

Fixed-Value and Stem Unobservability Theorems for Logic Redundancy Identification

September 14, 2003

Abstract – *There is a class of implication-based methods that identify logic redundancy from circuit topology and without any primary input assignment. These methods are less complex than automatic test pattern generation (ATPG) but identify only a subset of all redundancies. This paper provides new results to enlarge this subset. Contributions are a fixed-value theorem and two theorems on fanout stem unobservability. We represent signal controllabilities and observabilities using an implication graph and its transitive closure (TC). Both complete and partial implications are included. Weaknesses of this procedure are in dealing with the effects of fixed-valued variables on TC and the lack of observability relations across fanouts. The fixed-value theorem adds unconditional edges from all variables to the fixed variable and then recomputes TC recursively until no new fixed nodes are found. The stem unobservability theorems determine the observability status of a fanout stem from its dominator set, which either has fixed values, or is unobservable. Results are considerably improved from the previously reported implication-based identifiers. In the c5315 circuit we identify 58 out of 59 redundant faults. All 34 redundant faults of c6288 are identified.*

1. Introduction

Redundancy removal ensures that a circuit does not have unnecessary logic gates, which increase the chip area, power consumption and propagation delay [2, 18]. Another reason why redundancies should be identified is the reliability of the circuit. In the presence of redundant faults some testable faults may be masked. There are three different approaches to redundancy identification: *automatic test pattern generation* (ATPG) [4, 5, 8, 12, 15, 16, 23, 25, 27, 28], testability analysis where depending on the type of method we use, i.e., exact or approximate, we can identify all or a subset of “probably” redundant faults [9, 20, 22, 26], and implication-based methods [1, 7, 11, 13, 18, 19].

ATPG methods can find all redundant faults but they have very high complexity. Testability analysis, often restricted to a linear complexity, can identify “hard to test” faults some of which may be redundant. Implication-based methods do not guarantee to find all redundant

faults and their complexity is polynomial. Both testability analysis and implication-based algorithms do not target specific faults and are sometimes referred to as “fault-independent methods.”

Chakradhar *et al.* [3] define a Boolean false function to construct an implication graph from a given gate level netlist. Both true and false status of the signal line is represented by nodes in the implication graph. Pair-wise relationships of signal lines provide implication edges in the graph. Signal dependencies derived from the transitive closure are used to reduce ternary relations to binary relations that in turn dynamically update the transitive closure. When the ATPG problem is posed as Boolean satisfiability, the implication graph provides useful help in solving it. Recent work has produced several ATPG programs that use Boolean satisfiability [4, 12, 16, 27, 28].

The implication graph and transitive closure have also been used in fault-independent approaches to redundancy identification [1]. Here observabilities of signals are represented as additional Boolean variables in the implication graph. Gaur *et al.* [6, 7] improved such a redundancy identification technique, using a subset of all partial implications derived from the higher order terms represented using *anding* nodes. Mehta *et al.* [18] implemented all the unimplemented direct and partial implications and this improved the results considerably. The nodes in the graph represent the true and false status of the signal lines and true and false status of the observability of those signal lines. Directed edges represent the Boolean implication relationships between nodes. The motivation for the present work comes from the weaknesses of the existing technique. An analysis of redundant faults found by an ATPG program that could not be identified by the implication method shows:

- The circuit topology forces some signals to fixed values. The implication graph procedures could not analyze the effect when a set of fixed signals influence the state of another signal.
- There is no generally known procedure to determine the observability status of a fanout stem even when the fanout branches were unobservable or had fixed values.

Among the contributors to the non-graph based implication approaches are Iyer and Abramovici [13], Peng *et al.* [21], and Zhao *et al.* [29].

In Section 2, a theorem for fixed-value nodes. Stem unobservability theorems are discussed in Section 3. Section 4 proposes improvements in the graph technique based on the Boolean contrapositive law. Limitations of our technique are given in Section 5. Results are discussed in Section 6. Section 7 presents the conclusion of this paper.

2 Fixed-Valued Nodes

A Boolean variable x is represented by two nodes x and \bar{x} in the implication graph. Each node can be in a true or false state. When $x = 1$, node x is true and \bar{x} is false, and vice-versa. The variable x assumes a fixed value 0 if there exists an edge $x \rightarrow \bar{x}$ in the implication graph. Similarly, x assumes a fixed value 1 when the edge $\bar{x} \rightarrow x$ exists. When several nodes have fixed-values, we have found some limitations of the previously described transitive closure technique [6] in identifying certain redundancies. We consider:

- A primary output AND or NOR gate with an unexcitable s-a-1 redundant fault on its output line (see g s-a-1 in Figure 1).
- A primary output OR or NAND gate with an unexcitable s-a-0 redundant fault on its output line.

