

## 4 Homework: Velocity and Acceleration Analysis

### Part I

#### Problem 4.1: four-bar mechanism

The four-bar mechanism shown in Fig. P4.1 has the dimensions:  $AB=CD=0.04$  m and  $AD=BC=0.09$  m. The driver link  $AB$  rotates with a constant angular speed of 120 rpm. Find the velocities and the accelerations of the four-bar mechanism for the case when the angle of the driver link  $AB$  with the horizontal axis is  $\phi=30^\circ$ . For  $\phi=30^\circ$  the position of the mechanism is given by:  $x_B=0.034641$  m,  $y_B=0.02$  m,  $x_C=0.103859$  m,  $y_C=-0.0375222$  m,  $\phi_2=-39.7274^\circ$ ,  $\phi_3=-69.7274^\circ$ .

#### Results

$$\begin{aligned} \dot{x}_B &= -0.251327 \text{ m/s}, \quad \dot{y}_B = 0.435312 \text{ m/s}, \quad \ddot{x}_B = -5.47029 \text{ m/s}^2, \quad \ddot{y}_B = -3.15827 \text{ m/s}^2, \\ \dot{x}_C &= -0.884619 \text{ m/s}, \quad \dot{y}_C = -0.32675 \text{ m/s}, \quad \ddot{x}_C = 3.84741 \text{ m/s}^2, \quad \ddot{y}_C = 25.1222 \text{ m/s}^2, \\ \omega_2 &= \dot{\phi}_2 = -11.0095 \text{ rad/s}, \quad \alpha_2 = \ddot{\phi}_2 = 307.84 \text{ rad/s}^2, \\ \omega_3 &= \dot{\phi}_3 = -23.5759 \text{ rad/s}, \quad \alpha_3 = \ddot{\phi}_3 = 307.84 \text{ rad/s}^2. \end{aligned}$$

#### Problem 4.2: slider crank mechanism

The slider crank mechanism shown in Fig. P4.2 has the dimensions:  $AB = 0.1$  m and  $BC = 0.2$  m. The driver link 1 rotates with a constant angular speed of  $n = 60$  rpm. Find the velocity and acceleration of the slider 3 when the angle of the driver link with the horizontal axis is  $\phi = 45^\circ$ . For  $\phi=45^\circ$  the position of the mechanism is given by:  $x_B=0.0707107$  m,  $y_B=0.0707107$  m,  $x_C=0.257794$  m,  $y_C=0$  m,  $\phi_2=-0.361367$  rad.

#### Results

$$\begin{aligned} \dot{x}_B &= -0.444288 \text{ m/s}, \quad \dot{y}_B = 0.444288 \text{ m/s}, \quad \ddot{x}_B = -2.79155 \text{ m/s}^2, \quad \ddot{y}_B = -2.79155 \text{ m/s}^2, \\ \dot{x}_C &= -0.612213 \text{ m/s}, \quad \dot{y}_C = 0 \text{ m/s}, \quad \ddot{x}_C = -2.94227 \text{ m/s}^2, \quad \ddot{y}_C = 0 \text{ m/s}^2, \\ \omega_2 &= \dot{\phi}_2 = -2.37482 \text{ rad/s}, \quad \alpha_2 = \ddot{\phi}_2 = 12.7898 \text{ rad/s}^2. \end{aligned}$$

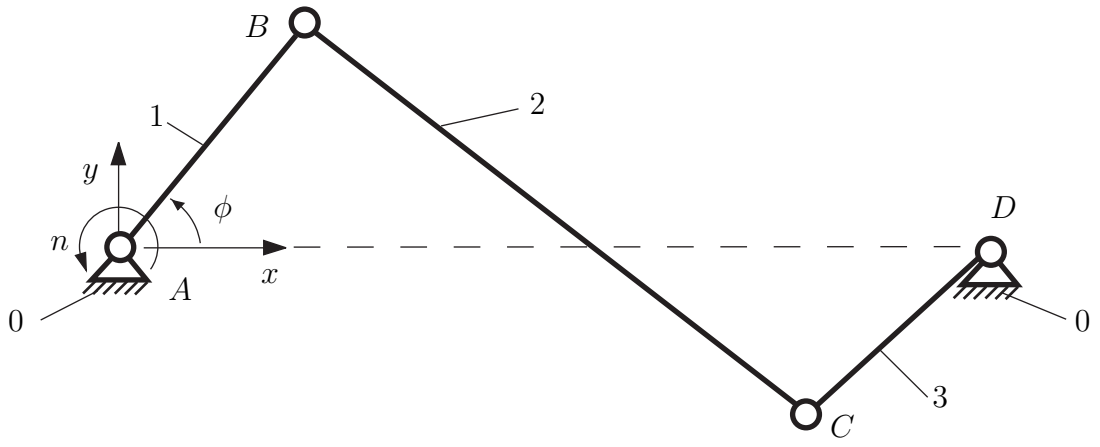


Figure P4.1

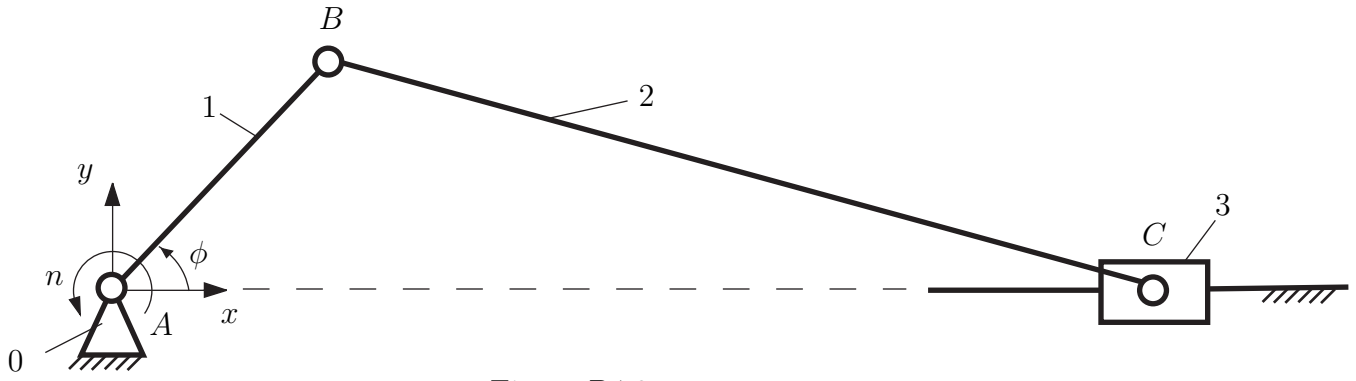


Figure P4.2