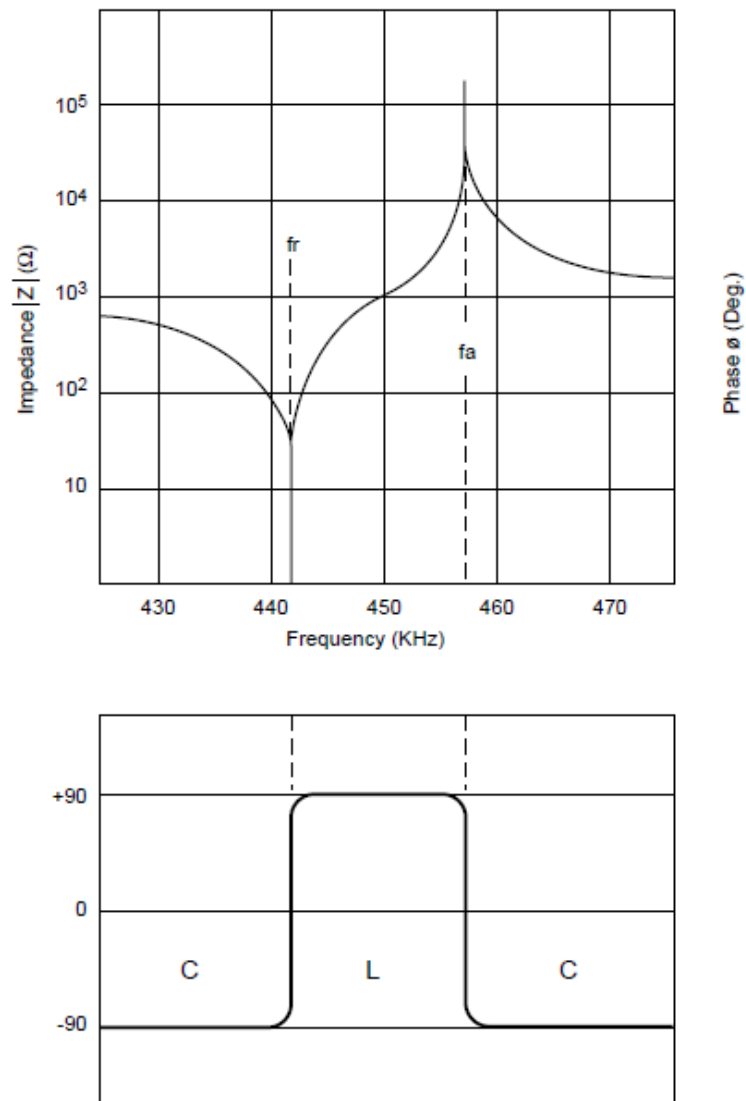
Figure 1.5) Impedance and Phase Characteristics for
Ceramic Resonators

FREQUENCY	CERAMIC RESONATOR				CRYSTAL			
	455KHz	2.50MHz	4.00MHz	8.00MHz	453.5KHz	2.457MHz	4.00MHz	8.00MHz
L_1 (µH)	8.8×10^3	1.0×10^3	385	72	8.6×10^3	7.2×10^3	2.1×10^3	1.4×10^4
C_1 (pF)	14.5	4.2	4.4	5.9	0.015	0.005	0.007	0.027
C_0 (pF)	256.3	33.3	36.3	39.8	5.15	2.39	2.39	5.57
R_1 (Ω)	9.0	17.6	8.7	4.8	1060	37.0	22.1	8.0
Q_m	2734	912	1134	731	23000	298869	240986	88677
ΔF (KHz)	12	147	228	555	0.6	3	6	19

Figure 1.1 Comparisons of equivalent Circuit Constants for Ceramic and Crystal Resonators
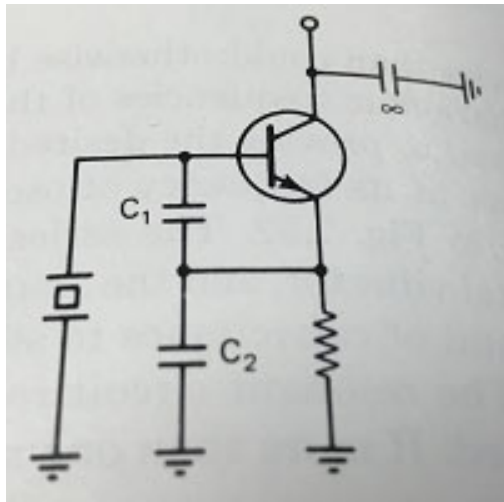
Courtesy ECE International, Inc.