The following theorem identifies the above mentioned redundancies.

Theorem 2.1 (Fixed-value) *If a Boolean variable in the implication graph is fixed to a true (false) value then there exist unconditional edges from all other nodes in the graph to the node representing the true (false) state of the fixed variable.*

Proof: Consider a fixed signal, $a = 0$. Then, there exists an edge from node a to \bar{a} in the graph (where a and \bar{a} represent true and complement values of signal line a in the circuit), then irrespective of the status of all other nodes in the graph, \bar{a} will be unconditionally true. This “unconditional truth” must be implied by all variables. In other words, there must be edges added from all the nodes in the graph to the node \bar{a} . ■

The example circuit shown in Figure 1 has 7 redundant faults. Previous work [6] could identify s-a-1 faults on lines e and f . They could not identify the other redundant faults: s-a-1 on line g because $e = f = 1$ did not imply $g = 1$ in the graph, and s-a-0 and s-a-1 on lines a and b were not identified due to a lack of stem unobservability relationships.

Without Theorem 2.1, we could not identify s-a-1 on line g as redundant. Figure 2 shows a part of the implication graph. The edges other than the three outgoing

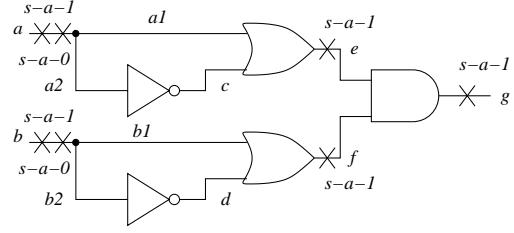


Figure 1: Example circuit with fixed-value nodes.

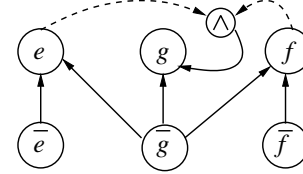


Figure 2: A part of implication graph that identifies $g = 1$ using Theorem 2.1.

edges from \bar{g} exist in the transitive closure. The faults e s-a-1 and f s-a-1 are identified to be redundant due to edges from nodes \bar{e} and \bar{f} in the transitive closure graph to nodes e and f , respectively. These faults are classified as unexcitable redundant faults. As these nodes are fixed to logic value 1, according to Theorem 2.1, we add unconditional edges from all other nodes in the graph to nodes e and f . This includes two edges from g to e and f , respectively. The transitive closure is obtained by a graph traversal from each node to determine its reachability. Traversal proceeds through an *anding* node (labeled as \wedge in Figure 2) only when paths arrive through all incoming edges. In this case, therefore, when we start at \bar{g} , g is reached and the edge $\bar{g} \rightarrow g$ is added. This sets g to a fixed value 1 and identifies the s-a-1 fault on line g as redundant. The other four faults, a and b s-a-0 and s-a-1, are not yet identified due to the absence of any false stem observability edges. These faults are identified as redundant with the theorems introduced in the next section.

3 Stem Unobservability Theorems

We define the *dominator set* of a fanout stem in a circuit as a minimal set of signals through which all forward paths originating at the stem must pass. Trivially, a dominator set for any signal can be found as the set of reachable primary outputs (POs). A dominator set consisting of a single signal is called a *unique dominator*. Our definition is consistent with the graph theory [10] and has also been used in an ATPG algorithm [14].

Theorem 3.1 (Stem unobservability) *A fanout stem is unobservable, if each signal in its dominator set assumes a constant value and:*

- the fanout stem does not hold a constant value, or
- the fanout stem holds a constant value and, in spite

of any local change in the stem signal, the dominator set values do not change.

A local change of a signal only affects the portion of the circuit between that signal and POs.

Proof: From the definition of the dominator set, if the stem under consideration is unobservable at the dominator set then it will be unobservable at primary outputs as well. So:

$$f_i(X, x_p) = c \quad (1)$$

where X is the set of primary inputs, x_p is the fanout stem under consideration, f_i is the dominator set function, that is a function of X and x_p and $i \in [1, k]$, where k is the cardinality of the dominator set and c is a constant, which can assume a logic 0 or 1 value. Expanding Equation 1 using Shannon's expansion theorem [2], we get:

$$x_p f_i(X, 1) + \overline{x_p} f_i(X, 0) = c \quad (2)$$

We consider two cases:

- $x_p \neq$ constant, then Equation 2 implies:

$$f_i(X, 1) = f_i(X, 0) = c \quad (3)$$

Taking the Boolean difference of dominator functions with respect to x_p , we get:

$$\frac{\partial f_i(X, x_p)}{\partial x_p} = f_i(X, 1) \oplus f_i(X, 0) \quad (4)$$

From Equation 3:

$$\frac{\partial f_i(X, x_p)}{\partial x_p} = c \oplus c = 0 \quad (5)$$

Thus, x_p is unobservable.

