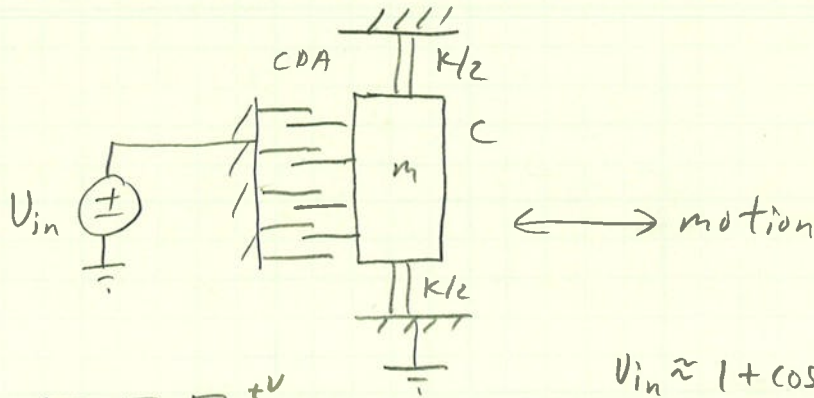


1. MEMS Electrostatic Resonators

consider this device:

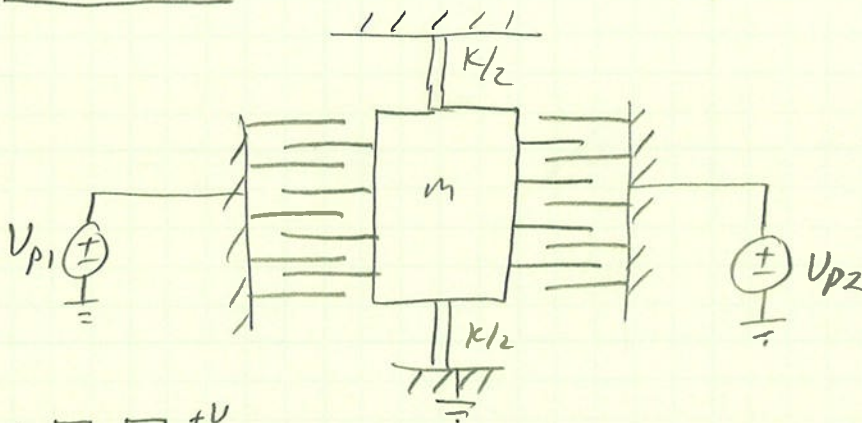


V_{in} : $f = f_n = \frac{1}{2\pi} \sqrt{\frac{K}{m}}$

$V_{in} \approx 1 + \cos(\omega t)$
 $\therefore V_{in}^2 \approx 1.5 + 2 \cos(\omega t) + 0.5 \cos(2\omega t)$

although V_{in} is a square wave, motion is nearly sinusoidal due to high Q of MEMS devices

a. Dual drive



V_{p1} : V_{p2} : } 180° out of phase, $f = f_n$

proof mass oscillates at ω_n

Applications: (1) MEMS vibratory gyroscope

(2) low P pressure sensor

(3) RF filter elements , (4) variable mass-detection sensor

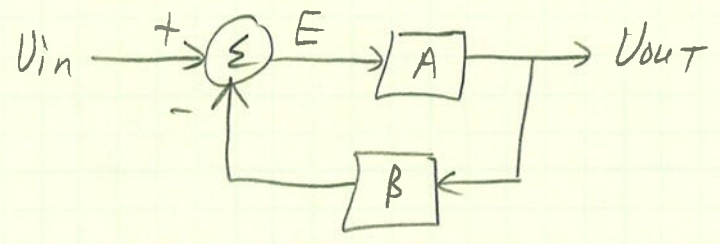
Problems with this approach:

- (1) Must tune V_{p1} and V_{p2} to ω_n
- (2) ω_n may change due to temperature, aging, etc.
- (3) harmonics of V_{p1} and V_{p2} may excite unwanted vibration modes in the mechanical system

→ ∴ use the MEMS device to realize a feedback sinusoidal oscillator

2. Review of Sinewave Oscillators

Consider this system:



$E \rightarrow$ "error signal"

$A + B$ are gains

$AB \equiv$ loop gain

(1) $E = V_{in} - BV_{out}$

(2) $V_{out} = EA$

(1) \rightarrow (2): $V_{out} = A[V_{in} - BV_{out}]$

$$V_{out}[1 + AB] = AV_{in}$$

$$\frac{V_{out}}{V_{in}} = \frac{A}{1 + AB}$$