Crystal and ceramic resonators can be used in linear or square wave oscillators. In a linear oscillator, they are used to replace the discrete inductor. Example linear oscillator circuits (biasing resistors omitted for simplicity):
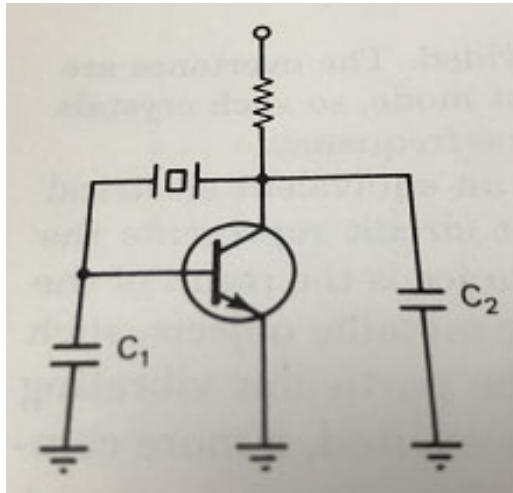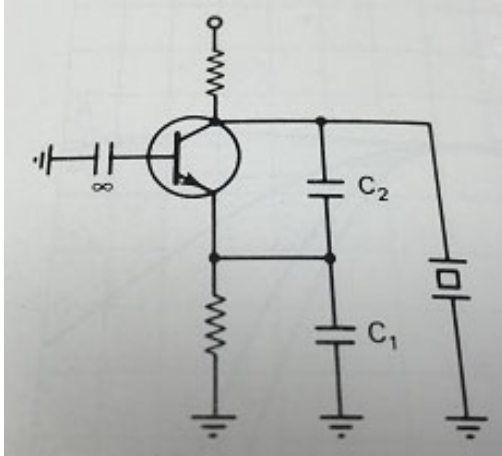

Pierce oscillator circuit.

The Pierce oscillator is a derivative of the Colpitts oscillator.

Clapp oscillator circuit with collector grounded.

The Clapp oscillator is also a derivative of the Colpitts oscillator, except that a 3rd capacitor, C_3, is used in series with the inductor (inherent in the resonator).

$$\omega_o = \sqrt{\frac{1}{L}\left(\frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3}\right)}$$

Clapp oscillator circuit with base grounded.

With each of these circuits, the crystal should be modelled with C_1, L_1, R_1 and C_o included.

These oscillator circuits are referred to as aperiodic oscillators, because they will occasionally operate in an overtone (higher frequency) mode. C_2 can be replaced with a resonant circuit to prevent this condition from occurring.
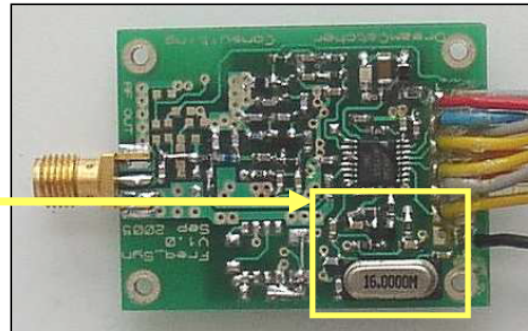
Note, these oscillators do not have AGC circuits. If the gain is too high, you may get a square wave output instead of a sinusoidal output.