- $x_p =$ constant. Substituting $x_p = 1$ in Equation 2, we get:

$$f_i(X, 1) = c \text{ and } f_i(X, 0) = \text{unknown} \quad (6)$$

and substituting $x_p = 0$ in Equation 2, we get:

$$f_i(X, 1) = \text{unknown} \text{ and } f_i(X, 0) = c \quad (7)$$

The Boolean difference of of dominator functions with respect to x_p is:

$$\frac{\partial f_i(X, x_p)}{\partial x_p} = f_i(X, 1) \oplus f_i(X, 0) \neq 0 \quad (8)$$

In the special case, when $f_i(X, 1) = f_i(X, 0) = c$, i.e., $f_i(X, x_p)$ remains unchanged when x_p assumes two different values, Equation 8 evaluates to 0 and the stem x_p becomes unobservable. ■

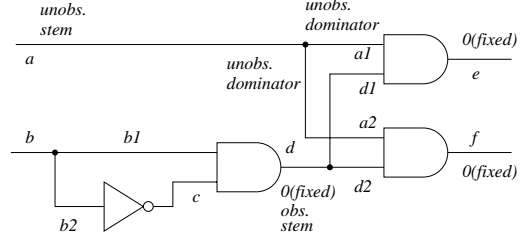


Figure 3: An illustrative example of Theorem 3.2.

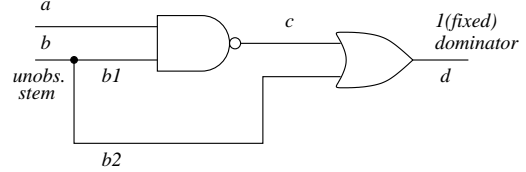


Figure 4: An illustrative example of Theorem 3.1.

Theorem 3.2 (Stem unobservability) A fanout stem is unobservable, if each signal in its dominator set is unobservable and:

- the stem does not hold a constant value, or
- the stem holds a constant value and, in spite of any local change in the stem signal, the unobservable status of the dominator set remains unchanged.

Proof: To be provided in the final submission of the paper. ■

The fanout stem b , shown in Figure 3, is not fixed and the dominator d has a constant value of 0. Thus, Theorem 3.1 identifies fanout stem b as unobservable. The fanout stem d , shown in Figure 3, is fixed to 0 and the dominator set $\{e, f\}$ holds a constant value of $\{0, 0\}$. Thus, Theorem 3.1, locally changes the value of d and checks the effect on the dominator set, which is found to be changed. Thus, Theorem 3.1 does not identify d as an unobservable stem. The fanout stem a , shown in the same figure, is not fixed and the dominator set signals $\{e, f\}$ are fixed to 0. Thus, Theorem 3.2 identifies a as an unobservable fanout stem. The fanout stem b , shown in Figure 4, is not fixed and the dominator d is fixed to 1. Thus, Theorem 3.1 identifies b as an unobservable fanout stem. The fanout stem c , shown in Figure 5, is fixed to 0 and the dominator set signals $\{c1, c2\}$ are unobservable. A change in the value of c changes the observability status of the dominator set. Thus, Theorem 3.2 does not identify c as an unobservable stem. Theorem 3.2 is consistent with a lemma given by Iyer and Abramovici [13]. Their lemma is a special case of the Theorem 3.2 because the theorem does not require the uncontrollability indicator condition required by the lemma. After the observability status of a fanout stem is decided, an unobservability edge is implemented in the implication graph.

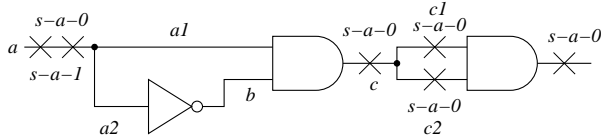


Figure 5: A circuit with observable and unobservable stems (all faults shown are redundant).

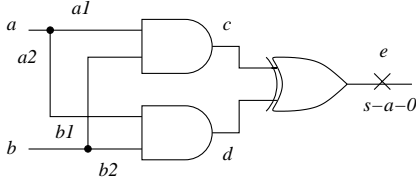


Figure 6: Example circuit showing the identification of redundant fault e s-a-0 due to contrapositive edges.