Example of Tuned Feedback Oscillator (3)
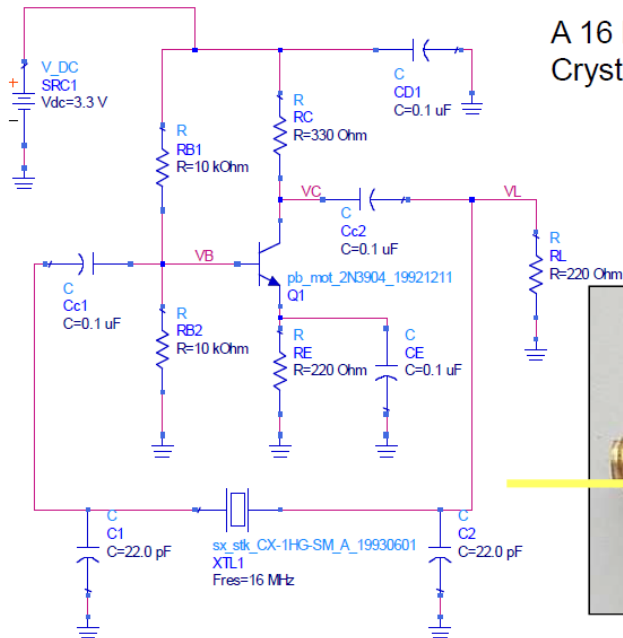
A 16 MHz Transistor Common-Emitter Crystal Oscillator

April 2012 © 2006 by Fabian Kung Wai Lee 14

Example crystal oscillator circuit using a common emitter amplifier in a Colpitts configuration.

Nonlinear Oscillators

Our definition: an oscillator with a periodic non-sinusoidal output, such as a square wave.

1) Sinusoidal oscillator circuit with a really high amplifier gain, much higher than necessary to satisfy the BSC

Let's revisit the Wein bridge oscillator (shown on next page)

R_3 of 15 kΩ achieved oscillation. Let's make R_3 by 25 kΩ and evaluate the difference. As R_3 gets large, the tops of the output signal flatten out, more closely approximating a square wave. This forces more of the time varying signal to reside in the nonlinear range of the op amp, effectively clipping it.

However, the bottom part of the output square wave is close to -4V, not 0V, as would be expected of a digital signal. A clipping diode can be added off the op amp output signal and applied to a 100 kΩ load resistor. This removes most of the negative going part of the periodic signal.

Two CMOS inverters were added after the 100 kΩ load resistor, and fed to another 100 kΩ load resistor to square up the signal <see below>.

PSpice Simulated Wain Bridge Oscillator
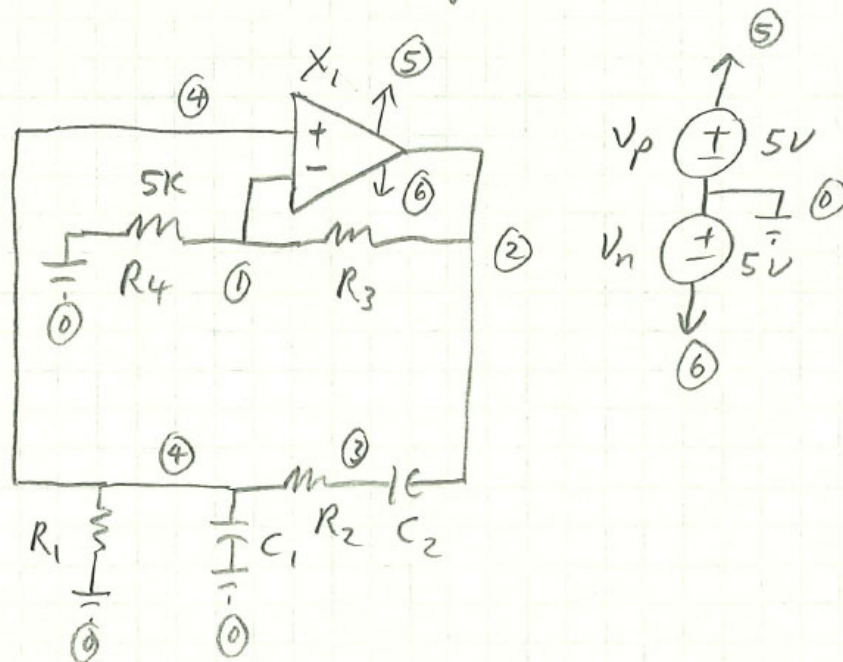
$$f = \frac{1}{2\pi RC} = \frac{1}{2\pi (159.155)(1\times10^{-6})} = 1000 \text{ kHz}$$