4 Using the Contrapositive Law

According to the contrapositive law, if there exists an edge from node p to node q then there must also exist an edge from node \bar{q} to \bar{p} [17, 24, 29]. The use of this concept further increases the number of redundant faults identified in combinational logic circuits, which is evident from the example circuit of Figure 6. Figure 7 shows the transitive closure graph for the circuit of Figure 6. Node c implies a and b , while a and b through an *anding* node (\wedge) imply d , so transitive closure graph has an edge from node c to node d . Similarly, we get an edge from node d to node c . The contrapositive edges for these two edges are: \bar{d} implying \bar{c} and \bar{c} implying \bar{d} , respectively. Now, from node c another *anding* node becomes true (with node d , implying \bar{e}). So, we get, another transitive closure edge from c to \bar{e} and its contrapositive from node e to node \bar{c} . Also, we get a transitive closure edge from \bar{c} to \bar{e} . Now, if we start our traversal from node e , we get implication to \bar{c} and \bar{c} implies \bar{e} . Thus, we get an transitive closure edge from e to \bar{e} (shown bold in Figure 7), which identifies s-a-0 fault on line e to be redundant. The results of Section 6 (Table 1) does not contain the implementation of the contrapositive rule.

5 Limitations

The fanout stem a in Figure 8 is unobservable and the dominator sets for stem a are neither fixed nor unobservable. Thus, Theorems 3.1 and 3.2 fail to identify the unobservability status of stem a .

Figure 9 shows a circuit with six redundant faults as found by an ATPG program. The fanout stem c could not be classified as unobservable by our theorems because no fixed-valued or unobservable dominator sets are found. So, the redundant faults c s-a-1 and s-a-0 could not be identified redundant by our technique. Faults a s-a-1, $c1$ s-a-1, and d s-a-1 are identified as redundant. The fault e s-a-1 is not identified because we do not have enough implications to traverse backwards from the true

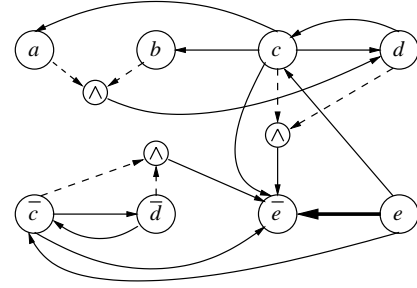


Figure 7: A part of transitive closure with contrapositive edges to find redundant e s-a-0 fault in Figure 6.

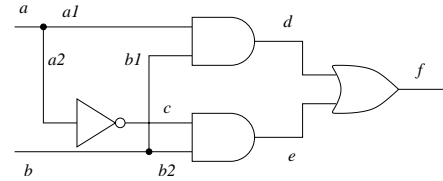


Figure 8: Example of an unobservable stem not identified by stem unobservability theorems.

node of the output of NAND gate towards its inputs, i.e., we do not have implications to traverse backwards from the true nodes of signal f and g of Figure 9. Due to this, we can not get an implication to identify the undrivable redundant fault e s-a-1. An extended implication method in which sets of signals are enumerated to check for essential assignments can identify such a redundancy at a higher computation cost [21]. The three redundant faults not identified in the circuit c432 are of this type (refer to Table 1).

6 Results

Table 1 shows the results obtained on ISCAS '85 and ISCAS '89 benchmark circuits. The first column shows the names of benchmark circuits for which results from various programs are compared with respect to the redundant faults identified and their respective CPU times. The next column shows the total number of collapsed single faults in the circuit. The next two columns show the redundant faults identified and CPU time in seconds for the ATPG tool TRAN [4] by Chakradhar *et al.*, which uses transitive closure for test generation. The next two columns lists the result of FIRE [13] by Iyer and Abramovici. The next two columns show the results of the transitive closure algorithm without partial implications by Agrawal *et al.* [1]. The next two columns show the result of the transitive closure algorithm with some of the partial implications by Gaur *et al.* [7]. The last two columns are the results of the new fault-independent algorithm, which uses transitive closure for redundancy identification. The sequential benchmark circuits were converted into combinational circuits by removing the flip-flops from the circuit and treating flip-flop outputs as primary inputs and flip-flop inputs as primary outputs.

Table 1: Combinationally redundant faults in ISCAS '85 and ISCAS '89 benchmark circuits.