$$C_1 = C_2 = 1\mu F$$

$$R_1 = R_2 = 159.155 \Omega$$

$$1 + \frac{R_3}{R_4} = 3 \rightarrow R_4 = 5k\Omega, \; R_3 = 10 k\Omega$$

X_1: AD8610 op amp $\rightarrow$ 25 MHz GBW product
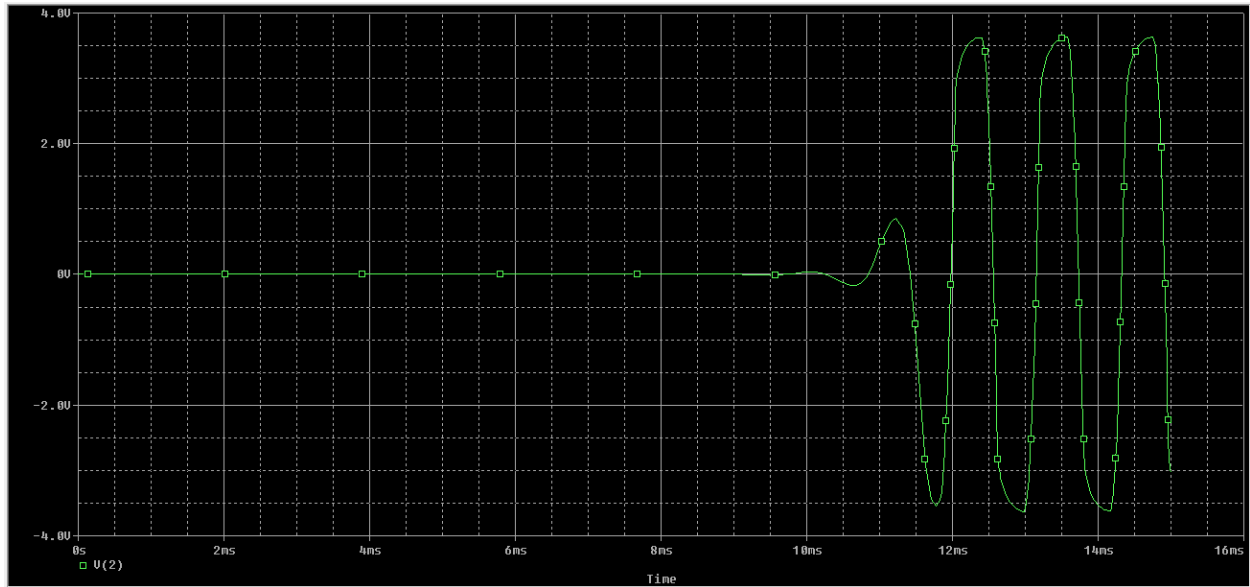
Result $\rightarrow$ no oscillation

∴ R_3 increased to 15 kΩ to achieve oscillation
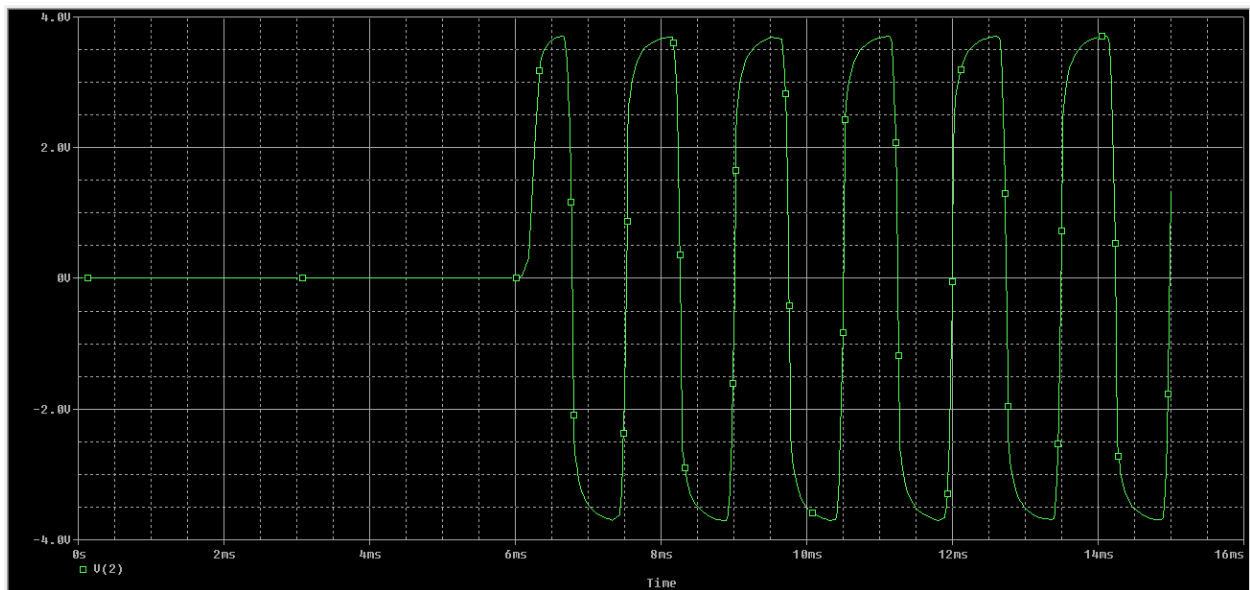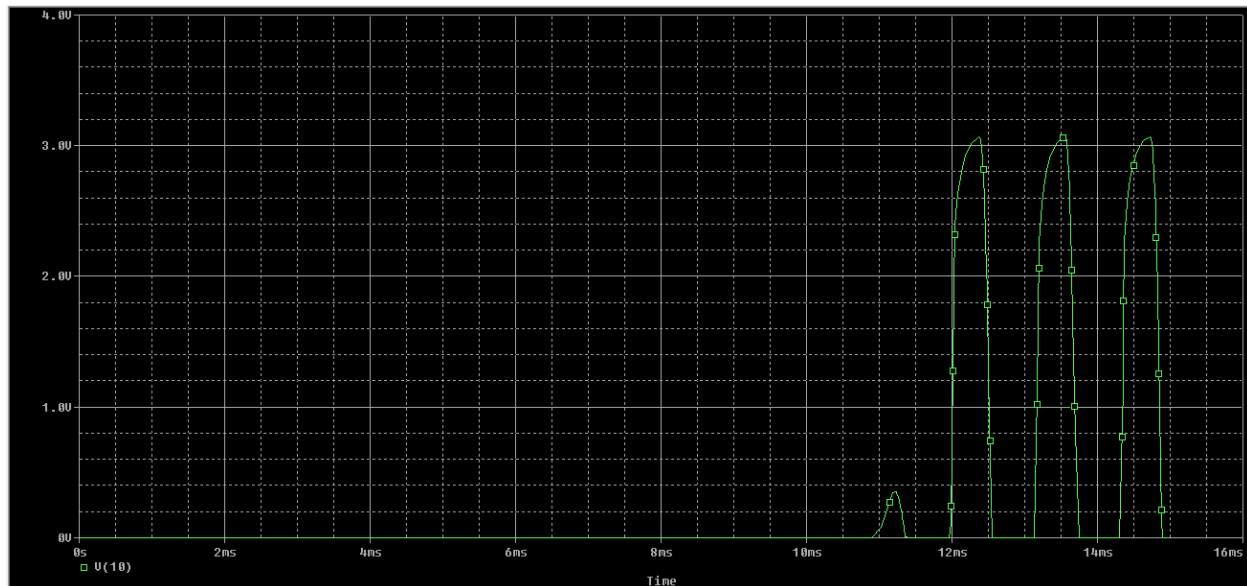Output: Distorted sinusoid: $f = 857.93$ Hz
Possible causes for lower freq:
  ① phase shift in op amp
  ② nonlinear distortion near power supply rails