Circuit	Total faults	Redundant faults identified and run time on Sun workstations (a: Sparc 5; b: Sparc 2)									
		<i>TRAN</i> [4]		<i>FIRE</i> [13]		<i>TC</i> [1]		<i>TC_{w-partial}</i> [7]		<i>Our Algo.</i>	
		Redun. faults	CPU s (a)	Redun. faults	CPU s (b)	Redun. faults	CPU s (a)	Redun. faults	CPU s (a)	Redun. faults	CPU s (a)
c432	524	4	0.8	-	-	0	0.1	0	0.2	1	0.2
c499	758	8	1.8	-	-	0	0.2	0	0.2	0	1.3
c880	942	0	4.0	-	-	0	0.3	0	0.4	0	0.4
c1355	1574	8	11.0	-	-	0	0.7	0	0.9	0	1.9
c1908	1879	7	13.0	6	1.8	2	0.8	2	0.9	2	3.2
c2670	2747	115	95.2	29	1.5	23	1.3	25	1.5	82	4.0
c3540	3428	131	24.9	93	11.9	54	5.9	74	6.2	111	16.2
c5315	5350	59	32.3	20	2.8	20	3.4	32	3.4	58	3.9
c6288	7744	34	38.0	33	1.3	31	1.0	31	1.8	34	7.2
c7552	7550	131	308.0	30	4.7	32	5.2	34	5.8	55	11.5
s349	350	2	0.3	2	0.2	1	0.1	2	0.2	2	0.2
s444	474	14	0.4	11	0.2	2	0.1	8	0.2	10	0.3
s713	581	38	3.1	32	0.1	29	0.3	35	0.3	38	0.6
s1238	1355	69	17.4	6	1.9	4	0.5	6	0.6	20	2.6
s1423	1515	14	8.5	5	0.3	4	0.6	8	0.7	12	1.0
s1494	1506	12	3.7	1	1.1	1	0.7	1	0.8	2	8.8
s5378	4603	40	73.0	34	3.7	20	2.5	22	3.0	27	8.3
s9234	6927	452	803.7	165	20.6	16	9.8	135	11.2	233	106.0
s13207	9815	151	806.5	55	23.2	9	11.2	60	13.6	77	158.8

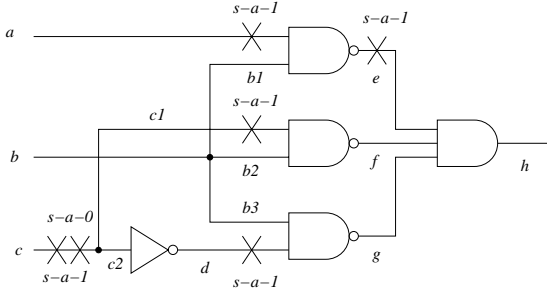


Figure 9: Another example of limitations.

There are no aborted faults in TRAN [4] for all circuits in Table 1. We use benchmark circuit c5315 to compare results for all these different programs with our work. The ATPG tool TRAN [4] identifies all the 59 redundant faults in the circuit without aborting any fault in CPU time of 32.3 sec. FIRE [13] identifies 20 redundant faults with a CPU time of 2.8 sec. Next, the transitive closure algorithm without partial implication [1] identifies 20 redundant faults with CPU time of 3.4 sec. Next, the transitive closure algorithm with some partial implications [7] identifies 32 redundant faults with CPU time of 3.4 sec. Finally, our algorithm with the fixed-value theorem and stem unobservability theorems implemented identifies 58 redundant faults in 3.9 sec. Thus, in the benchmark circuit c5315 our algorithm identifies more redundant faults than any of the fault independent algorithms. The redundant faults identified by our work are much greater than all the other implication-based methods described in the result table with comparable CPU time. The results are also comparable to the ATPG tool

TRAN because for the benchmark circuits c3540, c5315, c6288, s349, s444, s713, s1423 and s9234 our work provides either all or close to all redundant faults. We do recognize that there are ATPG programs [28] that are faster than TRAN, but then our present implementation is only experimental with many potential performance improvements possible.

An analysis of the benchmark circuit c432 reveals that due to the inability to take decision (*i.e.*, traverse backwards from the false node of the output of the AND gate, shown in Section 2) we can not identify 3 out of 4 redundant faults (*i.e.*, we identify only 1 out of 4 redundant faults.)

7 Conclusion

The fixed-value theorem and stem unobservability theorems enhance the transitive closure technique to identify redundant faults. Its other applications, not discussed here but under investigation, include the identification of the equivalent faults and equivalence checking of two given circuits. Future research may find new ways of taking decisions in the implication graph to traverse from the false status of the output signal of an AND gate. However, our technique retains a lower complexity than the exponential complexity of an ATPG algorithm and identifies many, though not all, redundant faults.

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