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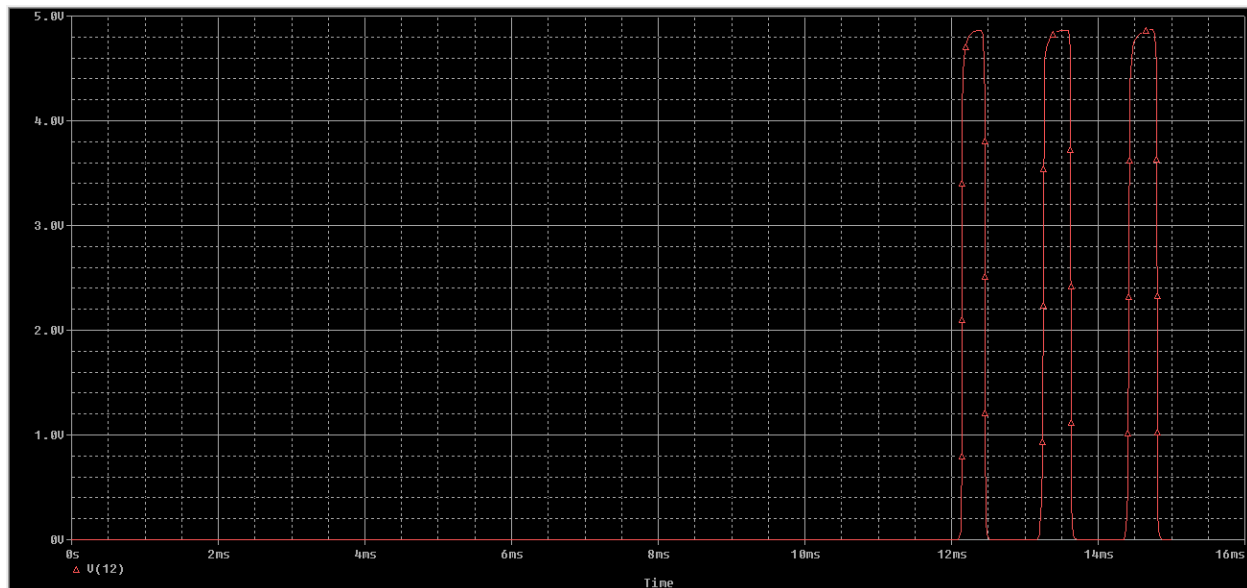
V(2) with R3 = 15 kΩ

V(2) with R3 = 25 kΩ

Voltage waveform after the diode. Observe that the peak voltage has dropped due to the forward voltage drop across the diode.
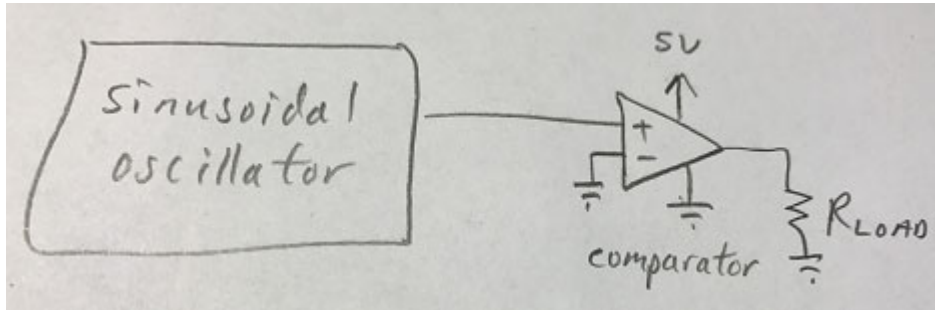

Voltage waveform after two CMOS inverters following the clipping diode circuit.

The duty cycle is less than 50%, but this is usually not a problem for many applications.

2) A rail-to-rail comparator added to the sinusoidal oscillator's output

This circuit can convert the sinusoidal output waveform into a square wave.

More on Nonlinear Oscillators
    a. Terminology

The term <u>Multivibrator</u> is often used in texts describing nonlinear oscillators. A multivibrator is an electronic circuit that switches between 2 states and consists of two amplifying devices cross-coupled with resistors and capacitors:

1. Astable Multivibrator: a multivibrator circuit where neither state is stable. It continually switches back and forth between the two states.

2. Monostable Multivibrator: a multivibrator circuit with one stable state and one unstable state. A trigger pulse causes the circuit to temporarily switch to the unstable state, where the circuit eventually switches back to the stable state and then stays there until another trigger pulse is applied. A "One Shot" is a monostable multivibrator.

3. Bistable Multivibrator: a multivibrator with two stable states. A trigger pulse is required to change either state. A flipflop is a bistable multivibrator.

A <u>Relaxation Oscillator</u> is an astable multivibrator that uses an active circuit element to charge an inductor or a capacitor through a resistor until a threshold current or voltage is reached, where the circuit then changes states and discharges or recharges the inductor or capacitor. The time constant of the inductor or capacitor circuit determines the oscillation frequency.

A <u>Ring Oscillator</u> consists of an odd number (n > 1) of inverters (NOT gates) connected in a continuous closed chain. The odd number results in the impossibility of a stable condition, so the circuit oscillates, and the oscillation frequency is due to the propagation delay through each inverter $(T = 2n\tau_D)$. Adding more inverters to the chain reduces the oscillation frequency.

b. Time constant trigger for a state change

Consider the RC circuit below:
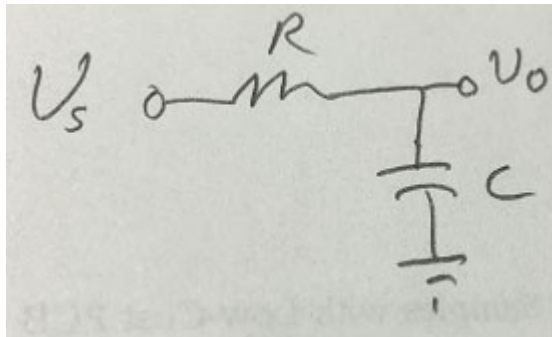
Initially, C has no stored charge $(V_o = 0V)$. At t=0, a positive DC voltage, V_s, is applied to the resistor. V_o will increase until it reaches a trip voltage level, t_{tr} s later.

$$V_o(s) = V_s(s)\frac{\frac{1}{sC}}{R + \frac{1}{sC}}$$

$$V_o(s) = V_s(s)\frac{\frac{1}{RC}}{s + \frac{1}{RC}}$$

$$V_s(s) = \frac{v_s}{s}$$

$$V_o(s) = \frac{v_s}{s}\frac{\frac{1}{RC}}{s + \frac{1}{RC}} = \frac{A}{s} + \frac{B}{s + \frac{1}{RC}}$$

Using partial fraction expansion:

$$A = \frac{v_s \dfrac{1}{RC}}{0 + \dfrac{1}{RC}} = v_s$$

$$B = \frac{v_s \dfrac{1}{RC}}{-\dfrac{1}{RC}} = -v_s$$

Therefore:

$$V_o(s) = \frac{v_s}{s} - \frac{v_s}{s + \dfrac{1}{RC}}$$

$$v_o(t) = v_s(1 - e^{-\frac{t}{RC}})$$

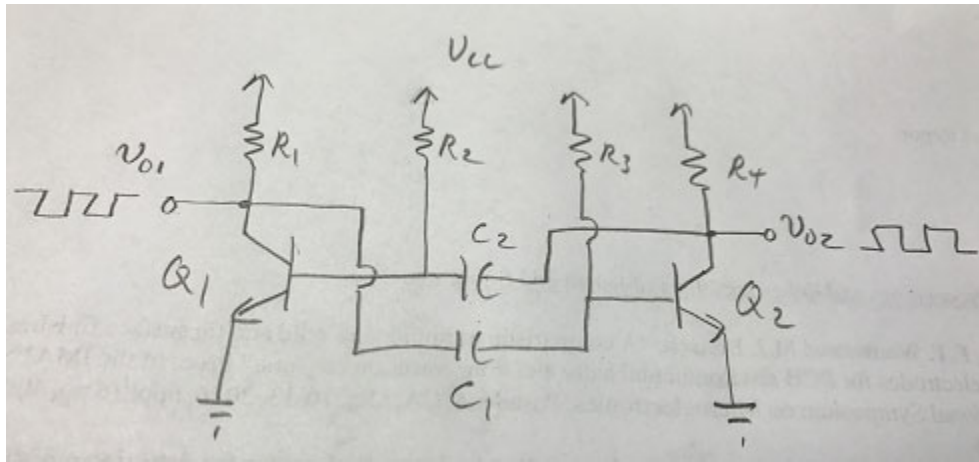Rearranging terms:

$$\frac{v_o}{v_s} = 1 - e^{-\frac{t}{RC}}$$

$$e^{-\frac{t}{RC}} = 1 - \frac{v_o}{v_s}$$

$$-\frac{t}{RC} = \ln\left(1 - \frac{v_o}{v_s}\right)$$

$$t = -RC\left[\ln\left(1 - \frac{v_o}{v_s}\right)\right]$$

τ is defined here as the time, t, it takes for $v_o(t)$ to reach the trip voltage level to cause the multivibrator circuit to change states. For an astable multivibrator with 2 time constant trip circuits, τ_1 and τ_2: $T \approx \tau_1 + \tau_2$.

c. 2 transistor classical astable multivibrator circuit

Q_1 and Q_2 are identical NPN transistors. Let's let $V_{cc} = 5V$.

$C_1 = C_2$

$R_1 = R_4$, and are relatively small

$R_2 = R_3$

For $v_{BE} < 0.7V$, Q_1 and Q_2 are in cutoff ($I_c = 0A$)

Assume that Q_1 is on ($v_{BE} = 0.7V$) and Q_2 is in cutoff.

The left plate of C_1 is approximately at 0V (gnd) while the right plate is tied to V_{cc} through R_3, charging it up.

The left plate of C_2 is held at approx. 0.7 V (v_{BE} of Q_1) while the right plate is held at approximately V_{cc} (~5V) through R_4 with Q_2's $I_c = 0V$)

Once the right plate of C_1 reaches 0.7V, Q_2 turns on (the right plate of C_2 drops to approx. 0V (gnd). Since the voltage across a capacitor cannot change instantaneously, the left plate voltage of C_2 drops from 0.7V to -4.3V, turning off Q_1.

C_2 then starts charging through R_2 until the Q_1's v_{BE} reaches 0.7V …

Therefore, τ_1 is set by C_1R_3 and τ_2 is set by C_2R_2.

$$f \approx \frac{1}{\tau_1 + \tau_2}$$
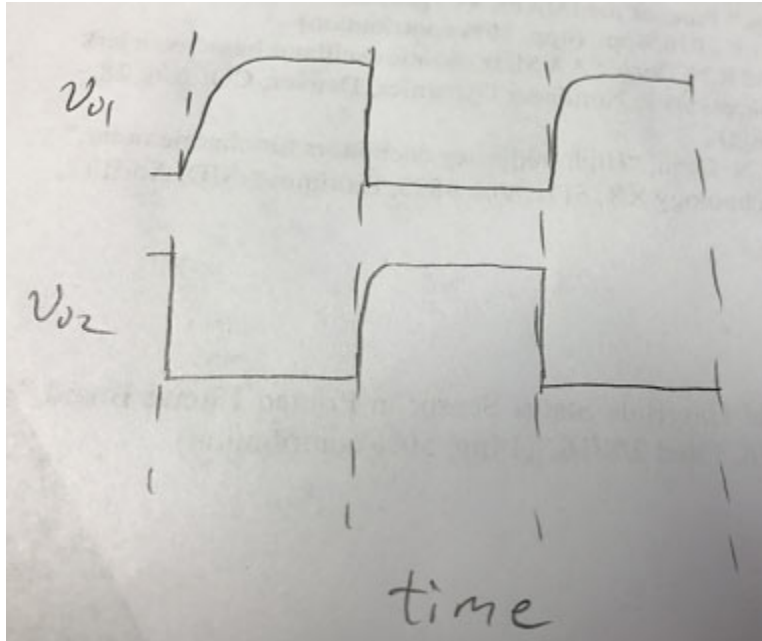
Approximate waveforms for $v_{o1}(t)$ and $v_{o2}(t)$.

The output voltages, $v_{o1}(t)$ and $v_{o2}(t)$, are inverted. The logic level "1" is V_{cc}. The exponential rise when either output voltage goes high is due to the capacitors charging through R_1 and R_4, respectively.

Application
Let V_{cc} be 12V (instead of 5V) and "gnd" be -12V (instead of 0V). Connect $v_{o1}(t)$ to $v_{o2}(t)$ through the secondary of a 10:1 transformer. The voltage across the primary of the transformer switches between 120V and -120V and is approximately a square wave. The circuit is now a simple DC to AC inverter for power applications, useful for non-sinusoidal power applications.